

BioMolecular Engineering

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**Experimental Effort needed without theory
is Enormous**

**Bio-Molecular
Engineering
is the
Future of Molecular
Biology,
whether biologists know it or not**

How does it work?

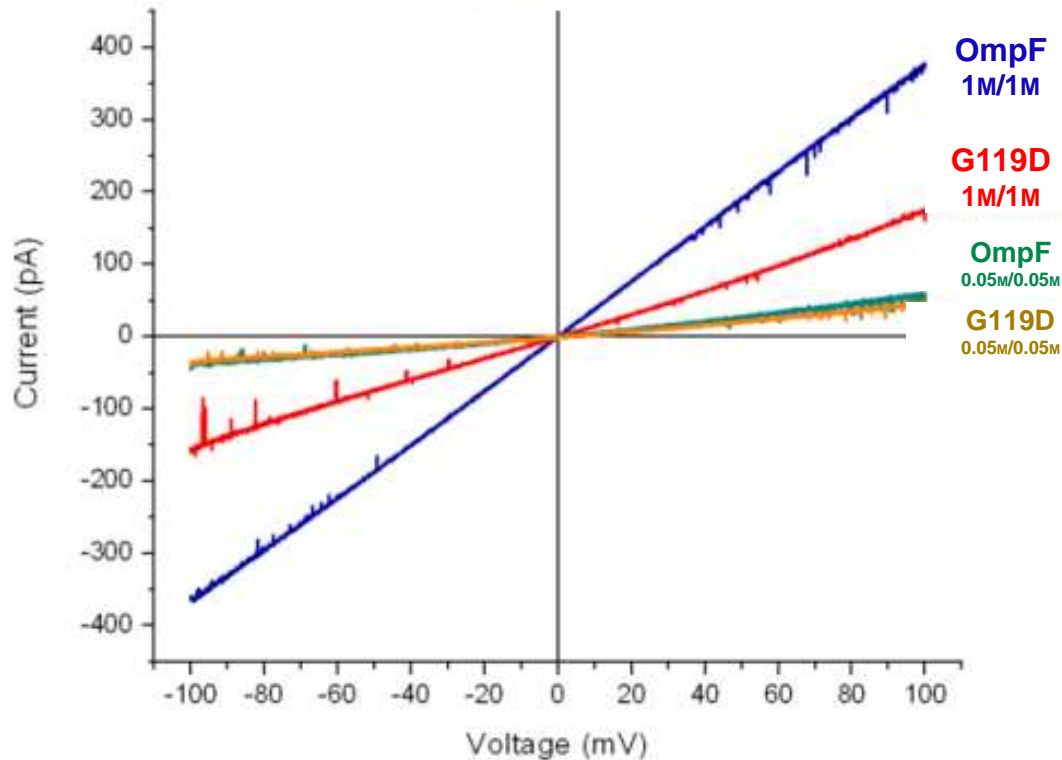
How do a few atoms control
(macroscopic)
Biological Function?

Much Molecular Biology
is
Reverse Engineering

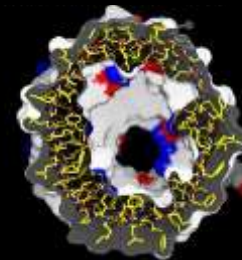
A few atoms make a BIG Difference

OmpF and G119D Porin Trimer Current Voltage Curves

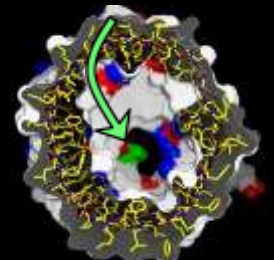
KCl Solutions



Ompf



G119D



Glycine
replaced by
Aspartate

Structure determined by
Raimund Dutzler
in **Tilman Schirmer's lab**
Current Voltage relation by
John Tang
in **Bob Eisenberg's Lab**

**Trial-and-Error Biology
is very inefficient**

but it is (almost)

**All we have available,
today.**

Experimental Effort needed without theory is Enormous

*USA: NIH $\$3.1 \times 10^{10}$
devoted almost entirely to descriptive experimental work*

**Trial-and-Error Biology
is very inefficient**
but it is (almost)
All we have available,
today.

Biology, Medicine. Engineering

are all about

Reduced Models

in which

SOME atomic details

Control Function

If Devices are to Work Engineers* must Grasp

and not just reach

Uncalibrated Devices do not Work!

**“Ah, ... a man's reach should exceed his grasp,
Or what's a heaven for?”**

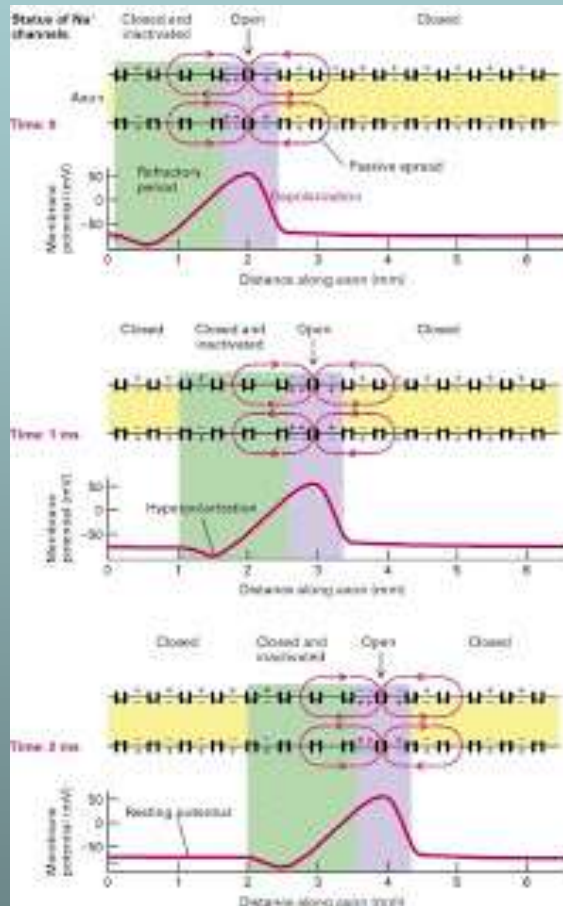
Robert Browning

"Andrea del Sarto", line 98

Poets hope we will never learn the difference between Dreams and Realities

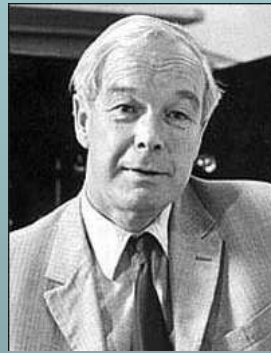
***Scientists and Poets can Reach
but Engineers must Grasp**

Biology is made of **Devices** and they are **MULTISCALE**

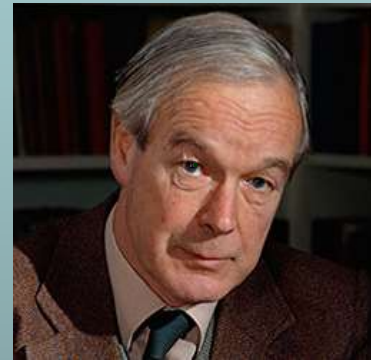


Hodgkin's Action Potential
is the
Ultimate Multiscale model
from
Ångstroms to Meters

Device Approach to Biology is a Great Success widely unknown



Alan Hodgkin
friendly



Alan Hodgkin:
“Bob, I would not put it that way”

Decisive Role of the Electric Field

in Semiconductors and Ionic Solutions

**Everything
Interacts with
Everything Else**

Semiconductor *PNP* Equations

For Point Charges

Poisson's Equation

$$-\frac{\epsilon_0}{A(x)} \frac{d}{dx} \left(\epsilon(x) A(x) \frac{d\phi}{dx} \right) = eP(x) + e \sum_i z_i \rho_i(x)$$

Dielectric Coefficient ϵ_0
 Cross sectional Area $A(x)$
 Permanent Charge of Protein $P(x)$
 Valence Proton charge z_i
 Number Densities $\rho_i(x)$

Drift-diffusion & Continuity Equation

$$\frac{dJ_i}{dx} = 0 \quad -J_i = D_i(x) A(x) \rho_i(x) \frac{d\mu_i}{dx}$$

Flux J_i
 Diffusion Coefficient $D_i(x)$

Chemical Potential $\mu_i(x)$

$$\mu_i(x) = z_i e \phi(x) + kT \ln \left(\frac{\rho_i(x)}{\rho^*} \right) + \mu_{i,2,3}^{\text{ex}}(x)$$

valence proton charge z_i
 Thermal Energy kT
 Finite Size Special Chemistry $\mu_{i,2,3}^{\text{ex}}(x)$

All we have to do is

Solve it / them!

