

# Poisson-Fermi Model of the Ion-exchange Mechanism of the SODIUM/CALCIUM exchanger NCX

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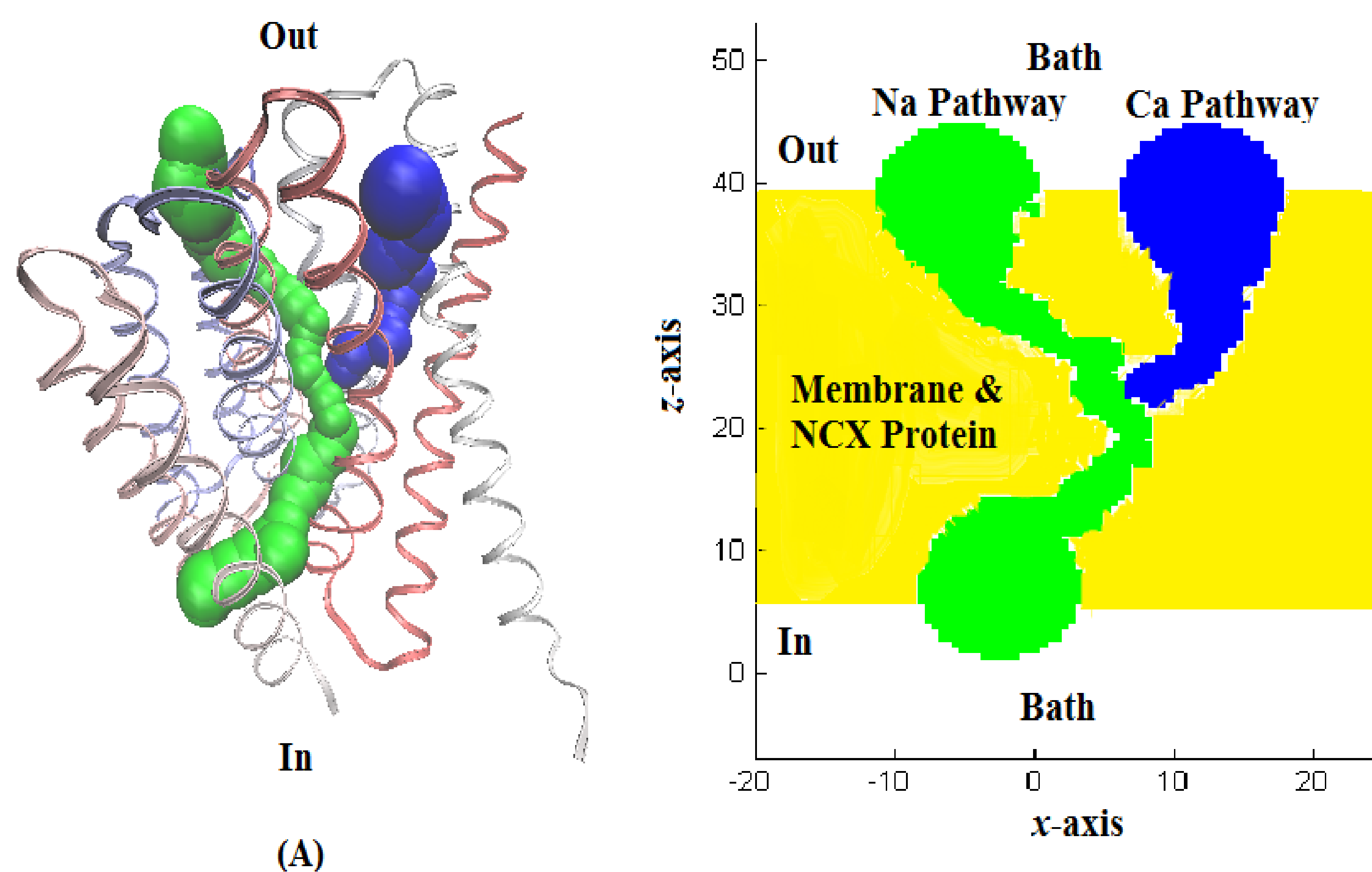
## Abstract

