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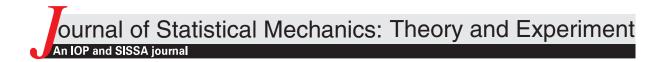
Putative resolution of the EEEE selectivity paradox in L-type Ca²⁺ and bacterial Na⁺ biological ion channels

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Putative resolution of the EEEE selectivity paradox in L-type Ca²⁺ and bacterial Na⁺ biological ion channels

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Abstract. The highly selective permeation of ions through biological ion channels can be described and explained in terms of fluctuational dynamics under the influence of powerful electrostatic forces. Hence valence selectivity, e.g. between Ca^{2+} and Na^+ in calcium and sodium channels, can be described in terms of ionic Coulomb blockade, which gives rise to distinct conduction bands and stop-bands as the fixed negative charge Q_f at the selectivity filter of the channel is varied. This picture accounts successfully for a wide range of conduction phenomena in a diversity of ion channels. A disturbing anomaly, however, is that what appears to be the same electrostatic charge and structure (the so-called EEEE motif) seems to select Na^+ conduction in bacterial channels but Ca^{2+} conduction in mammalian channels. As a possible resolution of this paradox it is hypothesised that an additional charged protein residue on the permeation path of the mammalian channel increases $|Q_f|$ by e, thereby altering the selectivity from Na^+ to Ca^{2+} . Experiments are proposed that will enable the hypothesis to be tested.

Keywords: Brownian motion, stochastic processes (theory), dynamics (theory), diffusion

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1. Introduction

Biological ion channels [1] are natural nanopores through cellular membranes. They provide for the fast and highly selective permeation of physiologically important ions like Na⁺, K⁺ and Ca²⁺. The conduction and selectivity of e.g. voltage-gated Ca²⁺ [2] and Na⁺ channels [3] are known to be determined by the ions' fluctuation-driven movements and interactions inside a short, narrow selectivity filter lined with negatively-charged protein residues⁴ It is known that permeation may sometime involve the correlated motion of more than one ion [4–6]. Mutation studies [3, 7–9] and simulations [10–15] show that the fixed charge Q_f provided by the residues is a determinant of the channel's conductivity and valence selectivity. Both nanopores [16] and ion channels [17] exhibit the phenomenon of ionic Coulomb blockade, closely analogous to electronic Coulomb blockade in mesoscopic systems [18–20].

Building on earlier work by Zhang *et al* [21] on ionic transport in water-filled periodically-charged nanopores, we used Brownian dynamics simulations of permeation in Ca^{2+} channels to reveal the existence of discrete conduction and selectivity bands as functions of Q_f [22, 23]. These were not only consistent with earlier speculations [19, 24] but were able to explain both the anomalous mole fraction effect (AMFE) [2] and a number of the puzzling mutation-induced transformations of selectivity in Ca^{2+}/Na^+ channels. More recently, we generalized the electrostatic analysis of the multi-ion energetics of conduction bands [23] by introducing an ionic Coulomb blockade model of conduction and selectivity in biological ion channels thereby bringing them into the context of mesoscopic phenomena [17, 25].

Although the Coulomb blockade theory [17, 25] seems to provide convincing explanations of a wide range of ion channel phenomena, it appears to be in direct

⁴ The protein residues are amino acids, of which aspartate (D) and glutamate (E) have negatively charged side

chains while lysine (K) and arganine (R) have positively charged side chains; we also mention neutral alanine (A), leucine (L), tryptophan (W) and serine (S).

contradiction to the experimental observation that the same electrostatic charge and structure (the so-called EEEE motif) at the selectivity filter seems to select Na⁺ conduction in bacterial channels but Ca²⁺ conduction in mammalian channels. We will refer to this apparent anomaly as the *EEEE paradox*. The aim of the present paper is to develop an idea introduced by Cheng *et al* [26] leading to a plausible resolution of the paradox.