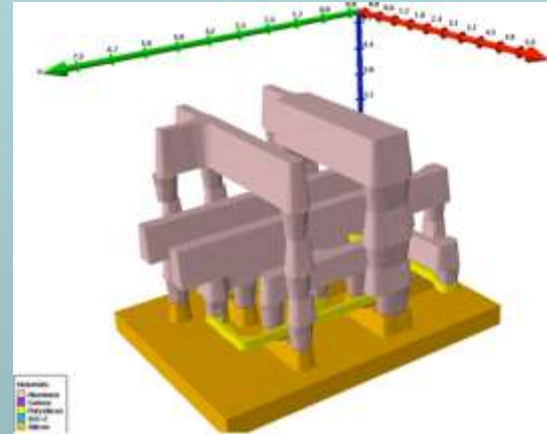
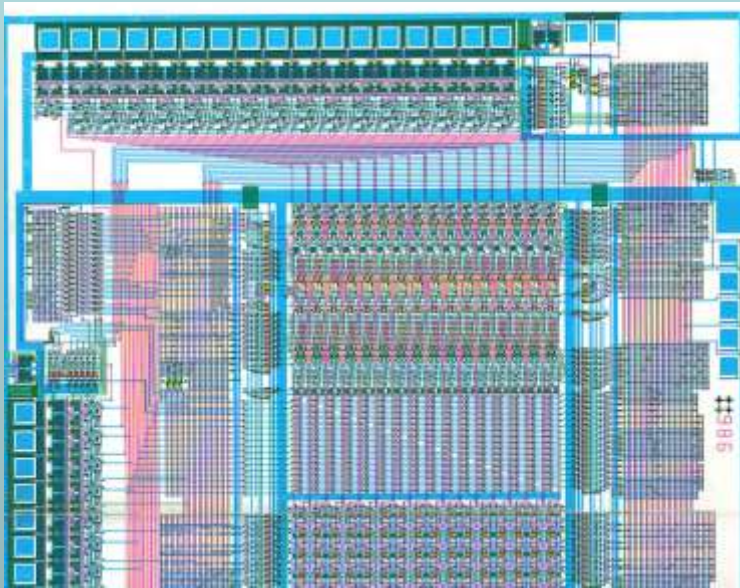
Boundary conditions:

STRUCTURES of Ion Channels

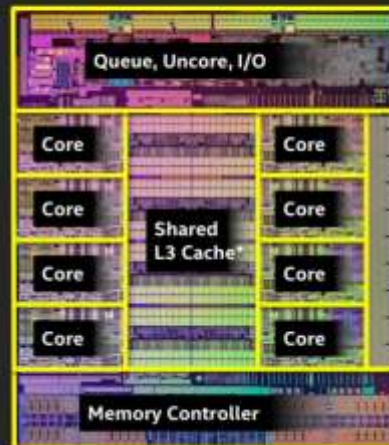
STRUCTURES of semiconductor
devices and integrated circuits

Integrated Circuit

Too small to see!



Intel® Core™ i7-5960X Processor Die Map
22nm Tri-Gate 3-D Transistors

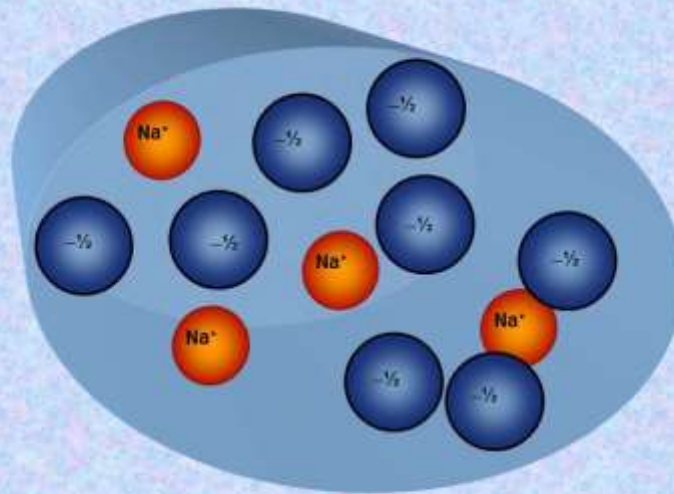


- Transistor count: 2.6 Billion
- Die size: 17.6mm x 20.2mm

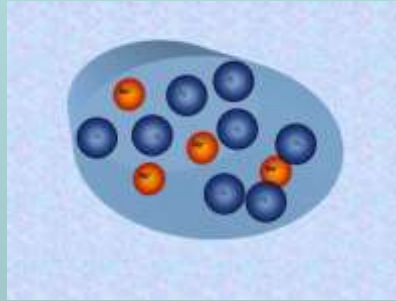
*20MB of cache is shared across all 8 cores

but

Ions are Spheres Crowded in Channels



Ions in Channels



Ions in Bulk Solutions



are

Complex Fluids

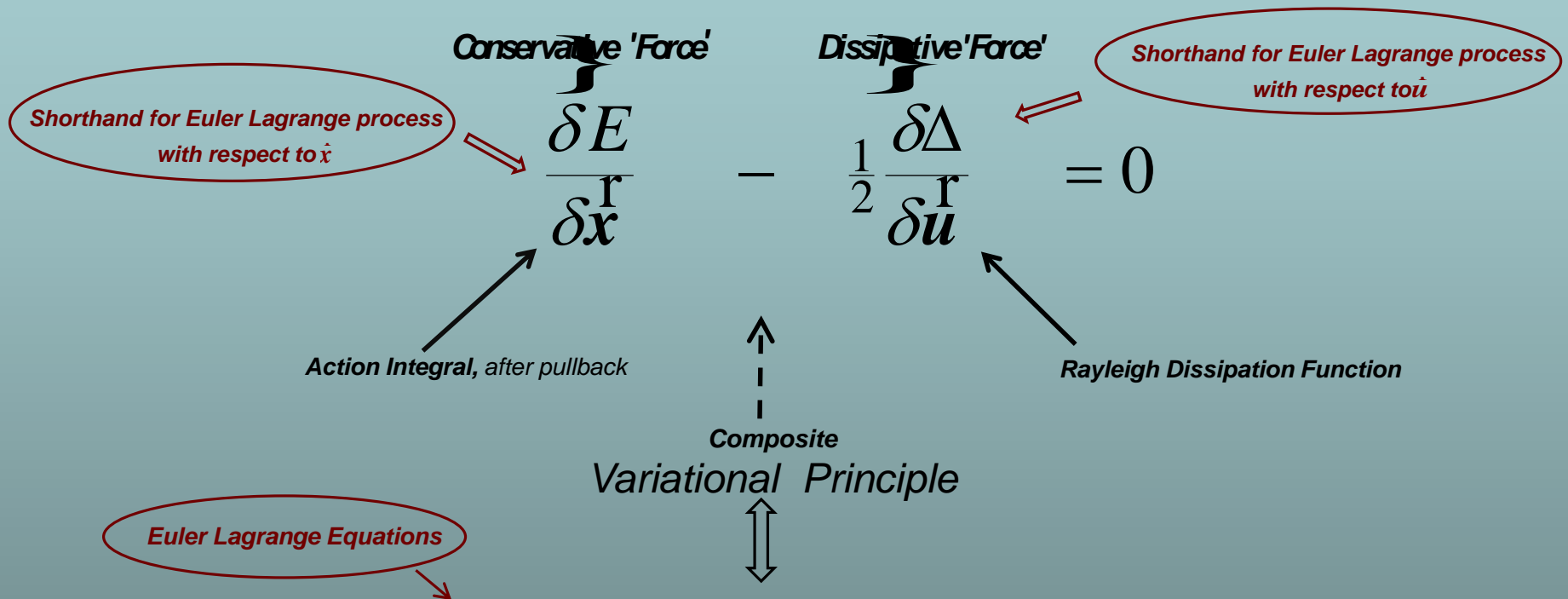
like liquid crystals of LCD displays

Energetic Variational Approach

EnVarA

Chun Liu, Rolf Ryham, and Yunkyong Hyon

Mathematicians and Modelers: two different 'partial' variations written in one framework, using a 'pullback' of the action integral



