Energetics of divalent selectivity in a calcium channel: the ryanodine receptor case study

Dirk Gillespie

Department of Molecular Biophysics and Physiology Rush University Medical Center Chicago, IL 60612 dirk_gillespie@rush.edu

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Abstract

A model of the ryanodine receptor (RyR) calcium channel is used to study the energetics of binding selectivity of Ca²⁺ vs. monovalent cations. RyR is a calcium-selective channel with a DDDD locus in the selectivity filter, similar to the EEEE locus of the L-type calcium channel. While the affinity of RyR for Ca²⁺ is in the millimolar range (as opposed to the micromolar range of the L-type channel), the ease of single-channel measurements compared to L-type and its similar selectivity filter make RyR an excellent candidate for studying calcium selectivity. A Poisson-Nernst-Planck/Density Functional Theory model of RyR is used to calculate the energetics of selectivity. Ca²⁺ vs. monovalent selectivity is driven by the charge/space competition mechanism in which selectivity arises from a balance of electrostatics and the exclude volume of ions in the crowded selectivity filter. While electrostatic terms dominate the selectivity, the much smaller excluded-volume term also plays a substantial role. In the D4899N and D4938N mutations of RyR that are analyzed, substantial changes in the chemical potential profiles are found far from the mutation site. These changes result in the significant reduction of Ca²⁺ selectivity found both theory and experiments.

Introduction

Calcium-selective ion channels play an important role in many physiological functions including in the excitation-contraction (EC) coupling pathway that links surface membrane excitation and calcium-dependent muscle contraction. Cardiac muscle EC coupling involves two kinds of calcium channels: depolarization of the transverse tubule activates the voltage-dependent L-type calcium channel (a.k.a. the dihydropyridine receptor) that generates a Ca²⁺ influx that activates nearby ryanodine receptor (RyR) calcium channels. RyR, in turn, conducts Ca²⁺ out of the sarcoplasmic reticulum, a Ca²⁺-storage organelle. It is this large Ca²⁺ release that regulates muscle contraction.

The L-type and RyR calcium channels have very different physiological functions. The L-type channel mediates a relatively small Ca²⁺ flux to locally activate RyR while RyR mediates a large Ca²⁺ flux to globally elevate cytosolic [Ca²⁺]. To accomplish these functions, the L-type and RyR calcium channels have very different permeation and selectivity properties: the L-type channel has a small conductance (1) and micromolar Ca²⁺ affinity (2,3) while RyR has a large conductance and only millimolar Ca²⁺ affinity (4). On the other hand, both the L-type and RyR calcium channels have negatively-charged, carboxyl-rich selectivity filters, the EEEE locus of L-type (5,6) and the DDDD locus of RyR (with a neighboring EEEE locus) (7). Therefore, it is plausible that both channels share a mechanism for selectivity that is determined by the EEEE/DDDD locus. In this paper, a model of RyR is used to understand how a EEEE/DDDD locus leads to a Ca²⁺-selective channel. RyR is used because a model of permeation through it already exists (and is expanded on here) and because it is relatively easy to perform single-channel measurements, providing a very large data set to work with.

Selectivity in calcium channels has been modeled most recently with general studies by Boda et al. (including the author) (8-12), specific studies of the L-type channel by Nonner et al. (13,14) and Corry et al. (15,16), and RyR by Chen et al. (17-19) and the author (20). From these studies two schools of thought have emerged with regard to why calcium channels prefer to bind/conduct Ca²⁺ over high levels of background monovalent cations. Corry et al. (15,16) argue that the L-type channel must be a single-filing channel and that Ca²⁺ is preferred because calcium ions see a much larger electrostatic energy well from the four glutamates than monovalent ions

(16). On the other hand, Nonner, Boda, the author, and co-workers argue that calcium channels have a small (but *not* single-filing) and crowded selectivity filter that prefers Ca²⁺ over monovalent cations because of the balance of electrostatic and excluded-volume forces (i.e., two ions cannot overlap) (8-12,14,20-22). For example, two Ca²⁺ can balance the four negative glutamates in half the volume of four Na⁺, a mechanism called charge/space competition (CSC).