To set the scene, we start by summarising the generic electrostatics and Brownian dynamics model of calcium/sodium channels (section 2), including a short description of the Coulomb blockade model of permeation (section 2.2), and a classification of permeation mechanisms (section 2.3), also commenting on the success of the Coulomb blockade theory in accounting for AMFE. We then point out (section 2.4) that the EEEE paradox appears to cast doubt on the whole Coulomb blockade picture. In section 3 we propose a way in which the EEEE paradox may be resolved and we also suggest ways in which the corresponding hypothesis can be tested. Finally, we summarise and draw conclusions in section 4

In what follows, with SI units, e is the proton charge, z the ionic valence, ϵ_0 the vacuum permittivity, T the temperature, and $k_{\rm B}$ Boltzmann's constant.

2. Electrostatic permeation theory

2.1. Generic model of calcium channel

The generic electrostatic model of the SF of a $\operatorname{Ca}^{2+}/\operatorname{Na}^{+}$ ion channel used in earlier electrostatic modelling is shown in figure 1. The channel is described as an axisymmetric, water-filled, cylindrical pore of radius $R = 0.3 \,\mathrm{nm}$ and length $L = 1.6 \,\mathrm{nm}$ through a protein hub in the cellular membrane. A centrally-placed, uniform, rigid ring of negative charge Q_f in the range $0 \leq |Q_f| \leq 7e$ is embedded in the wall at $R_Q = R$. The lefthand bath, modeling the extracellular space, contains non-zero concentrations of Ca^{2+} and/or Na⁺ ions. We take both the water and the protein to be homogeneous continua with relative permittivities $\epsilon_w = 80$ and $\epsilon_p = 2$, respectively, but describe the ions as discrete charges $q_i = ze$ within the framework of the implicit hydration model moving in single file within the channel, with bulk values of diffusion coefficients D_i . The BD simulations solve the coupled 3D axisymmetrical Poisson electrostatic equation and 1D overdamped Langevin stochastic equation numerically and self-consistently at each simulation step [5, 10, 22, 23, 27].

Although the model represents a simplification of the actual electrostatics and dynamics of ions and water molecules within the selectivity filter [28], we may note that reduced models can successfully reproduce significant properties of real biological channels [10, 12] and artificial nanopores [16, 21, 28]. Details of the model, its range of validity, and its limitations, have been presented and discussed elsewhere [22, 23].

2.2. Coulomb blockade model of ionic permeation

The single- and multi-ion conduction bands found in the BD simulations [22, 23] are shown in figures 2(a) and (b) which plot the Ca^{2+} current J and channel occupancy P



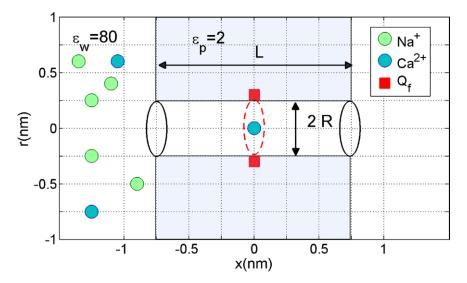


Figure 1. Electrostatic model of a Ca^{2+} or Na^+ channel, after [22, 23]. Ions move in single file along the channel axis. See text for details.

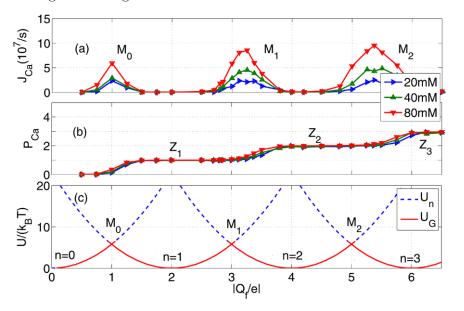


Figure 2. Brownian dynamics simulations of multi-ion conduction and occupancy in a Ca²⁺ channel model versus the effective fixed charge Q_{f_2} (a),(b) are reworked from [22] and (c) from [17]. (a) Plots of the Ca²⁺ current J for pure Ca²⁺ baths of different concentration (20, 40 and 80 mM as indicated). (b) The occupancy P. (c) The excess self-energy U_n and ground state energy U_G versus Q_f for channels with n = 0, 1, 2 and 3 Ca²⁺ ions inside. The conduction bands M_n and the blockade/ neutralisation points Z_n are discussed in the text.

for pure baths of different concentration. Figure 2(a) shows narrow conduction bands M_0 , M_1 , M_2 separated by stop-bands of almost zero-conductance centred on the blockade points Z_1 , Z_2 , Z_3 . Figure 2(b) shows that the M_n peaks in J correspond to transition regions in channel occupancy, where P jumps from one integer value to the next, and that the stop-bands correspond to saturated regions with integer P = 1, 2, 3...