Field Theory of Ionic Solutions: Liu, Ryham, Hyon, Eisenberg

Allows boundary conditions and flow
Deals Consistently with Interactions of Components

PNP (Poisson Nernst Planck) for Spheres

Non-equilibrium variational field theory *EnVarA*

Nernst Planck Diffusion Equation

for **number density** c_n of negative n ions; positive ions are analogous

Diffusion Coefficient

$$\frac{\partial c_n}{\partial t} = \nabla \cdot \left[D_n \left\{ \nabla c_n + \frac{c_n}{k_B T} \left(z_n e \nabla \phi - \int \frac{12 \varepsilon_{n,n} (a_n + a_n)^{12} (\mathbf{x} - \mathbf{y})}{|\mathbf{x} - \mathbf{y}|^{14}} c_n(\mathbf{y}) d\mathbf{y} \right. \right. \right. \\ \left. \left. \left. - \int \frac{6 \varepsilon_{n,p} (a_n + a_p)^{12} (\mathbf{x} - \mathbf{y})}{|\mathbf{x} - \mathbf{y}|^{14}} c_p(\mathbf{y}) d\mathbf{y} \right) \right\} \right],$$

Thermal Energy

Coupling Parameters

Ion Radii

Number Densities

Poisson Equation

Dielectric Coefficient

$$\nabla \cdot (\varepsilon \nabla \phi) = - \left(\rho_0 + \sum_{i=1}^N z_i e c_i \right) \quad i = n \text{ or } p$$

Permanent Charge of Protein

valence proton charge

All we have to do is

***Solve the
Partial Differential Equations
with Boundary Conditions***

Fermi Poisson

Largest Effect
of
Crowded Ions
is
Saturation

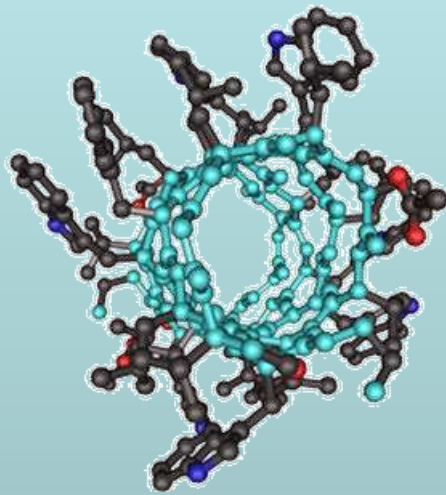
*Saturation cannot be described at all by classical Poisson Boltzmann approach and is described in a uncalibrated way by **present day** Molecular Dynamics when Mixtures and Divalents are Biologically Important in Concentrations of 10^{-8} to 10^1 M*

Fermi Description

is designed to deal with

Saturation of Concentration

Simulating saturation by interatomic repulsion (Lennard Jones)
is a significant mathematical challenge
to be side-stepped if possible
Eisenberg, Hyon and Liu (2010). JChemPhys 133: 104104



Gramicidin A

Unusual SMALL Bacterial Channel

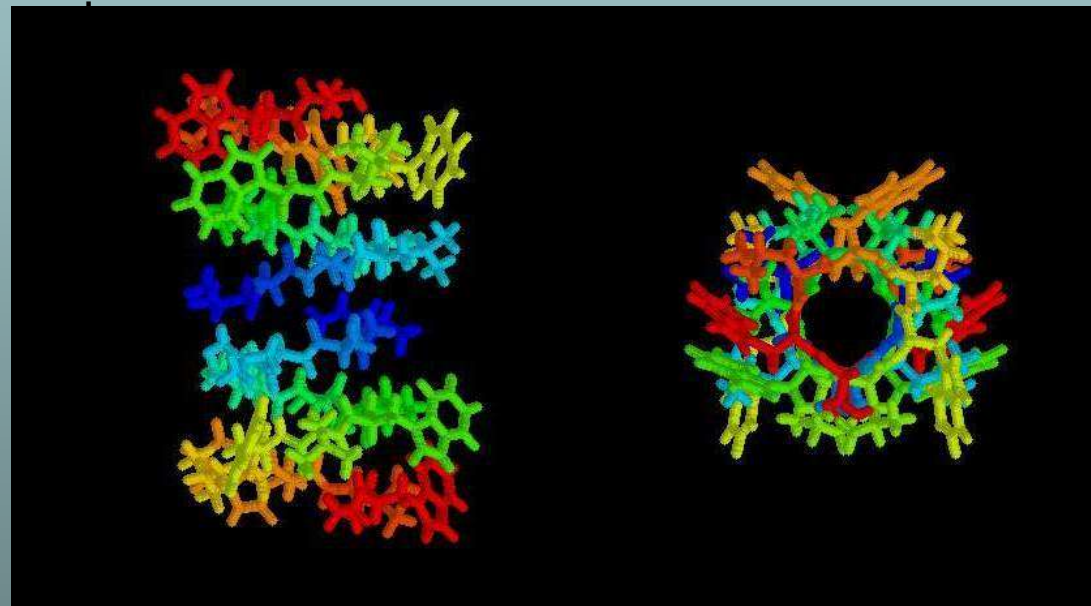
often simulated and studied

*Margaret Thatcher,
student of Nobelist Dorothy Hodgkin
Bonnie Wallace leading worker*

Validation of PNP Solvers with Exact Solution

following the lead of
Zheng, Chen & Wei

J. Comp. Phys. (2011) **230**: 5239



PNPF

Poisson-Nernst-Planck-Fermi

Implemented fully in 3D Code to accommodate 3D Protein Structures

$$\text{Flow} \left\{ \begin{array}{l} \nabla \cdot \mathbf{J} = 0 \\ \mathbf{J}_i = -D_i \left[\nabla C_i + (z_i \mathbf{e} / k_b T) \nabla \phi - C_i \nabla S^{steric} \right] \end{array} \right.$$

$$\text{Force} \left\{ \begin{array}{l} \nabla^2 \phi = \psi \\ \epsilon_{water} (l_c \nabla^2 - 1) \nabla^2 \phi(\mathbf{r}) \psi = \rho(\mathbf{r}) \end{array} \right.$$

$\epsilon_{water} (l_c \nabla^2 - 1)$ approximates dielectric of entire bulk solution including correlated motions of ions, following **Santangelo** 2006¹ used by Kornyshev 2011² with Liu's corrected and consistent Fermi treatment of spheres