Both schools argue that they qualitatively reproduce the important characteristics of the L-type channel (e.g., the anomalous mole fraction effect, AMFE, where micromolar concentrations of Ca²⁺ block Na⁺ current), but both have problems in fully testing their hypotheses. For example, it is not practical for Corry et al. (or any particle simulation method) to simulate the low voltages and low Ca²⁺ concentrations where almost all experiments have been done. Instead, they extrapolate four orders of magnitude between their simulation data at 18 mM Ca²⁺ to 1 µM Ca²⁺ where the AMFE is experimentally observed (15). Moreover, they only simulate Ca²⁺ vs. Na⁺ selectivity and do not simulate other monovalent cations to see if their theory is consistent with experiments. They also do not simulate monovalent vs. monovalent selectivity (e.g., Na⁺ vs. K⁺). This makes it difficult to determine by what mechanism their model channel distinguishes between monovalents, which they are known to do (1); *a priori*, electrostatics alone would not seem to be enough. Moreover, the physical forces used by a channel to distinguish one monovalent from another must also be present in divalent vs. monovalent selectivity. Monovalent vs. monovalent selectivity is likely a point where the two models give qualitatively different results.

On the other hand, much of the work on the CSC mechanism has been done with equilibrium simulations that do not compute current, but only channel occupancy (8-12,14). When current was computed, it required data-fitting of excess chemical potentials (see below) (13,18,19)—rather than using a theory to compute them—which gave reasonable values for these potentials and reproduced the AMFE of the L-type channel (14). Much of the effort by the CSC school has been directed at studying a wide range of selectivity including Ca²⁺ vs. different monovalents (9,14,21) and monovalent vs. monovalent selectivity (9,12) to show that a crowded filter prefers small, high-valence cations. In recent work they have also shown that reducing both the pore radius and the protein polarization can account for the very different Ca²⁺ affinities observed in L-type and RyR channels (11,12). These studies have shown mechanisms that work in principle. Recent mutations of OmpF porin have started to experimentally verify these predictions (23-25).

To move these theories beyond "in principle," a model of a real calcium channel that reproduces—and predicts—the experimental data over a wide range of ionic conditions and mutations is vital. Many models can account for selectivity under a small set of conditions, but to distinguish between them and to have confidence in any model, a large experimental data set is necessary. In this paper, a model that quantitatively reproduces and predicts RyR experimental data in over 100 different ionic solutions is used to study the energetics of selectivity in RyR. The experimental verification of one of these predictions is also shown here. Specifically, the model predicted an AMFE between Ca²⁺ and monovalent cations (Na⁺ and Cs⁺). In this AMFE, current is reduced by up to 65% which is large, but not as dramatic as the >90% reduction found in the L-type calcium channel (2).

The Poisson-Nernst-Planck/Density Functional Theory (PNP/DFT) model used here computes quickly (minutes for a whole current/voltage curve), computes the excess chemical potentials from thermodynamic formulas, and uses exactly nine experimental data points to determine the ion diffusion coefficients of seven ion species. Another advantage of the

PNP/DFT model is that it naturally computes the components of the chemical potential of the ions. That decomposition is used here to dissect Ca²⁺ vs. monovalent selectivity in both native and mutant RyR. It is found that different terms are important under different circumstances. Also, in mutations differences between mutant and native can extend 7.5 Å beyond the mutation site. The results indicate the Ca²⁺ vs. monovalent cation selectivity in RyR is driven by the CSC mechanism.

Theory and methods

The Poisson-Nernst-Planck/Density Functional Theory model

The flux through the RyR pore is described by a constitutive relationship that is a generalization of the Poisson-Nernst-Planck (PNP) equations (26-29):

$$-\mathbf{J}_{i}(\mathbf{x}) = \frac{1}{kT} D_{i}(\mathbf{x}) \rho_{i}(\mathbf{x}) \nabla \mu_{i}(\mathbf{x})$$
(1)

where J_i , D_i , ρ_i , and μ_i are the local flux density, diffusion coefficient, density, and chemical potential, respectively, of ion species i. k is the Boltzmann constant and T is the temperature. The chemical potential is decomposed into different terms (14,22,30-34):

$$\mu_{i}(\mathbf{x}) = kT \cdot \ln \left(\frac{\rho_{i}(\mathbf{x})}{\Lambda_{i}^{3}}\right) + \sum_{i=0}^{\text{mean electrostatic}} z_{i}e\phi(\mathbf{x})$$

$$+ \mu_{i}^{\text{SC}}(\mathbf{x}) + \mu_{i}^{\text{HS}}(\mathbf{x})$$
(2)

where e is the elementary charge and where the length scale is the de Broglie wavelength Λ_i (35) and z_i is the valence of ion species i.