Identification problems for calcium ion channels

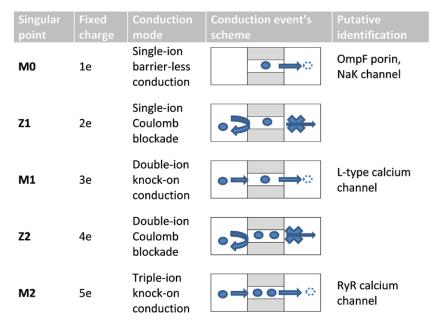


Figure 3. Physical mechanisms of multi-ion blockade and permeation of calcium ions.

Coulomb blockade appears in low-capacitance systems from quantization of the quadratic energy form at a grid of discrete states, provided that the Coulomb energy gap $\Delta U_n = U_s$ is large enough $(\Delta U_n \gg k_{\rm B}T)$ to block transitions between neighbouring $\{n\}$ states; that is a strong electrostatic exclusion principle. Figure 2(c) plots U_n and the ground state potential energy $U_{\rm G}$ as functions of Q_f . We see a periodic pattern with two kinds of $U_{\rm G}$ singular points in, marked as M_n and Z_n . The minima of $U_{\rm G}$ (and the blockade regions) appear around the neutralisation points $Z_n = -zen$ where $Q_{\rm G} = 0$ and the occupancy P_c is saturated at an integer value [21, 23]. For divalent Ca^{2+} ions $\Delta U_n \approx 20k_{\rm B}T$ and hence the blockade is strong. The crossover points M_n ($U_n = U_{n+1}$) allow barrier-less $\{n\} \leftrightarrows \{n+1\}$ transitions; they correspond to the P_c transition regions and to the conduction peaks in J [23].

The positions of the singular Q_f points in figure 2(c) can be written as:

$$Z_n = -zen \pm \delta Z_n \approx 0e, -2e, -4e...$$
(Coulomb blockade)
$$M_n = -ze(n+1/2) \pm \delta M_n \approx -1e, -3e, -5e... (Resonant conduction)$$
(1)

where δZ_n , δM_n are possible corrections for the singular part of affinity and ion-ion interactions, not accounted for here.

2.3. Mechanisms of blockade and permeation

The Coulomb blockade model predicts a very strict and clearly-defined pattern of ionic blockade and conduction [17, 25] where the physical processes occurring at the various conduction and blocking points (see below) are sketched in figure 3.

Figure 4 presents the sequence of singular points that appear for Ca^{2+} ions in the generic model as a function of Q_f , as predicted by (1). The sequence starts from the Coulomb blockade point $Z_0 = 0e$, i.e. the neutralized channel is impermeable for divalent ions due to strong Coulomb blockade by the induced charges. This blockade point



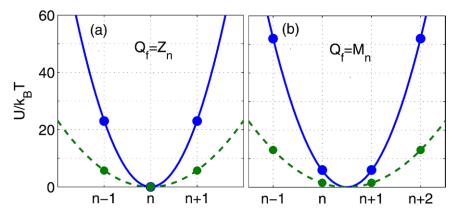


Figure 4. Valence-selective Coulomb blockade and resonant conduction. (a) Coulomb blockade. Plots of the self-energy U_s for Z_n points versus n, with Ca²⁺ (blue), Na⁺ (green), and quantization points (filled circles). (b) Resonant conduction. Plots of the self-energy U_s plots for the M_n points versus n with Ca²⁺ (blue), Na⁺ (green), and quantization points (filled circles).

than repeats itself with period $\approx 2e$ as Z_1 , Z_2 etc with growing number of blocking ions (1 for Z_1 , and 2 for Z_2).