Ion-exchange mechanism of the **NCX transporter** crystallized by Liao, Li, Zeng, Sauer, Belmares, and Jiang *Science* (2012) 335:686 is studied using the **Fermi Poisson theory** developed by Jinn Liang Liu, *Journal of Computational Physics* (2013) 247:88 and Jinn Liang Liu and Bob Eisenberg *Journal of Physical Chemistry B* (2013) 117:12051 *J Chem Phys* (2014) 141:07510; *J Chem Phys* (2014) 141:22D532 arXiv:1506.06203 *Physical Review E* (2015) 92: 012711 arXiv: 1506.05953 *Chemical Physics Letters* (2015) 637:1

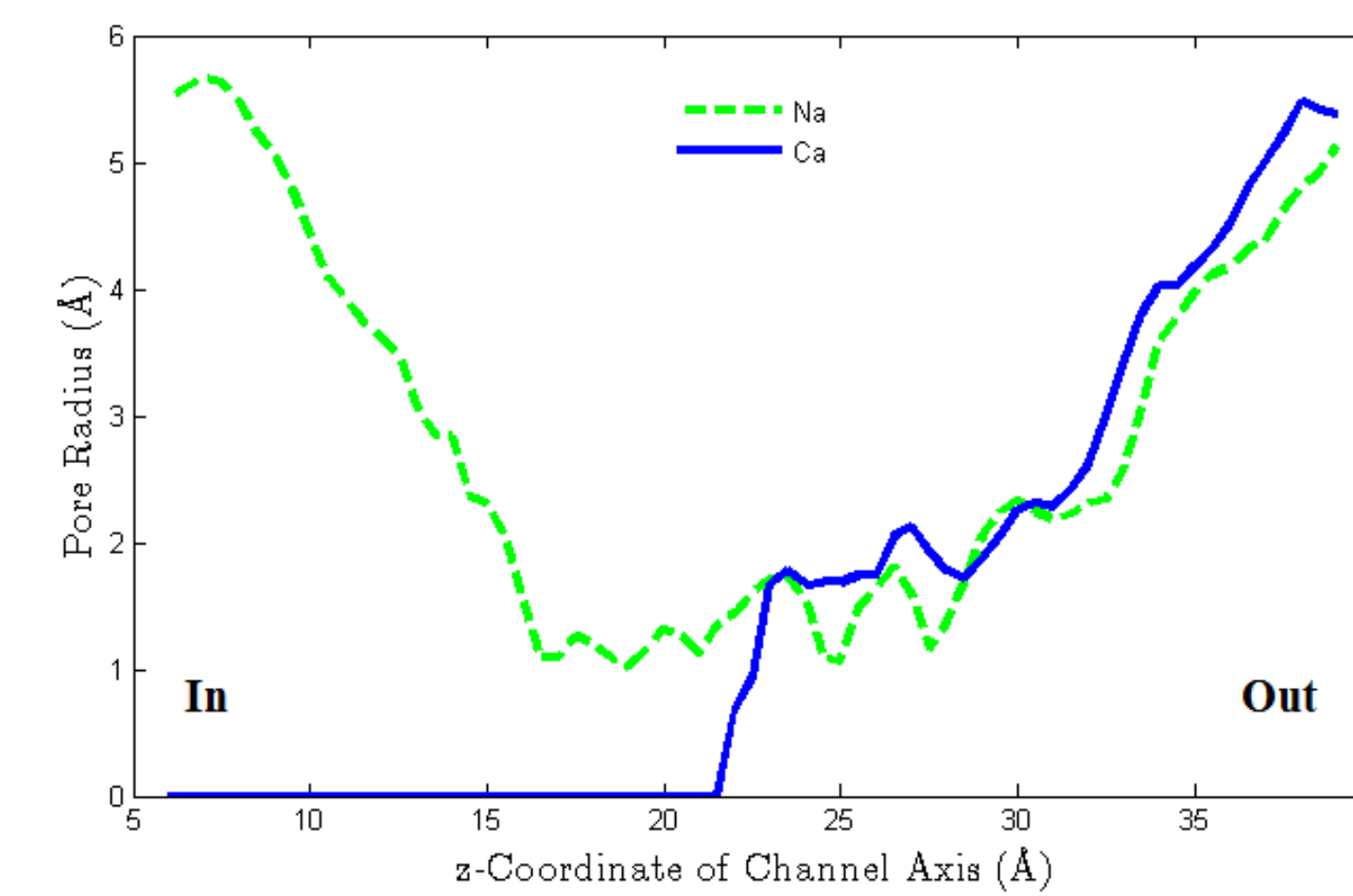
The theory considers the **steric effect of ions and water** molecules with different sizes and **interstitial voids**, the correlation effect of crowded ions with different valences, and the screening effect of **polarized water molecules** in an inhomogeneous aqueous electrolyte.