In this decomposition of the chemical potential, there are two electrostatic terms and an excluded-volume term in addition to the usual ideal gas term. The mean electrostatic potential ϕ is given by the average (i.e., long-time, many particle ensemble average) ion densities via the Poisson equation:

$$-\varepsilon_0 \nabla \cdot (\varepsilon(\mathbf{x}) \nabla \phi(\mathbf{x})) = e \sum_i z_i \rho_i(\mathbf{x})$$
(3)

where ε_0 is the permittivity of free space and ε is the local dielectric coefficient. The sum on the right-hand side includes both the densities of the permeating ions and the protein charge densities. If the chemical potential is defined with only the ideal gas and mean electrostatic terms, then Eqs. (1) and (3) reduce to the normal PNP equations of charged, point ions.

The mean electrostatic potential is only part of the electrostatics in electrolytes. To compute ion density profiles, the electrostatic potential that should be used is, in principle, given by the Poisson equation with *conditional* concentrations (not average) on the right-hand side of Eq. (3). These conditional concentrations are the concentration of species i at \mathbf{x} given an ion of species j fixed at location \mathbf{y} (the "fixed ion") and can be expressed via pair correlation functions (29,34). This conditional concentration profile is the result of how well all the ions within a screening (Debye) length of the fixed ion arrange around it. This depends on the ions' size and charge. The timescale of this ionic screening is orders of magnitude faster than that of the mean electrostatic potential that is calculated from the ion concentrations averaged over the permeation timescale of microseconds. A well-known approximation of this term (not used here) is the

Debye/Hückel theory (34,36). In the DFT, this conditional concentration approach is approximated by splitting the electrostatics into the mean electrostatic and screening terms as described (22,32,33,37,38).

The last term in Eq. (2) describes the energy required to insert an *uncharged* ion at any location. In this paper, ions are modeled as charged, hard spheres and water as an uncharged, hard sphere, and therefore excluded volume is purely due to hard-sphere (HS) repulsion. The screening term also includes ion size, but is much less sensitive to changes in ion size than the excluded-volume term (see below).

Both the screening and excluded-volume terms are computed using DFT of classical fluids (*not* electron orbitals). DFT is currently one of the state-of-the-art theories in physics of confined fluids (e.g., see the reviews by Evans (35) and Wu (31)). The specific DFT of charged, hard spheres used here has been tested against multiple Monte Carlo simulations to assess its accuracy (22,33,38).

The work shown in this paper is computed with a one-dimensional approximation of Eqs. (1)-(3) that was described previously (13,39) where the dielectric coefficient ε was constant at 78.4 throughout the system. How the model pore and input parameters were determined from experimental data is described in the Appendix. Also in the Appendix are comparisons between the model and experiments.

The geometry of the model RyR pore is shown in Fig. 1.

Analysis of binding selectivity

The energetics of ion binding within the pore is most easily analyzed in equilibrium when no currents from any ion species are flowing (i.e., $J_i = 0$ for all ion species) and the chemical potential is constant throughout the system (in the baths and the pore):

$$\mu_i^{\text{bath}} = \mu_i^{\text{pore}}(x). \tag{4}$$

In this paper the baths are identical in concentration and composition, and all the analysis of selectivity is done in equilibrium based on the decomposition of the chemical potential described above (Eq. (3)).

AMFE experiments

The experimental results shown in Fig. 2 were measured by the lab of Michael Fill (Rush University Medical Center) using standard, previously described methods (40). These experiments were performed on the cardiac isoform (RyR2) that still had regulatory proteins (e.g., the negatively-charged calsequestrin) attached to them. In this way, these channels are different from the "purified" RyR channels for which the theory was originally developed (7,20,41). This may contribute to the larger discrepancies between theory and experiment than those described in the Appendix. Nevertheless, the model is in very good agreement with experiment. The experiments were performed *after* the theoretical calculations to test the predictive power of the model. No parameters were changed in the model to better reproduce the experimental data.