The resonant point M_0 shows single-ion resonant (barrier-less) conduction mechanism (see [23] for details) when induced charges balance the charge of the moving ion. The M_1 resonant point represents conduction via double-ion knock-on (figure 3). In our previous papers we identified M_1 with the L-type calcium channel assuming that protonation might account for the charge discrepancy. We will propose below an alternative explanation in which the L-type channel is actually an M_2 channel. Note that in the absence of a crystal structure for the calcium channel all such explanations are inevitably putative. The M_2 point represents conduction via triple-ion knock-on (figure 3). We have already connected this point with RyR calcium channel. The highest resonances are probably related to large-charge mutants of the bacterial sodium channels CaChBac and CavAB [3, 8].

All these mechanisms can be described in terms of single-vacancy conduction [29, 30]. Evenly-charged Z_i loci provide divalent block while oddly-charged M_i points provide AMFE, i.e. divalent block plus fast multi-ion barrier-less conduction. In addition, the Coulomb blockade model predicts exponential growth of binding strength with the net charge Q_f , which agrees well with experiment [17].

Thus the ionic Coulomb blockade model predicts a universal, valence-dependent, periodic pattern of stop/conduction bands similar to the electronic Coulomb blockade oscillations of conductance in quantum dots [18, 20]. It allows us to identify conduction bands with real calcium-conductive channels/mutants. Unlike its electronic counterpart, ionic Coulomb blockade is valence-dependent: the bands M_n shift in proportion to z due to (1) and broaden/narrow in proportion to z^2 [31].

Figure 4(a) plots the energy U_n of an *n*-occupied channel against *n* for the blockade/ neutralisation points Z_n . For divalent Ca²⁺ (full curve) U_n has a sharp minimum for state $\{n\}$, separated from neighbouring $\{n \pm 1\}$ states by an impermeable barrier of $20k_BT$. This is strong blockade closely similar to electronic Coulomb blockade in quantum dots [18, 32]. The same plot for Na⁺ ions (dashed curve) reveals a permeable $5k_BT$ barrier, that is weak ionic Coulomb blockade. Figure 4(b) show a similar plot for the resonant

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Channel	Segment	First residue		
$\overline{\mathrm{Ca}_v 1.2}$	IP IIP IIIP IVP	$379 \\ 722 \\ 1132 \\ 1432$	p41 L T V F Q C I T M E L T V F Q I L T G E M A L F T V S T F E L L L F R C A T G E	$\begin{array}{c} \mathbf{D} \le \mathbf{N} \le \mathbf{V} \le \mathbf{M} \le \mathbf{Y} \\ \mathbf{G} \le \mathbf{V} \ge \mathbf{L} \le \mathbf{Y} \end{array}$
NaChBac	IP-IVP	182	p1 L T L F Q VV T L E	p11

Table 1. Alignment of the protein P-loops near the selectivity filters of Ca^{2+} [26] and Na⁺ [8] channels.

Note: The charged glutamate (E) and aspartate (D) resides that form the electrostatically-active part of the selectivity filter are emboldened. Note that all 4 segments of the NaChBAC selectivity filter are identical. It is unknown whether or not the D on p51 of the Ca^{2+} channel should be considered as part of the selectivity filter.

conduction points M_n . Again, it is strong ionic Coulomb blockade ($\Delta U \approx 40 k_{\rm B} T$) for Ca²⁺ ions and weak ionic Coulomb blockade ($\Delta U \approx 10 k_{\rm B} T$) for Na⁺ ions.

The ionic Coulomb blockade approach can be also applied to a mixed $\operatorname{Ca}^{2+}-\operatorname{Na}^+$ bath at the $Q_f = -3e$ point, which is M_1 for Ca^{2+} and Z_3 for Na^+ ions. The combination $1\operatorname{Ca}^{2+} + 1\operatorname{Na}^+$ (with +3e charge) inside the SF is neutralized ($Q_n = 0$) and so the channel is asymmetrically blocked due to ionic Coulomb blockade (figure 4(a))—which is strong for Ca^{2+} and weak for Na^+ . Similarly $3\operatorname{Na}^+$ (with +3e) also blocks the channel by weak ionic Coulomb blockade at the Z_3 point for Na^+ ions. Otherwise, a channel contents of $2\operatorname{Ca}^{2+}$ (+4e) gives $Q_n = +1e$ and resonant conduction (figure 4(b)). Hence ionic Coulomb blockade provides a natural explanation of AMFE in Ca^{2+} channels consistent with experiment and with analysis in terms of a potential energy landscape [23, 31].