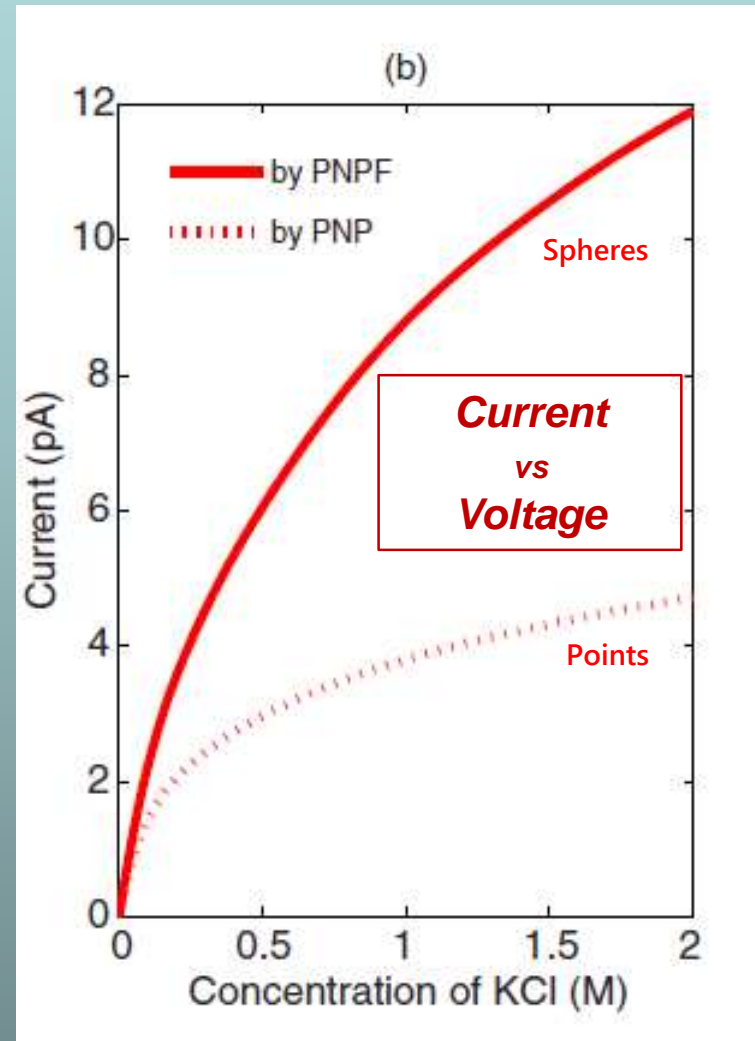
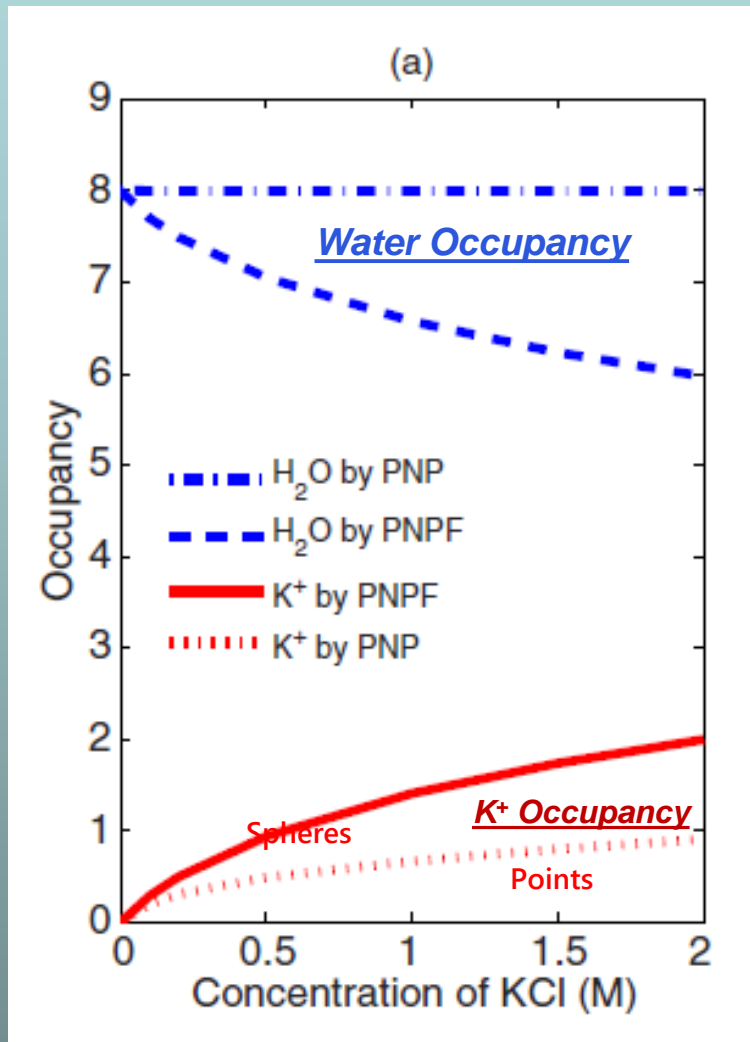
We introduce^{3,4} **two second order equations** and **boundary conditions**

That give the polarization charge density $-\epsilon_{water} \psi = \rho_{pol}$

3D computation is facilitated by using 2nd order equations

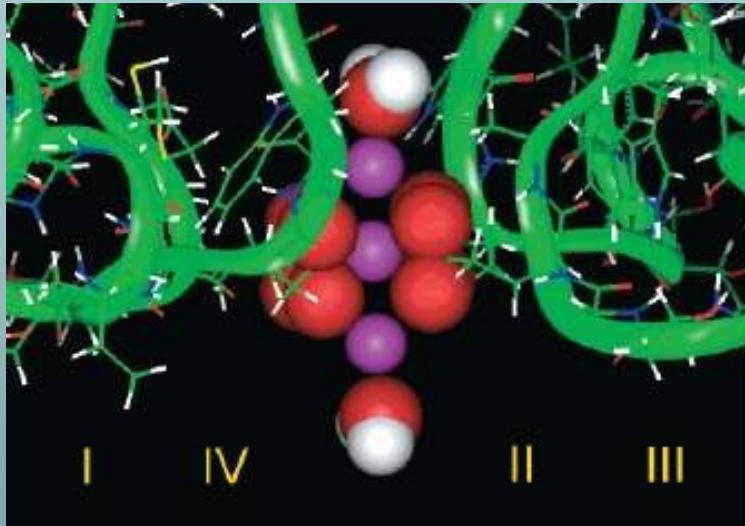
¹PhysRev E (2006) 73:041512 ²PhysRev Ltrs (2011) 106:046102 ³JCompPhys (2013) 247:88 ⁴J PhysChem B (2013) 117:12051

Steric Effect is Large in (*crowded*) Gramicidin PNP spheres **VS** PNP points



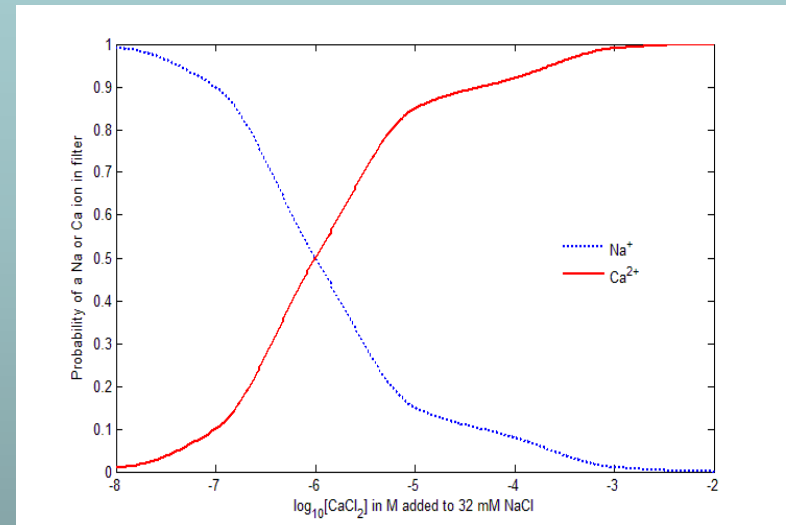
Cardiac Calcium Channel $\text{Ca}_v.n$

Lipkind-Fozzard Model



Ca^{2+} are shown in **violet**,
8 $\text{O}^{0.5-}$ in **red**, H_2O in **white and red**
Lipkind & Fozzard, *Biochem* (2001) **40** 6786