Results

AMFE for Ca²⁺ and monovalent cations

Several mole fraction experiments have been performed in RyR, both for mixtures of monovalent cations with other monovalents and mixtures of divalents with other divalents (42,43). In these experiments, the relative concentrations of two ion species was changed while the total concentrations of both species was kept constant and the conductance was measured as a function of mole fraction. None of these experiments showed a minimum (an AMFE) until the RyR model of Gillespie et al. (20) predicted an AMFE for mixtures of Na⁺ and Cs⁺. This was experimentally verified after the model calculations were done (Fig. 20A in the Appendix).

Here we present another AMFE prediction of the RyR model, this time in mixtures of Ca²⁺ and Cs⁺ as well as Ca²⁺ and Na⁺. Because millimolar Ca²⁺ concentration on the cytosolic side of RyR decreases open probability (44), it is not possible to perform mole fraction experiments with symmetric bath conditions. Instead, we follow Almers, McCleskey, and Palade (2) who used symmetric, fixed concentrations of a monovalent cation and only increased lumenal [Ca²⁺]. This protocol produced the classical AMFE in the L-type calcium channel that showed the block of Na⁺ current by micromolar Ca²⁺ (2,3).

The calculations were completed—with all model parameters fixed—before the experiments were performed. The model predicted not only the presence of a minimum, but also that the minimum for Cs^+ would be deeper than for Na^+ . Specifically, the theory predicted a reduction in current of 47% for Na^+ at 1 mM Ca^{2+} (compared to 1 μ M Ca^{2+}) and a 59% reduction in current for Cs^+ . The experimental results were 42% and 65%, respectively (Fig. 2). Moreover, the theory predicted that 10 μ M Ca^{2+} added to Na^+ would not substantially change the net current (Fig. 2, the two left-most squares) while 10 μ M Ca^{2+} added to Cs^+ would decrease net current by about 20% (Fig. 2, the two left-most circles). These results and those shown in the Appendix (Fig. 22) indicate that the model can accurately reproduce Ca^{2+} vs. monovalent cation selectivity data over a very wide range of conditions (i.e., 0–50 mM Ca^{2+} ; –150 to +150 mV applied voltage; Na^+ , K^+ , and Cs^+ as monovalents).

More study is planned to understand the molecular origin of the AMFE in RyR. However, the calculations show that the AMFE in RyR does *not* require the correlated motion of multiple ions through a long, single-filing pore (45), because the model pore does not include a single-filing selectivity filter (it is 8 Å in diameter). Moreover, the model does not include the conservation of momentum necessary to model correlated ion motion; the Nernst-Planck equation used to describe ion flux (Eq. (1)) only includes conservation of mass (46,47). In general, the physical interpretations of the AMFE are highly model-dependent. Because classical barrier models of ion permeation do not include the physics known to exist in electrolytes, using these models to infer the occupancy—or any property—of a channel is problematic (13,17,48-50).

Dependence of Ca2+ vs. K+ selectivity on bath Ca2+ concentration

To study binding selectivity (i.e., the amount of an ion species that accumulates at one location in the pore), it is easiest to analyze the equilibrium situation where the chemical potential of each ion species is constant in the baths and within the pore (Eq. (4)). In this case, the baths must be identical in ionic composition and concentration. Then, the partitioning of ion species i between the bath and location x in the pore can be written as

$$\ln\left(\frac{\rho_i(x)}{\rho_i^{\text{bath}}}\right) = -\frac{z_i e}{kT}\phi(x) - \frac{\Delta\mu_i^{\text{SC}}(x)}{kT} - \frac{\Delta\mu_i^{\text{HS}}(x)}{kT}.$$
 (5)

where $\Delta \mu_i^{\text{SC}}(x)$ indicates the screening chemical potential at x minus the bath value (and similarly for the HS term). Each of these terms are shown in Figs. 3–6 for a bath containing 150 mM KCl and varying amounts of CaCl₂ ranging from 1 μ M to 50 mM. In these figures, a negative term favors partitioning from the bath into the pore while a positive term indicates that for this component the ion is more energetically stable in the bath.