2.4. Apparently anomalous EEEE selectivity in the mammalian Ca^{2+} channel

Notwithstanding the great success of the Coulomb blockade model in explaining many different, previously puzzling, features of ion channel conduction, the EEEE paradox (see above) represents a serious concern: for the same $Q_f = -4e$ at the selectivity filter to give rise to both Na⁺ and Ca²⁺ resonances is clearly impossible, and therefore the paradox threatens the whole edifice of understanding that has been developed around electrostatics and Coulomb blockade. If we are to retain the Coulomb blockade theory of selectivity, then we are obliged to find an explanation of what we may choose to regard as the anomalous properties of the L-type Ca²⁺ channel. We propose such an explanation in section 3.

3. Proposed resolution of the EEEE Paradox in calcium channels

Table 1 lists comparable alignments of the P—and S—segments in Ca_v.1.2 mammalian calcium [26] and NaChBac bacterial sodium [8] channels. It is usually supposed [2] that the selectivity filter of the mammalian calcium channel is based upon a 4-glutamate EEEE locus and hence has a total charge $Q_f = -4e$. This locus is known to be

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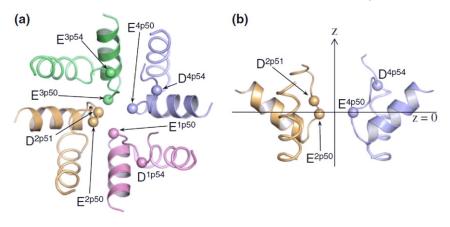


Figure 5. The Cav1.2 outer pore model with repeats I, II, III, and IV colored pink, orange, green, and blue, respectively. Alpha-carbons of the selectivity filter glutamates E^{p50s} , D^{2p51} , and acid residues in positions p54 are shown as spheres. (a) Extracellular view. (b) Side view with the *xy*-plane and the *z*-axis. From [26], with permission from Springer.

highly conserved, meaning that the sequence has remained the same over many generations despite the vagaries of evolution and speciation, and implying that the structure is important because any small mutation makes the organism significantly less fit. However this proposition not only leads to structural problems [15], but it is also inconsistent with expectations based on the Coulomb blockade model (see above). If we have pseudo-similar loci with similar Q_f but different function, this directly contradicts our central idea of valence selectivity being of electrostatic origin. Secondly, and in particular, the evenly-charged EEEE locus corresponds to the *blockade point* Z_1 rather than to any of resonant conduction points M_i (figures 2–4). Note that similar EEEE loci in the ChNaBac and NavAB bacterial channels provide for sodium selectivity and divalent block, rather than calcium selectivity.

It always was clear that differences will exist between formally identical loci, and that these differences do not necessarily follow from the structure itself. In the absence of structural data, information related to the positions of particular residues comes mainly from mutagenesis results. One possible source of differences could be protonation [33], which is able to change the effective charge of the selectivity filter, but there is no confirmation from structure simulations, so that this explanation seems speculative and *ad hoc*.

We note, however, that an aspartate D^{2p51} residue exists in the structure; no associated mutagenesis data are available, so some authors have supposed that it is not located at the selectivity filter [34]. Yet it provides a possible resolution of the EEEE paradox [26]. Repeat II of α -unit of the calcium channel has this D^{2p51} residue at a position next to the EEEE, and it is highly conserved, so that the locus can be thought as EEEED [26] with nominal charge $Q_f = -5e$. Figure 5 shows the results of Monte-Carlo simulations of the putative molecular structure by Cheng *et al* [26]. The additional D^{2p51} aspartate side chain is evidently located very close to the main 4-glutamate EEEE ($E^{(1-4)p50}$) ring both in both the radial (a) and axial (b) directions, and must thus play an equal role in the electrostatic interactions. Following their suggestion [26], we conclude that the calcium channel's locus is actually EEEED, with a charge of -5e, rather than the EEEE with -4e which correctly describes the sodium channel. This would correspond to conduction at the triple-ion M_2 resonant point (figure 3) [17]. Such an identification would differ from our previous conclusion that the L-type channel conducts at the $M_1 = -3e$ singular point [22, 23], but it appears more likely to be correct. From this viewpoint, there is no EEEE paradox at all, and we are able to include both channels within the Coulomb blockade classification scheme (1).