We calculate the electrostatic and steric potentials of the **four binding sites in NCX**, i.e., three Na<sup>+</sup> binding sites and one Ca<sup>2+</sup> binding site, with protein charges provided by the software *PDB2PQR*. The energy profiles of Na<sup>+</sup> and Ca<sup>2+</sup> ions along their respective Na<sup>+</sup> and Ca<sup>2+</sup> pathways in experimental conditions enable us to explain the fundamental mechanism of NCX that extrudes intracellular Ca<sup>2+</sup> across the cell membrane against its chemical gradient by using the downhill gradient of Na<sup>+</sup>. Atomic and numerical details of the binding sites are given to illustrate the ion-exchange mechanism.

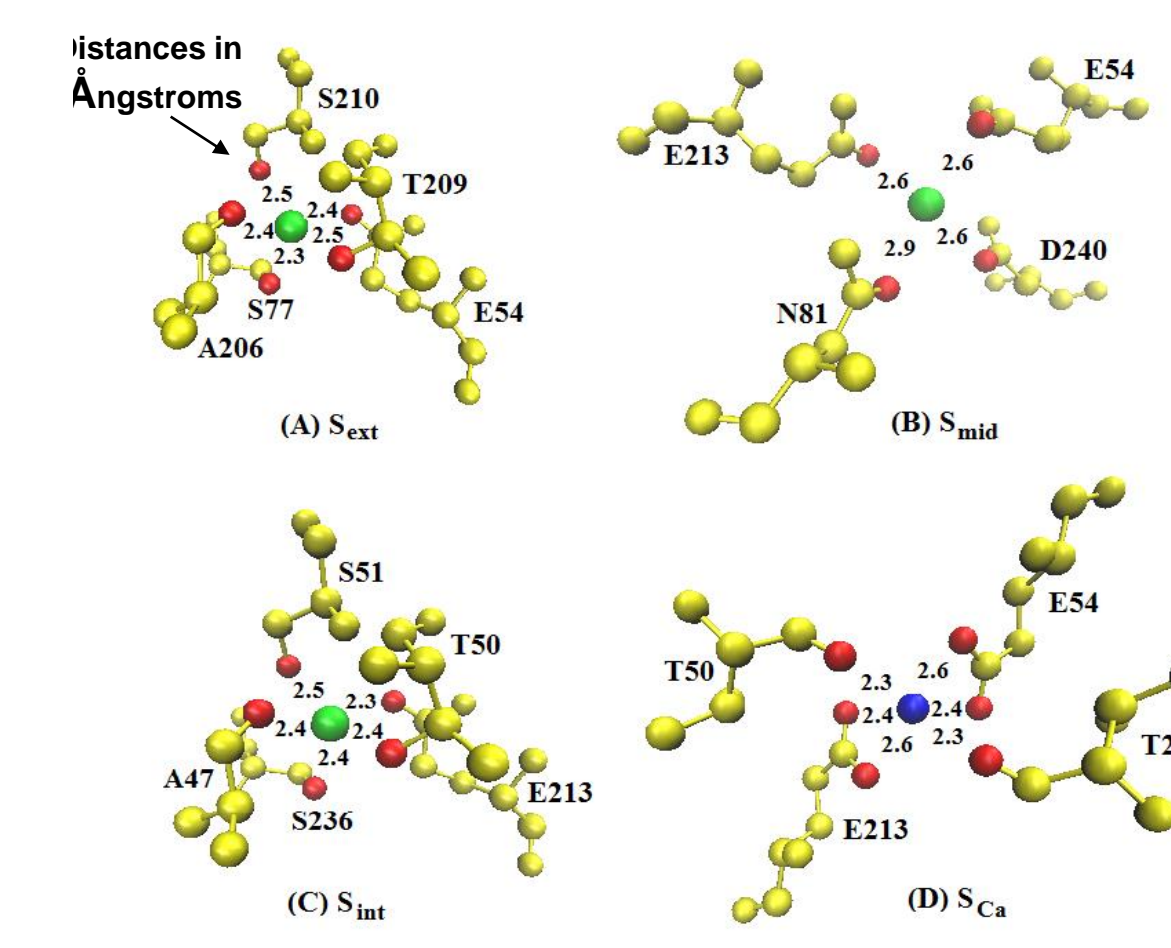