Fig. 3 shows the partitioning coefficient plotted logarithmically (the left-hand side of Eq. (5)) for K⁺ and Ca²⁺ (panel B). For K⁺ (panel A), the bath concentration is held constant and so the decrease in partitioning as $[Ca^{2+}]$ increases is a direct result of K⁺ being replaced by Ca^{2+} everywhere within the pore. For Ca^{2+} (panel B) on the other hand, partitioning reflects both an increase in $\rho_{Ca}(x)$ within the pore, but also an increase in bath $[Ca^{2+}]$. Even though more and more Ca^{2+} enters the pore as $[Ca^{2+}]$ increases, the ratio of $\rho_{Ca}(x)$ to $[Ca^{2+}]$ —the partitioning—decreases as more Ca^{2+} is added to the bath; the increase of Ca^{2+} concentration in the pore is proportionately smaller than the increase of Ca^{2+} concentration in the baths.

Fig. 4 shows the *mean electrostatic* component $z_i e \phi(x)$ of the partitioning in Eq. (5). Because Ca²⁺ has twice the charge of K⁺ this component is twice as large for Ca²⁺ (panel B) as for K⁺ (panel A). For both ion species, this term makes up much more than half of the partitioning. Also, it is important to note that $\phi(x)$ changes from a deep well in the selectivity filter when [Ca²⁺] is low to being very close to zero throughout the channel when [Ca²⁺] is high; the mean electrostatic potential changes significantly as [Ca²⁺] changes. This indicates that the *entire* pore is becoming more and more charge-neutral (on average over a long-time and many particles passing through the channel) as [Ca²⁺] is increased. It must be the entire pore that is becoming electroneutral because any significant net charge in any region of the pore would create an electrostatic potential well or barrier in the electrostatic potential profile computed from the Poisson equation (Eq. (3)).

Fig. 5 shows the screening component of the partitioning $\Delta \mu_i^{\text{SC}}(x)$ in Eq. (5) that describes the electrostatics beyond the mean electrostatic component (i.e., the component computed from Eq. (3)). These correlations due to electrostatics are most intuitively described as the ion's ability to screen the charge of another ion and therefore this component is called the *screening* (SC) component. In general, the smaller or higher-valence ion screens a charge more efficiently than the larger or lower-valence ion. This is reflected in Fig. 5 by the much more negative screening term for Ca²⁺ (dashed lines) compared to the slightly negative screening term for K⁺ (solid lines). This component of the partitioning is always negative (favoring partitioning into the pore) and changes little as $[Ca^{2+}]$ increases.

Fig. 6 shows the hard-sphere (HS) component $\Delta \mu_i^{\text{HS}}(x)$ in Eq. (5) that describes the contribution of the ions' excluded volume; it is the excess chemical potential of an uncharged, hard-sphere fluid with the same density profile $\rho_i(x)$ as the ionic fluid. This *excluded-volume* term is positive, indicating that it is more difficult to insert an ion-sized particle into the selectivity filter than into the bath. The size of the ions hinders ion partitioning into the pore from the bath. This term is, however, small in the pore (<1 kT), and, in general, the smaller the ion, the smaller the excluded-volume term. Like the screening term, $\Delta \mu_i^{\text{HS}}(x)$ changes little as $[\text{Ca}^{2+}]$ increases.

While these profiles are useful for understanding the partitioning of one ion species into the pore, by themselves they do not show why one ion species is favored over another because they do not directly compare two ion species. For this, the difference in the partitioning between the two ion species (K^+ and Ca^{2+} in this example) is necessary. Specifically, the relative concentrations in the pore are considered:

$$\frac{\ln\left(\frac{\rho_{\text{Ca}}(x)}{\rho_{\text{K}}(x)}\right) = \ln\left(\frac{\left[\text{Ca}^{2^{+}}\right]}{\left[K^{+}\right]}\right) + \left(z_{\text{K}} - z_{\text{Ca}}\right) \frac{e\phi(x)}{kT}}{\left[K^{+}\right]} + \frac{1}{kT}\left(\Delta\mu_{\text{K}}^{\text{SC}}(x) - \Delta\mu_{\text{Ca}}^{\text{SC}}(x)\right)}{\left[kT\right]} + \frac{1}{kT}\left(\Delta\mu_{\text{K}}^{\text{HS}}(x) - \Delta\mu_{\text{Ca}}^{\text{HS}}(x)\right) \tag{6}$$

Here, the *binding selectivity* is defined by the ratio of the ion concentrations in the pore and by Eqs. (2) and (5) is naturally decomposed into four energetic *advantages*, energy differences that each favor the binding of one ion species over the other. In this case, a positive term favors the binding of Ca²⁺ while a negative term favors K⁺.