Finally, we emphasise that both the old and new M_i identifications for the L-type channel are speculative, and that our tentative conclusions need to be confirmed by mutation studies of the D^{2p51} side chain using $D \to E$, $D \to K$ and $D \to A$ point mutations. We may anticipate: that a $D \to E$ mutation giving an EEEEE locus will leave the channel properties unchanged; that a $D \to A$ mutation leading to an EEEEA mutant will result in a Na⁺-selective channel exhibiting divalent block similar to the NaChBac channel; and that a $D \to K$ mutation leading to EEEEK ($Q_f = -3e \Rightarrow M_1$) will yield a new Ca²⁺-selective channel.

4. Conclusions

The conclusions are to be considered within the context of our model, which embodies many simplifications. In particular, the permanent charge that we discuss is an effective variable bearing an unknown relationship to the full three-dimensional distribution of permanent charge in the channel protein. This reality reflects (1) many contributions of three-dimensional details of structure not captured in models of reduced dimensionality, (2) protein flexibility and dynamics over an enormous range of times $(10^{-15}-10^{-6} \text{ s}, \text{ for}$ example) that are not present in our model, and (3) possible additional sources of excess free energy. What is important is that the model reproduces important behavior for some specific choices of permanent charge that are not changed from condition to condition.

Within this context, we have suggested a possible resolution of the EEEE selectivity paradox for calcium/sodium channels, using the Coulomb blockade model to reinforce an idea proposed by Cheng *et al* [26]. The explanation supposes that the D^{2p51} residue is ionized, and that it is on the permeation path and part of the selectivity filter, very close to the EEEE ring. Hence the effective locus for calcium channels is actually EEEED implying $Q_f = -5e$, and providing for a triple-ion knock-on mechanism at the M_2 resonance. This inference awaits experimental confirmation.

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References

- [1] Hille B 2001 Ion Channels Of Excitable Membranes 3rd edn (Sunderland, MA: Sinauer Associates)
- [2] Sather W A and McCleskey E W 2003 Permeation and selectivity in calcium channels Ann. Rev. Physiol. 65 133–59
- [3] Tang L, El-Din T M G, Payandeh J, Martinez G Q, Heard T M, Scheuer T, Zheng N and Catterall W A 2014 Structural basis for Ca²⁺ selectivity of a voltage-gated calcium channel Nature 505 56–61