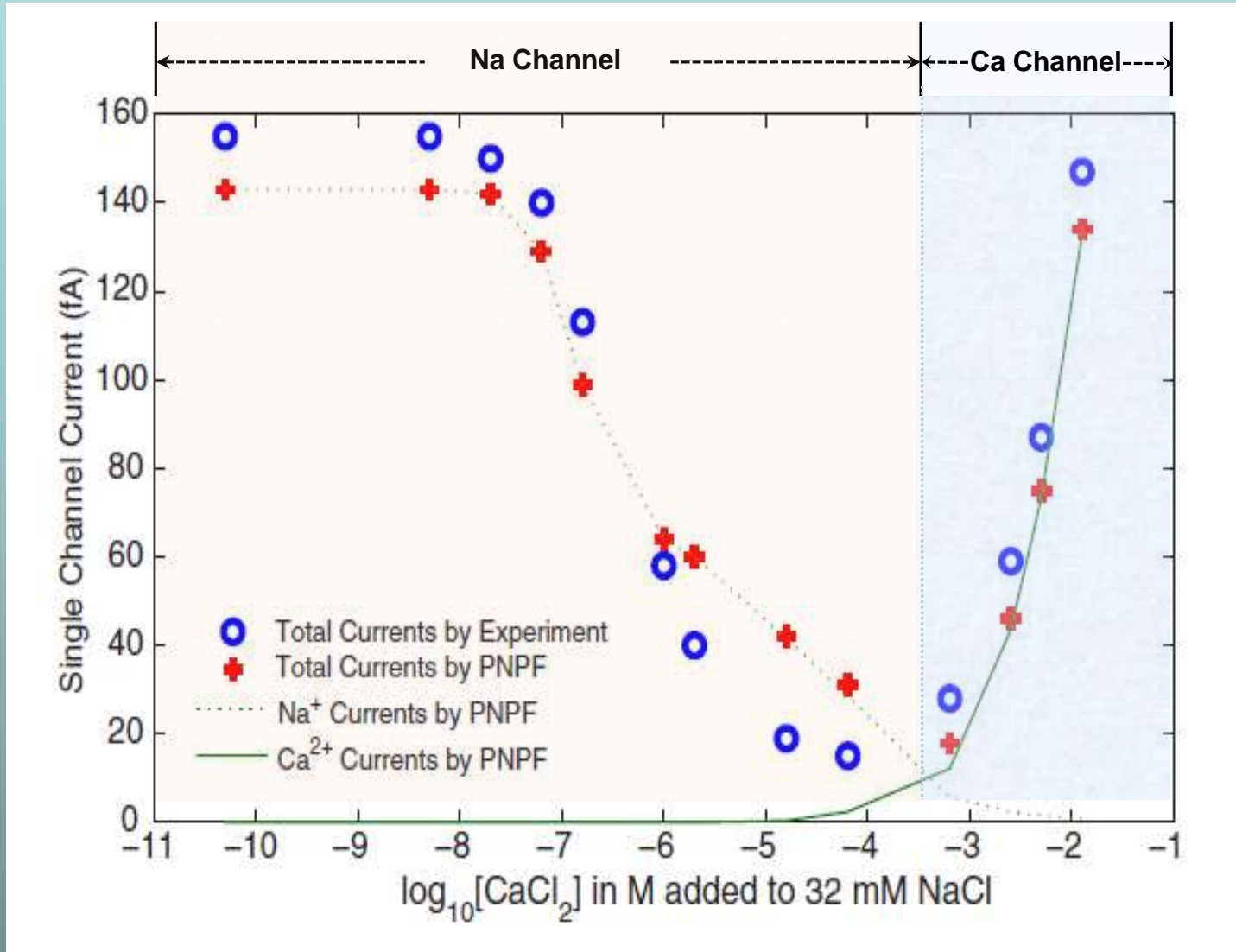
Binding Curve



Liu & Eisenberg J Chem Phys 141(22): 22D532

Cardiac Calcium Channel $\text{Ca}_v1.n$

Experimental Signature *Anomalous** Mole Fraction



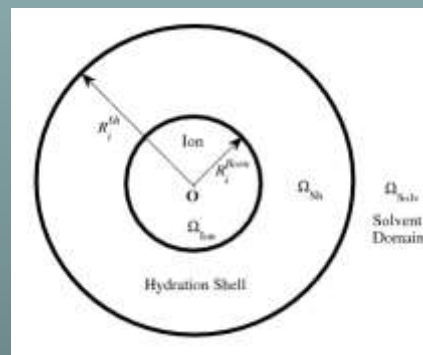
* *Anomalous* because **CALCIUM CHANNEL IS A SODIUM CHANNEL** at $[\text{CaCl}_2] \cong 10^{-3.4}$
 Ca^{2+} is conducted for $[\text{Ca}^{2+}] > 10^{-3.4}$, but Na^+ is conducted for $[\text{Ca}^{2+}] < 10^{-3}$.

Liu & Eisenberg (2015) *Physical Review E* 92: 012711

Poisson Fermi Approach to Bulk Solutions



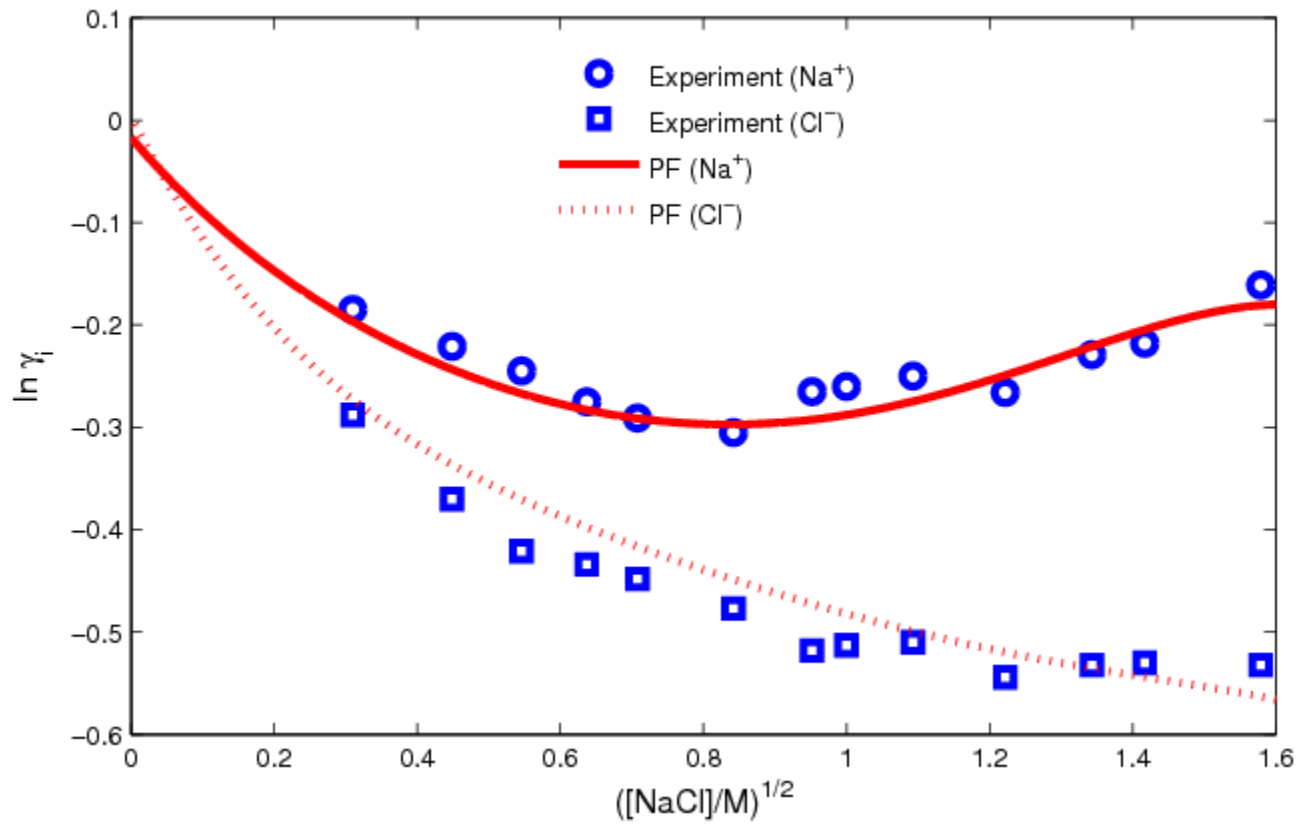
Same Fermi Poisson Equations,
different model of nearby atoms in hydration shells