It is more convenient to describe the energetics of binding selectivity with a single number rather than an entire profile (like in Figs. 3–6), and so only the relative concentrations of Ca^{2+} and K^{+} in Eq. (6) in the middle of the Asp-4899 region (i.e., at x = 20 Å) are considered. This location is chosen because it is representative of the changes in general, as well as being the location where ion concentration are highest and ion selectivity occurs.

All the terms of Eq. (6) are shown in Fig. 7 for $[Ca^{2+}]$ ranging from 1 μ M to 50 mM. As $[Ca^{2+}]$ increases, the overall binding selectivity of Ca^{2+} increases (solid line). This displacement of K^+ by Ca^{2+} is determined by how each of the terms in Eq. (6) changes as $[Ca^{2+}]$ increases:

- (1) Number advantage (horizontal-hatched column). The only term that favors K^+ binding in the pore is its number advantage; there is more K^+ in the baths than Ca^{2+} and therefore it is more probable that a K^+ ion enters the channel. Even this advantage is overcome by the electrostatic and excluded-volume terms at just 0.1 mM $CaCl_2$ in the bath. It is important to note, however, that the number advantage is physiologically real; with $[Ca^{2+}]$ at 1 mM (approximately the free Ca^{2+} in the sarcoplasmic reticulum) the K^+ number advantage is 5 kT, just 1 kT less than the combined electrostatic terms (the diagonal- and cross-hatched bars in Fig. 7). This term is especially important for the L-type Ca^{2+} channel where the Ca^{2+} affinity of the channel is 1 μ M and the number advantage for K^+ is 12 kT.
- (2) Mean electrostatic advantage (diagonal-hatched column). The mean electrostatic potential inside the pore always favors Ca^{2+} , but it reduces to almost zero as $[Ca^{2+}]$ becomes comparable to $[K^+]$ (see also Fig. 4). The long-ranged average electrostatic potential only attracts Ca^{2+} to the pore when $[Ca^{2+}]$ is low. When $[Ca^{2+}]$ becomes comparable to $[K^+]$, this attraction is quite small and it is the decrease in the number advantage of K^+ that favors Ca^{2+} binding in this case (since the two other terms are virtually unchanged as $[Ca^{2+}]$ increases, as described below).
- (3) Screening advantage (cross-hatched column). When [Ca²⁺] is higher than about 0.1 mM, then the largest term favoring Ca²⁺ binding in the pore is the screening advantage of Ca²⁺. Fig. 5 showed that the screening term of Ca²⁺ in the selectivity filter was approximately -4.5 kT

while for K^+ it was only about -1 kT; the large difference in these terms is the 3.5 kT screening advantage for Ca^{2+} shown in Fig. 7. Most importantly, this screening advantage is *unchanged* as $[Ca^{2+}]$ is increased to provide the largest continuous preference for Ca^{2+} over K^+ (and over other monovalent cations as described below). While the excluded-volume advantage of Ca^{2+} is also unchanged, that term is much smaller (see below). Also, the mean electrostatic potential can be larger than the screening advantage, but that term decreases to only 0.5 kT as $[Ca^{2+}]$ increases (see above).

(4) Excluded-volume advantage (solid column). This term is also unchanged as $[Ca^{2+}]$ is increased, but at approximately 0.5 kT it is generally the smallest term favoring Ca^{2+} binding in the pore. Because Ca^{2+} ions are smaller than K^+ ions (diameters of 2 Å vs. 2.76 Å, respectively), it easier to insert a Ca^{2+} ion into the crowded pore than a K^+ ion. While the excluded-volume advantage of Ca^{2+} is generally small, this term does have a significant effect on Ca^{2+} vs. monovalent selectivity as described below.