## Structure



## Winding Tortuous Irregular Pore

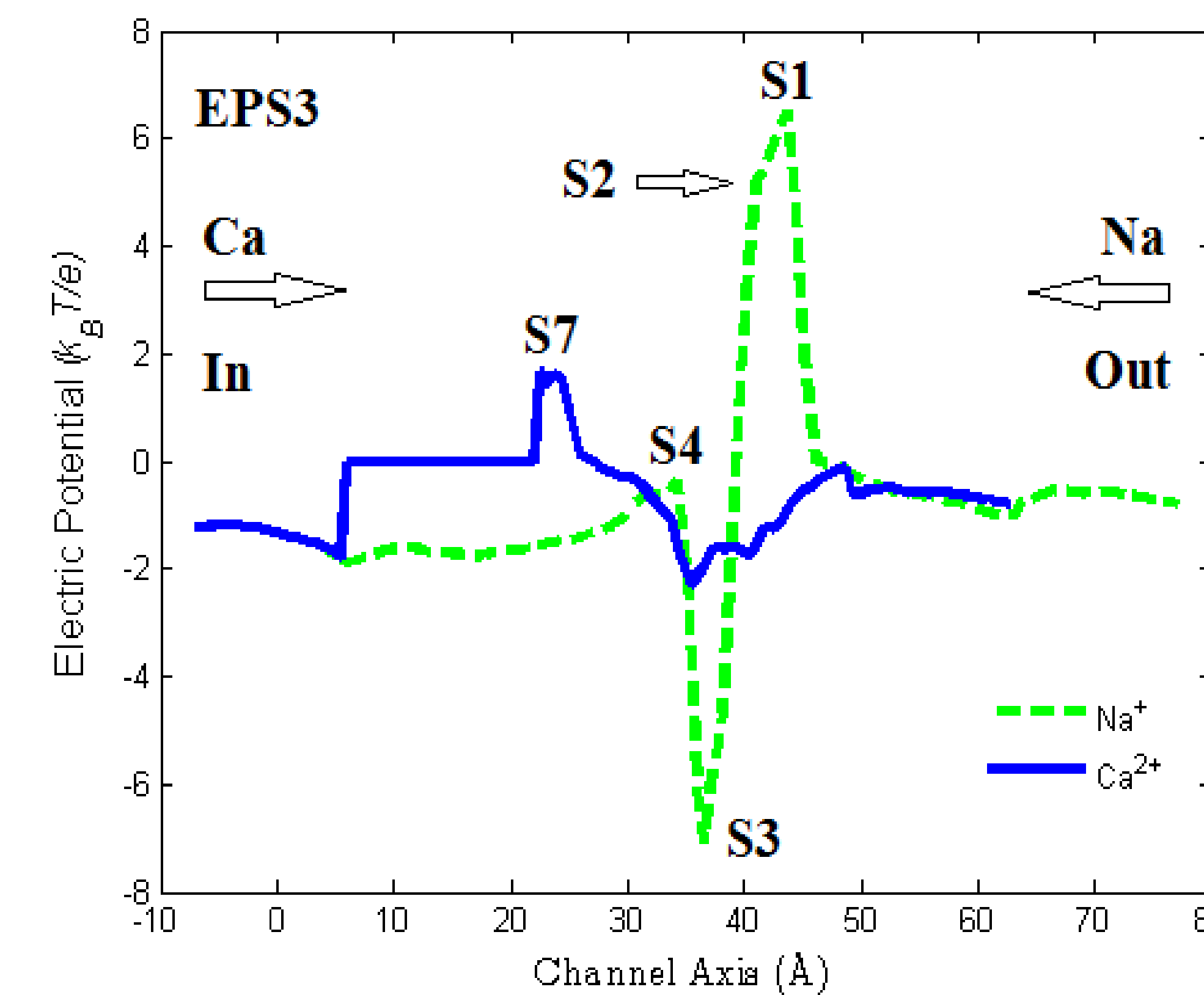


## Binding Sites

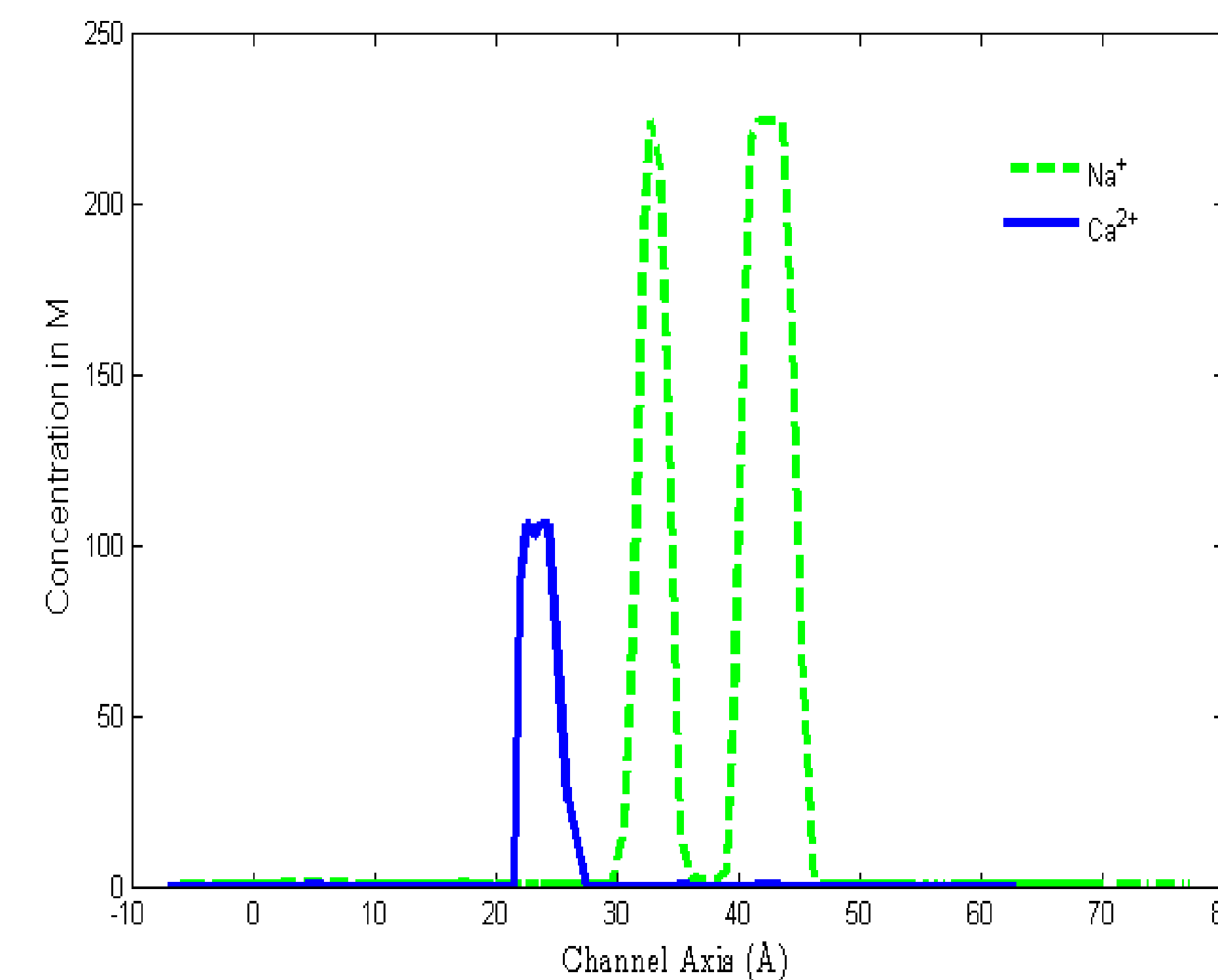


## Electrical Potential and Concentration Profiles

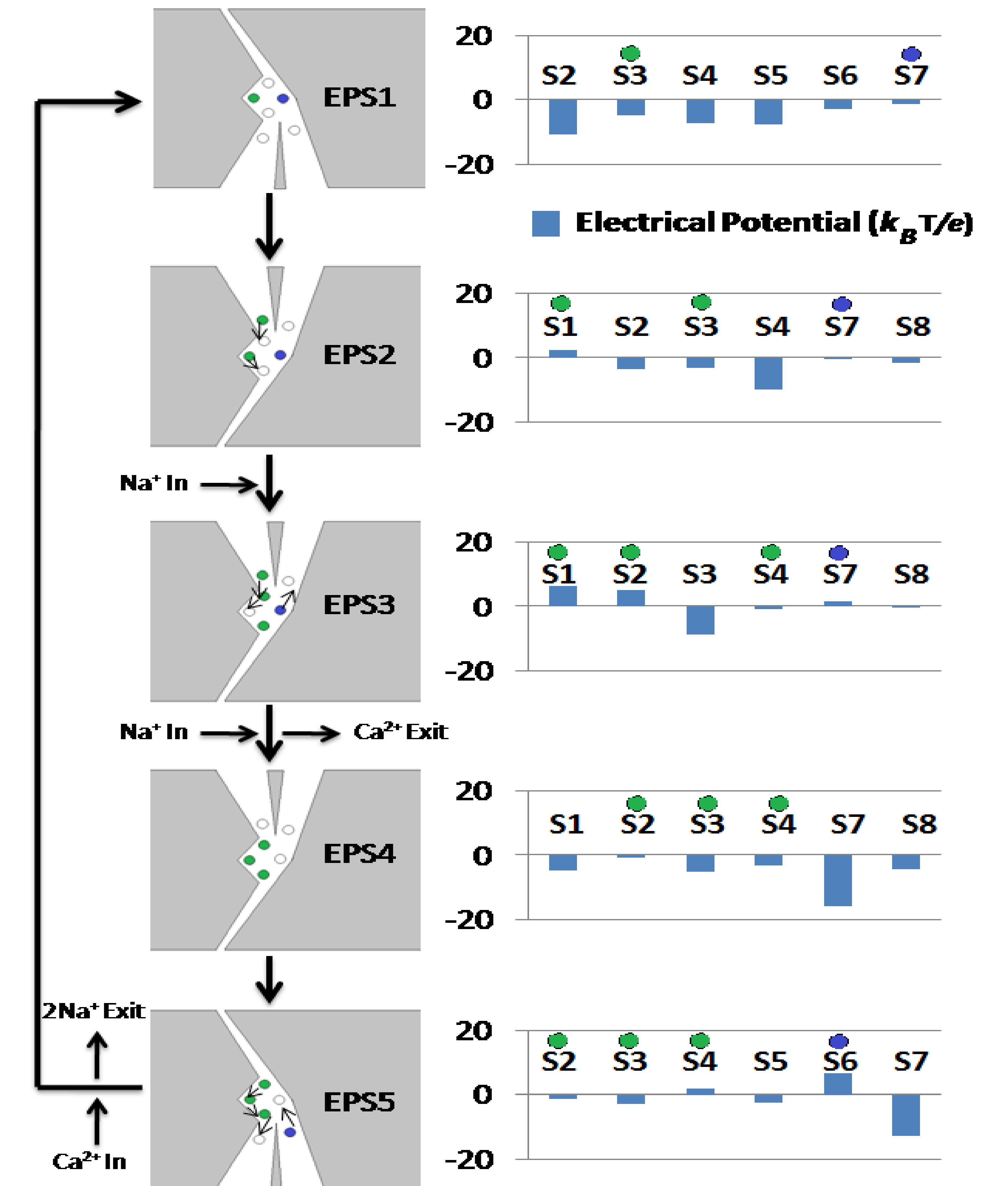
### Electrical Potential



### Concentration



## Energies of Binding Sites computed as outputs of Fermi Poisson



## Fermi (like) Distribution

$$C_i(\mathbf{r}) = C_i^{bath} \exp(-\beta_i \phi(\mathbf{r}) + S^{steric}(\mathbf{r}))$$

$$S^{steric}(\mathbf{r}) = \ln(\Gamma(\mathbf{r}) / \Gamma(bath))$$

$$\Gamma(bath) = \text{volume fraction of voids in bath}$$

$$\Gamma(\mathbf{r}) = \text{volume fraction of voids in channel}$$

Explicit formulae in publications  
 e.g., *Phys Rev E* (2015) 92: 012711