Identification problems for calcium ion channels

- [4] Armstrong C M and Neyton J 1991 Ion permeation through calcium channels Ann. NY Acad. Sci. 635 18–25
- [5] Roux B, Allen T, Berneche S and Im W 2004 Theoretical and computational models of biological ion channels Q. Rev. Biophys. 37 15–103
- [6] Kharkyanen V N, Yesylevskyy S O and Berezetskaya N M 2010 Approximation of super-ions for single-file diffusion of multiple ions through narrow pores Phys. Rev. E 82 051103
- [7] Heinemann S H, Teriau H, Stuhmer W, Imoto K and Numa S 1992 Calcium-channel characteristics conferred on the sodium-channel by single mutations Nature 356 441–3
- [8] Yue L X, Navarro B, Ren D J, Ramos A and Clapham D E 2012 The cation selectivity filter of the bacterial sodium channel, NaChBac J. Gen. Physiol. 120 845–53
- [9] Miedema H, Meter-Arkema A, Wierenga J, Tang J, Eisenberg B, Nonner W, Hektor H, Gillespie D and Meijberg W 2004 Permeation properties of an engineered bacterial OmpF porin containing the EEEE-locus of Ca²⁺ channels Biophys. J. 87 3137–47
- [10] Corry B, Vora T and Chung S H 2005 Electrostatic basis of valence selectivity in cationic channels Biochim. Biophys. Acta—Biomembr. 1711 72–86
- Boda D, Nonner W, Henderson D, Eisenberg B and Gillespie D 2008 Volume exclusion in calcium selective channels Biophys. J. 94 3486–96
- [12] Boda D 2014 Monte Carlo simulation of electrolyte solutions in biology: in and out of equilibrium Annual Reports in Computational Chemistry vol 10, ed D Gillespie and N Baker (Elsevier: Amsterdam) chapter 5, pp 127–64
- [13] Corry B 2013 Na^+/Ca^{2+} selectivity in the bacterial voltage-gated sodium channel NavAb PeerJ 1 e16
- [14] Csányi E, Boda D, Gillespie D and Kristf T 2012 Current and selectivity in a model sodium channel under physiological conditions: dynamic Monte Carlo simulations Biochim. Biophys. Acta—Biomembr. 1818 592–600
- [15] Shuba Y M 2014 Models of calcium permeation through T-type channels Pflügers Arch.—Eur. J. Physiol. 466 635–44
- [16] Krems M and Di Ventra M 2013 Ionic Coulomb blockade in nanopores J. Phys.: Condens. Matter 25 065101
- [17] Kaufman I K, McClintock P V E and Eisenberg R S 2015 Coulomb blockade model of permeation and selectivity in biological ion channels New J. Phys. 17 083021
- [18] Beenakker C W J 1991 Theory of Coulomb-blockade oscillations in the conductance of a quantum dot Phys. Rev. B 44 1646–56
- [19] Stopa M 2002 Rectifying behavior in Coulomb blockades: charging rectifiers Phys. Rev. Lett. 88 146802
- [20] Likharev K K 2003 SET: Coulomb blockade devices Nano et Micro Technol. 3 71–114
- [21] Zhang J, Kamenev A and Shklovskii B I 2006 Ion exchange phase transitions in water-filled channels with charged walls Phys. Rev. E 73 051205
- [22] Kaufman I K, Luchinsky D G, Tindjong R, McClintock P V E and Eisenberg R S 2013 Multi-ion conduction bands in a simple model of calcium ion channels Phys. Biol. 10 026007
- [23] Kaufman I K, Luchinsky D G, Tindjong R, McClintock P V E and Eisenberg R S 2013 Energetics of discrete selectivity bands and mutation-induced transitions in the calcium–sodium ion channels family Phys. Rev. E 88 052712
- [24] Eisenberg R S 1996 Atomic biology, electrostatics and ionic channels New Developments in Theoretical Studies of Proteins ed R Elber (Singapore: World Scientific) pp 269–357
- [25] Kaufman I, Gibby W, Luchinsky D, McClintock P and Eisenberg R 2015 Coulomb blockade oscillations in biological ion channels IEEE Conf. Proc. 23rd Intern. Conf. Noise and Fluctuations (Xian)
- [26] Cheng R C, Tikhonov D B and Zhorov B S 2010 Structural modeling of calcium binding in the selectivity filter of the L-type calcium channel Eur. Biophys. J. 39 839–53
- [27] Berti C, Furini S, Gillespie D, Boda D, Eisenberg R S, Sangiorgi E and Fiegna C 2014 Three-dimensional Brownian dynamics simulator for the study of ion permeation through membrane pores J. Chem. Theor. Comput. 10 2911–26
- [28] Laio A and Torre V 1999 Physical origin of selectivity in ionic channels of biological membranes Biophys. J. 76 129–48
- [29] Hille B and Schwarz W 1978 Potassium channels as multi-ion single-file pores J. Gen. Physiol. 72 409–42
- [30] Schumaker M F and MacKinnon R 1990 A simple model for multi-ion permeation. Single-vacancy conduction in a simple pore model Biophys. J. 58 975–84
- [31] Kaufman I K, Tindjong R, Luchinsky D G, McClintock P V E and Eisenberg R S 2013 Resonant multi-ion conduction in a simple model of calcium channels *IEEE Conf. Proc. 22nd Intern.Conf.on Noise and Fluctuations (Montpellier, 24–8 June 2013)* ed J M Routoure *et al* (Piscataway, NJ: IEEE)
- [32] Alhassid Y 2000 Statistical theory of quantum dots Rev. Mod. Phys. 72 895–968
- [33] Furini S, Barbini P and Domene C 2014 Effects of the protonation state of the EEEE motif of a bacterial Na⁺-channel on conduction and pore structure Biophys. J. 106 2175–83
- [34] Lipkind G M and Fozzard H A 2001 Modeling of the outer vestibule and selectivity filter of the L-type Ca²⁺ channel Biochemistry 40 6786–94