Combining these results, it is clear that the origin of the Ca²⁺ selectivity of RyR is electrostatics; the sum of the mean electrostatic and screening advantages is enough to overcome the large number advantage of K⁺. However, the average electrostatic attraction of the Ca²⁺ ions from any net charge in the selectivity filter that is not solely responsible for the selectivity. While a Ca²⁺ ion always "feels" twice the electrostatic pull that a K⁺ ion does because of its two positive charges, the net charge throughout the pore is close to zero in the pore as [Ca²⁺] increases above 10 mM (Fig. 7); that is, there is little electrostatic pull on the cations (on average) to move into the pore at high [Ca²⁺]. When [Ca²⁺] becomes comparable to [K⁺] it is *only* the superior ability of the Ca²⁺ to screen the protein charges that favors Ca²⁺ accumulation in the pore because all other terms are small in comparison. The number advantage is also an important term. Not only is it *physiologically present*, but when [Ca²⁺] is less than about 3 mM Ca²⁺ (the physiological upper limit in the sarcoplasmic reticulum) it is larger than any other single term. Moreover, when considering the L-type Ca²⁺ channel that has a Ca²⁺ affinity of 1 µM, the monovalent number advantage is a whopping 12 kT that must be overcome by the other terms.

Role of monovalent size in Ca2+ vs. monovalent cation selectivity

In vivo, RyR must select Ca²⁺ ions from a background of K⁺ ions, but *in vitro*, many different kinds of cations can be used. An important check for any theory that reproduces the Ca²⁺ vs. K⁺ selectivity is to use the same pore model to reproduce the selectivity data of different monovalent cations. The model of RyR described here does this. Besides the figures shown in the Appendix, Fig. 2 shows that the model can *predict* measurable differences in the selectivity of Ca²⁺ vs. Na⁺ and Ca²⁺ vs. Cs⁺. These two monovalents were chosen because they have similar conductances through RyR, and therefore any differences are mainly due to their size difference (Na⁺ and Cs⁺ diameters are 2 Å and 3.42 Å, respectively (51)).

The significant changes that occur when different monovalent cations compete with Ca^{2+} for the pore can be seen in Fig. 8. In this figure, the concentration profiles of the monovalents and Ca^{2+} in the pore are shown for $[X^+] = 150$ mM $(X^+ = Li^+, Na^+, K^+, and Cs^+, listed from smallest to largest) and <math>[Ca^{2+}] = 1$ mM. As monovalent diameter increases from 1.33 Å for Li^+ to 3.42 Å for Cs^+ , the monovalent concentration throughout the pore decreases and the Ca^{2+} concentration increases. Within the selectivity filter itself, there is a >80% decrease in monovalent selectivity $(Cs^+ vs. Li^+)$ and a 40% increase in Ca^{2+} concentration. To understand

this substantial change, Fig. 9 shows the chemical potential decomposition of Eq. (6) for different monovalents:

- (1) Number advantage (horizontal-hatched column). This term is constant since $[Ca^{2+}]$ and $[X^{+}]$ are constant.
- (2) Mean electrostatic advantage (diagonal-hatched column). All of the monovalents create the same mean electrostatic potential inside the selectivity filter and therefore this advantage for Ca²⁺ accumulation is constant.
- (3) Screening advantage (cross-hatched column). Ca²⁺ still has a screening advantage because of its higher valence. The relative screening between two cations in the pore is not just a function of the valence, however. The relative size of the ions is also important. This can be seen from the analytic formulas of the mean spherical approximation for homogeneous electrolytes (14,30,34). Because of this, the screening advantage for Ca²⁺ is approximately 0.5 kT smaller when competing against Li⁺ and than when competing against Cs⁺.
- (4) Excluded-volume advantage (solid column). This term favors the smaller ion. Since Li⁺ is the only monovalent considered that is smaller than Ca²⁺, it is the only one with an excluded-volume advantage (albeit a very small one at approximately 0.25 kT). Ca²⁺, however, has a relatively large excluded-volume advantage over Cs⁺ of approximately 1 kT.