Activity Coefficients

Na⁺ Cl⁻

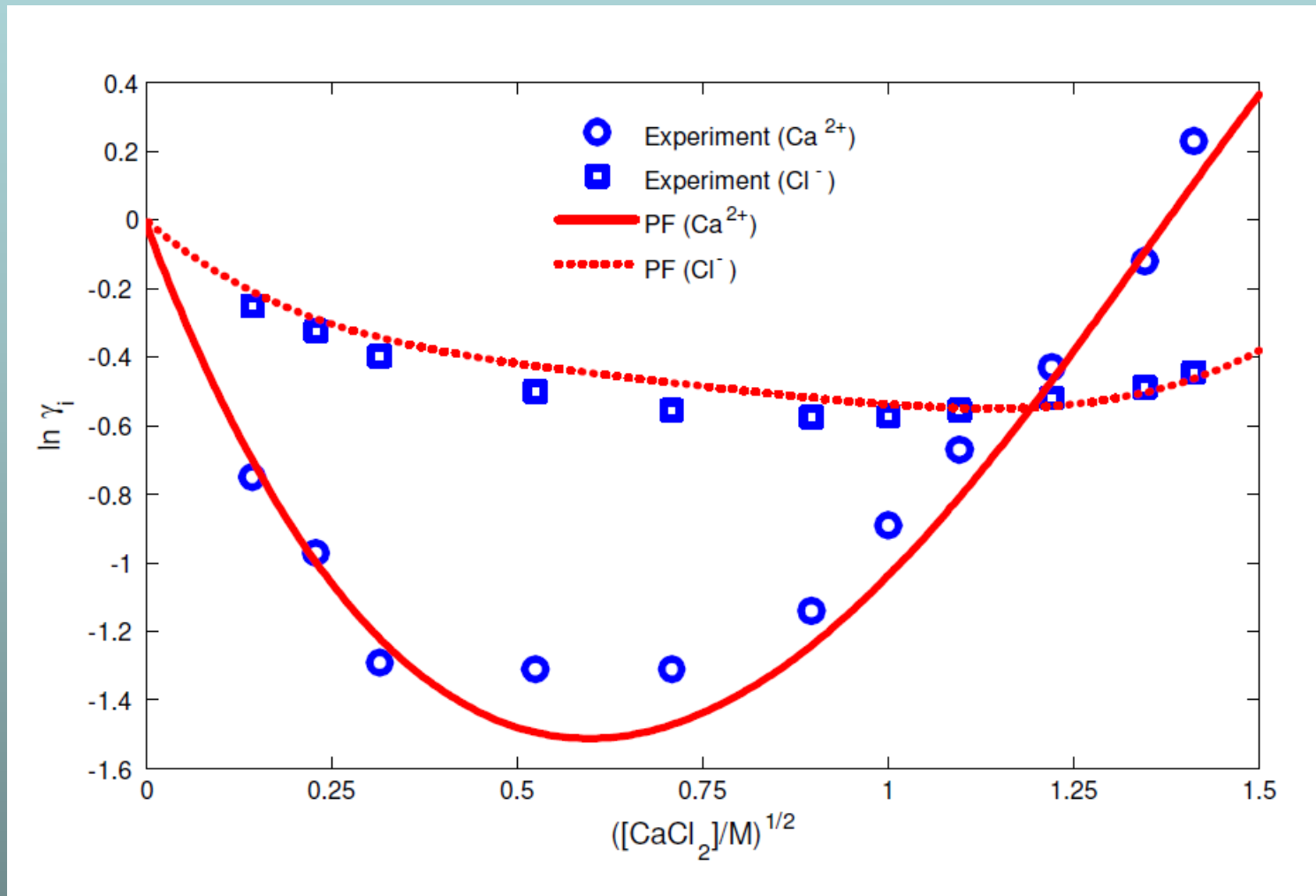
'normalized' free energy per mole



Activity Coefficients

$\text{Ca}^{2+}\text{Cl}_2^-$

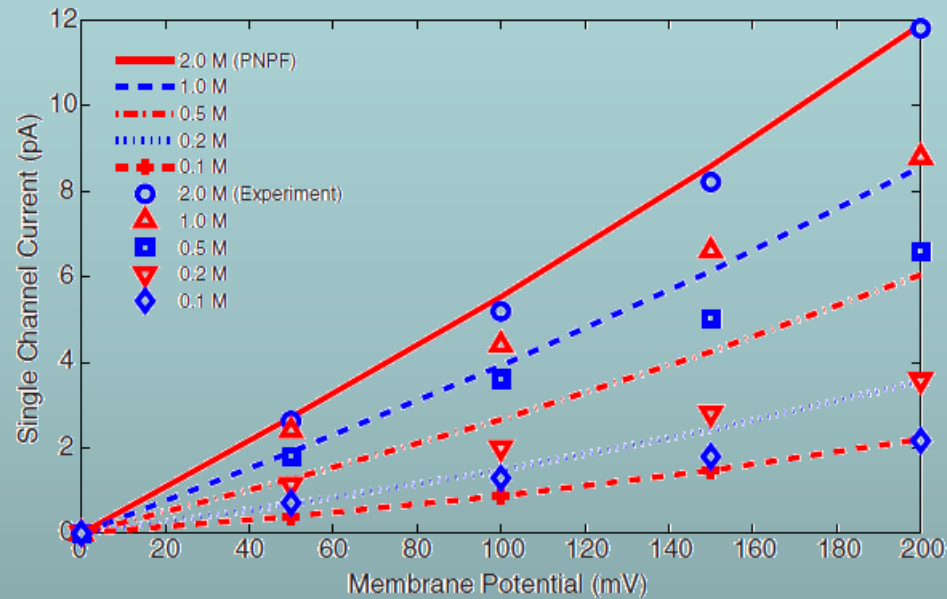
'normalized' free energy per mole



The End

Any Questions?

Three Dimensional Theory Comparison with Experiments Gramicidin A

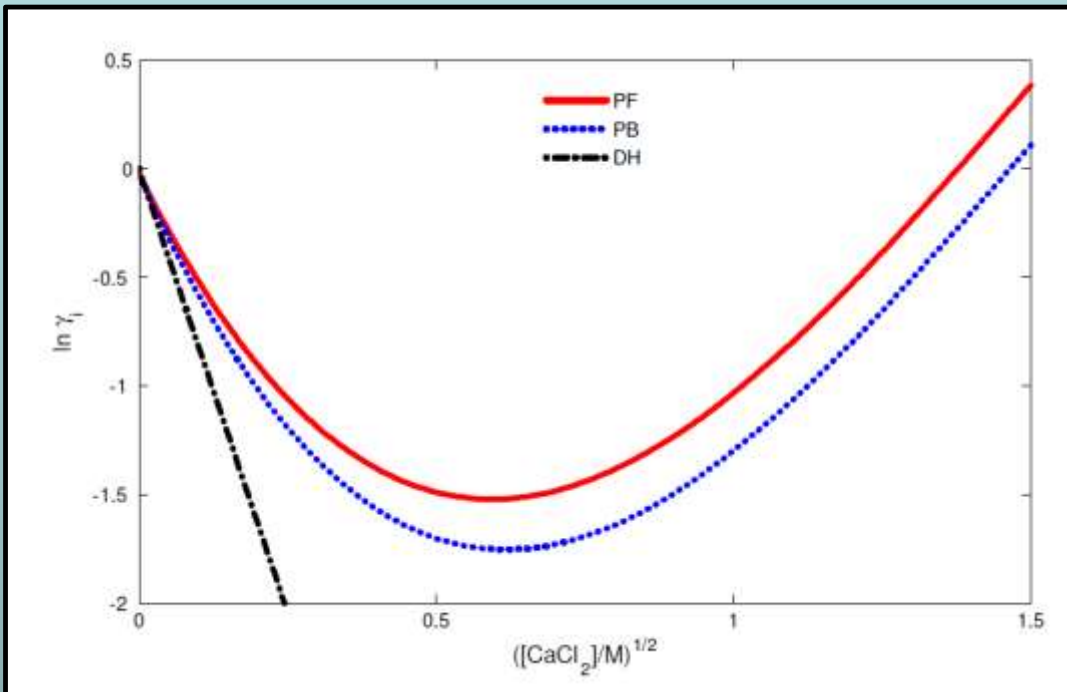


Data from

Cole, Frost, Thompson, Cotten, Cross, & Busath, Biophys J (2002) 83:1974

Theory from *Liu & Eisenberg J ChemPhys 141: 22D532*
with one adjustable parameter never changed

Debye-Hückel Fails Disastrously
 Poisson Boltzmann is quite inaccurate
Poisson Fermi does Surprisingly Well



Parameters, NOT further adjusted

$l_c = 2a_i$	correlation length	$i = \text{Na}^+, \text{Ca}^{2+}, \text{Cl}^-$	Å
$a_{\text{Na}^+}, a_{\text{Ca}^{2+}}$	radii	0.95, 0.99	Å
$a_{\text{Cl}^-}, a_{\text{H}_2\text{O}}$	radii	1.81, 1.4	Å
$R_{\text{Na}^+}^0, R_{\text{Ca}^{2+}}^0, R_{\text{Cl}^-}^0$	Born radii in Eq. (12)	1.617, 1.706, 2.263	Å
$\delta_{\text{Na}^+}, \delta_{\text{Ca}^{2+}}, \delta_{\text{Cl}^-}$	in Eq. (11)	4.2, 5.1, 3.8	
O_i^w	in Eq. (10)	18	

Evidence

(start)

Best Evidence is from the
RyR Receptor

Dirk Gillespie

Dirk_Gillespie@rush.edu



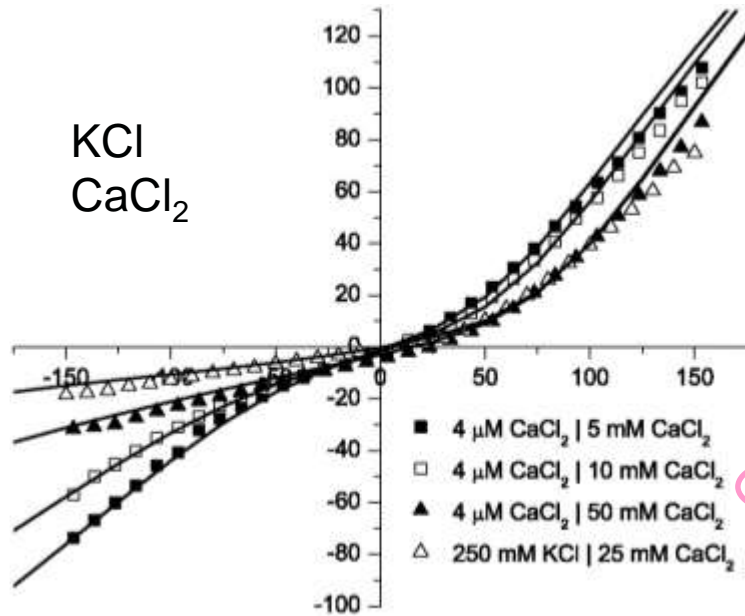
Gerhard Meissner, Le Xu, et al,
not Bob Eisenberg

- **More than 120 combinations of solutions & mutants**
- **7 mutants with significant effects fit successfully**

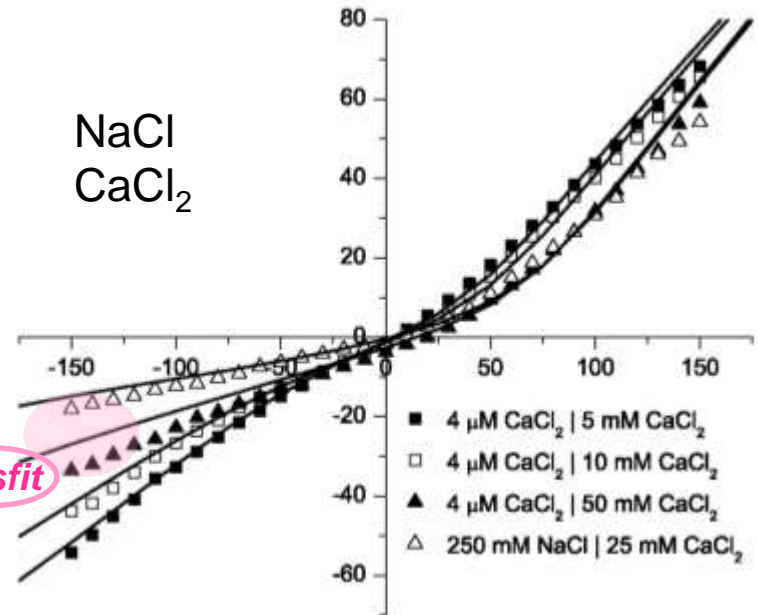
1. Gillespie, D., Energetics of divalent selectivity in a calcium channel: the ryanodine receptor case study. *Biophys J*, 2008. 94(4): p. 1169-1184.
2. Gillespie, D. and D. Boda, Anomalous Mole Fraction Effect in Calcium Channels: A Measure of Preferential Selectivity. *Biophys. J.*, 2008. 95(6): p. 2658-2672.
3. Gillespie, D. and M. Fill, Intracellular Calcium Release Channels Mediate Their Own Countercurrent: Ryanodine Receptor. *Biophys. J.*, 2008. 95(8): p. 3706-3714.
4. Gillespie, D., W. Nonner, and R.S. Eisenberg, Coupling Poisson-Nernst-Planck and Density Functional Theory to Calculate Ion Flux. *Journal of Physics (Condensed Matter)*, 2002. 14: p. 12129-12145.
5. Gillespie, D., W. Nonner, and R.S. Eisenberg, Density functional theory of charged, hard-sphere fluids. *Physical Review E*, 2003. 68: p. 0313503.
6. Gillespie, D., Valisko, and Boda, Density functional theory of electrical double layer: the RFD functional. *Journal of Physics: Condensed Matter*, 2005. 17: p. 6609-6626.
7. Gillespie, D., J. Giri, and M. Fill, Reinterpreting the Anomalous Mole Fraction Effect. The ryanodine receptor case study. *Biophysical Journal*, 2009. 97: p. pp. 2212 - 2221
8. Gillespie, D., L. Xu, Y. Wang, and G. Meissner, (De)constructing the Ryanodine Receptor: modeling ion permeation and selectivity of the calcium release channel. *Journal of Physical Chemistry*, 2005. 109: p. 15598-15610.
9. Gillespie, D., D. Boda, Y. He, P. Apel, and Z.S. Siwy, Synthetic Nanopores as a Test Case for Ion Channel Theories: The Anomalous Mole Fraction Effect without Single Filing. *Biophys. J.*, 2008. 95(2): p. 609-619.
10. Malasics, A., D. Boda, M. Valisko, D. Henderson, and D. Gillespie, Simulations of calcium channel block by trivalent cations: Gd(3+) competes with permeant ions for the selectivity filter. *Biochim Biophys Acta*, 2010. 1798(11): p. 2013-2021.
11. Roth, R. and D. Gillespie, Physics of Size Selectivity. *Physical Review Letters*, 2005. 95: p. 247801.
12. Valisko, M., D. Boda, and D. Gillespie, Selective Adsorption of Ions with Different Diameter and Valence at Highly Charged Interfaces. *Journal of Physical Chemistry C*, 2007. 111: p. 15575-15585.
13. Wang, Y., L. Xu, D. Pasek, D. Gillespie, and G. Meissner, Probing the Role of Negatively Charged Amino Acid Residues in Ion Permeation of Skeletal Muscle Ryanodine Receptor. *Biophysical Journal*, 2005. 89: p. 256-265.
14. Xu, L., Y. Wang, D. Gillespie, and G. Meissner, Two Rings of Negative Charges in the Cytosolic Vestibule of T Ryanodine Receptor Modulate Ion Fluxes. *Biophysical Journal*, 2006. 90: p. 443-453.

Divalents

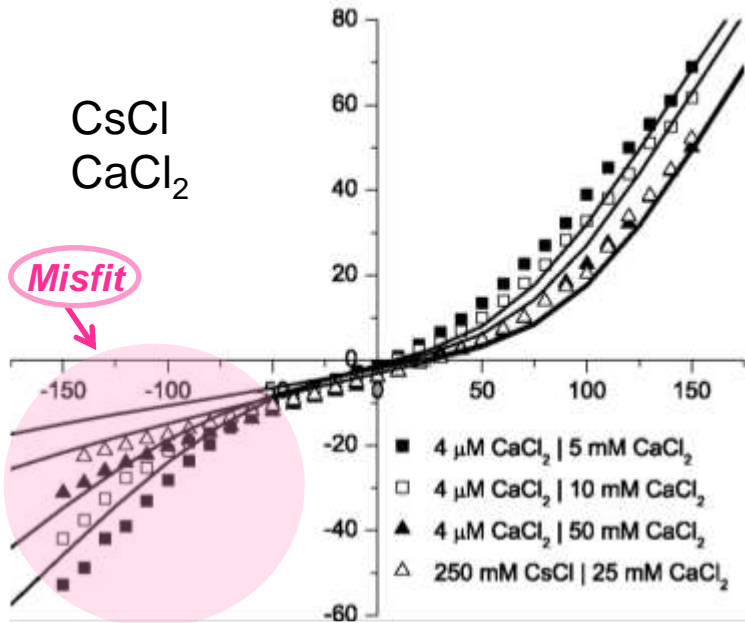
KCl
CaCl₂



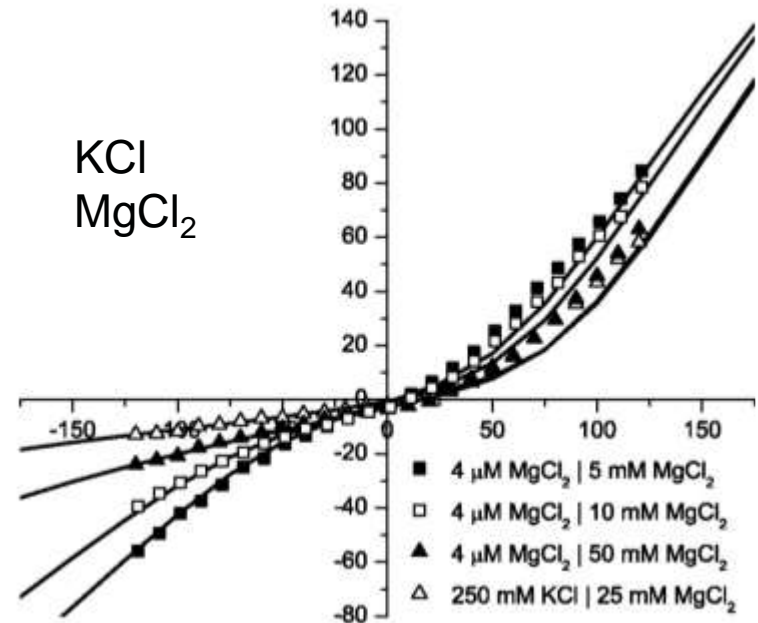
NaCl
CaCl₂



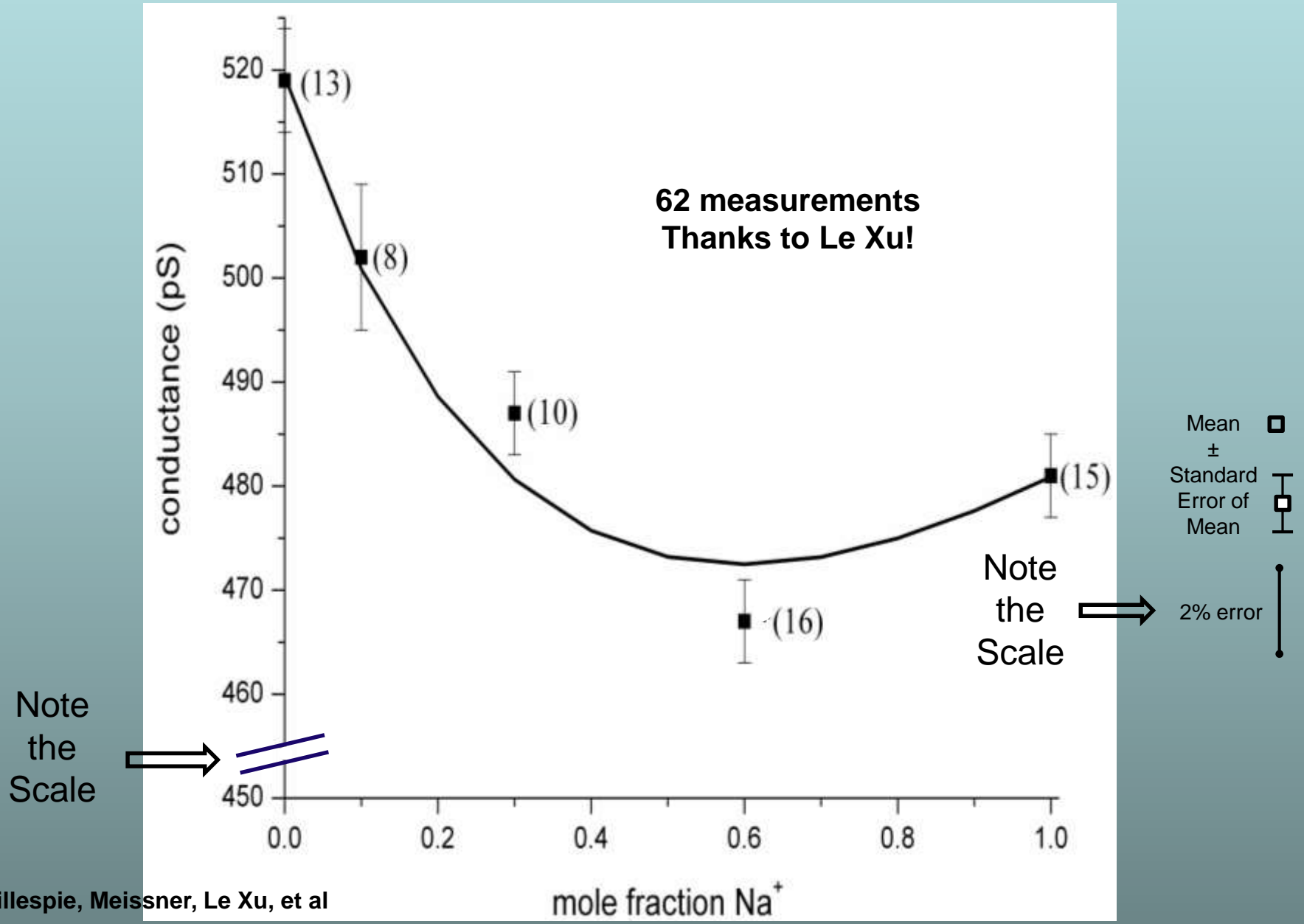
CsCl
CaCl₂



KCl
MgCl₂



The model predicted an AMFE for Na⁺/Cs⁺ mixtures before it had been measured

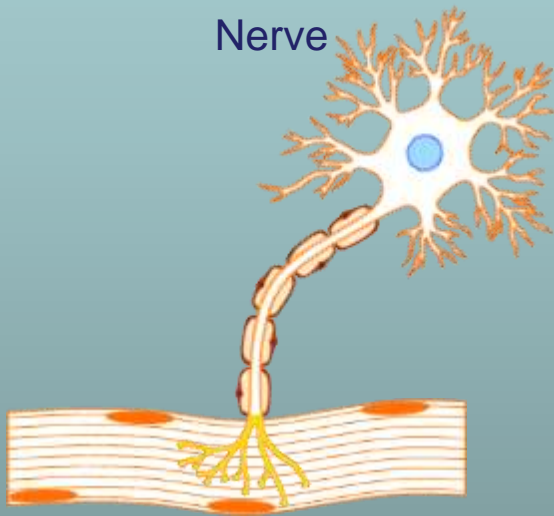


Evidence
(end)

All Spheres Models

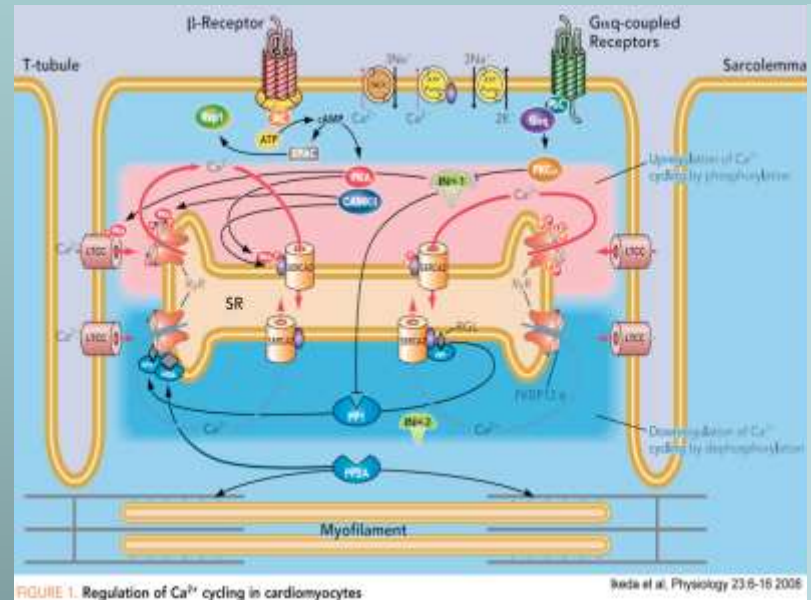
work well for

Calcium and Sodium Channels



Nerve

Skeletal muscle



Heart Muscle Cell

Fermi (like) Distribution

$$C_i(\mathbf{r}) = C_i^{bath} \exp(-\beta_i \phi(\mathbf{r}) + S^{teric}(\mathbf{r}))$$

$$S^{teric}(\mathbf{r}) = \ln(\Gamma(\mathbf{r}) / \Gamma(bath))$$

$\Gamma(bath)$ = bulk void concentration; $\Gamma(\mathbf{r})$ = channel void concentration

Fermi (like) Distribution

is a general

Quantitative Statement of Charge-Space Competition

Simulated and compared to experiments in
> 35 papers of *Boda, Henderson, et al*,
and >10 papers of *Gillespie, et al*,

also gives

Gibbs Fermi Functional

J Comp Phys, 2013 247:88; *J Phys Chem B*, 2013 117:12051

so the Fermi approach

Can be embedded in the **Energy Variational Formulation**

EnVarA developed by **Chun Liu**, more than anyone

Eisenberg, Hyon and Liu (2010). JChemPhys 133: 104104