Combining these results, it is the number and mean electrostatic terms that remain constant as monovalent size is changed; previously, when $[Ca^{2+}]$ was changed, these terms changed substantially. Visa versa, the screening and excluded-volume terms that remained approximately constant as $[Ca^{2+}]$ varied now change as monovalent size is varied. These two terms combined only change about 1.75 kT, but this is enough to change the relative concentrations of Ca^{2+} and monovalent in the selectivity filter from approximately 1:1 for Ca^{2+} vs. Li^+ to more than 7:1 Ca^{2+} vs. Cs^+ (Fig. 8). The excluded-volume term is the one that changes the most. Therefore, is the most significant factor in determining the amount of Ca^{2+} vs. monovalent selectivity, even though it is generally less than 1 kT in magnitude.

Effects of mutations on Ca2+ vs. K+ selectivity

The model of RyR permeation and selectivity described here correctly reproduces and predicts the Ca²⁺ vs. monovalent cation selectivity. Without adjusting any parameters the model also reproduces the experimentally-measured decrease in conductance and selectivity when specific charged amino acids are mutated to neutral analogs. These include the mutations D4899N, E4900Q, and D4938N (see Appendix). In the model, these mutations are produced by changing the charge on these amino acids to zero; no other parameters (e.g., diffusion coefficients, pore radius) are changed.

Here, two of these mutations are considered in detail: D4899N and D4938N. Each results in a significant reduction of Ca^{2+} vs. K^+ selectivity; D4899N reduces the permeability ratio P_{Ca}/P_K from a native (WT) value of 7.0 to 3.4 and D4839N reduces it to 3.3 (41,52). This loss of selectivity is reflected in the cation profiles shown in Figs. 10 and 11. In both cases, there is a significant reduction in both Ca^{2+} and K^+ in the region where the mutation occurred (indicated by the vertical lines) and a neighboring region. In other parts of the pore, the profiles are virtually identical to the native profiles. The changes are very localized, but the resulting large changes in the current/voltage curves (see Appendix) show that these localized changes in the cation profiles have significant and important measurable effects.

To understand the differences in binding selectivity in these mutations compared to native RyR, the same chemical potential decomposition of Eq. (6) can be used. In this case,

however, it is more instructive to consider the entire profile through the pore rather than just a single location. Figs. 12 and 13 show the energetics for D4899N and D4938N (dashed lines), respectively, compared to native RyR (solid lines). In both cases, there is a significant (approximately 3 kT) loss of Ca²⁺ binding compared to K⁺ in the mutated region (panel A). In the regions neighboring the mutation site—up to 7.5 Å away—there is also significant loss of Ca²⁺ binding; each mutation has far-reaching effects. Analyzing the chemical potential components again gives insight into why this occurs:

- (1) Excluded-volume advantage (panel B). This term does not change significantly in the mutant RyRs.
- (2) Mean electrostatic advantage (panel C). Zeroing the charge in a region of the pore is expected to change the mean electrostatic potential in that region, and it does. But, in the two mutations the results are different. In D4899N (Fig. 12C), the region where the mean electrostatic potential differs from native profile by more than 1 kT is small compared to D4938N (Fig. 13C). For that mutant, the entire mutation site as well a neighboring region has a mean electrostatic potential difference (compared to native) of approximately 1.5 kT. In both mutations, the change in this potential is localized to the mutation site and approximately 2.5 Å on either side; in the rest of the pore the potential is the same as in native RyR.
- (3) Screening advantage (panel D). The largest change is a reduction in the screening advantage of Ca^{2+} in and around the mutation site. This change—up to 2 kT—extends up to 7.5 Å away from the mutation sites.

Altogether, the charge-deletion mutations result in an environment with significantly smaller mean electrostatic and screening advantages of Ca²⁺ over K⁺; Ca²⁺ retains some advantage, but in each case up to 2 kT less then in native RyR. Because electrostatic correlations range over the local screening (Debye) length (22,33), changes in the mutation site produce changes in the ionic concentration a distance away. Both Ca²⁺ and K⁺ concentrations are reduced and because of the loss of up to 4 kT between these two advantages, the K⁺ concentration is now significantly higher than that of Ca²⁺ (Figs. 12A and 13A).

Discussion

In equilibrium, the energetics of Ca²⁺ vs. monovalent cation binding selectivity in the pore RyR can be decomposed into the four terms in Eq. (6): (1) the number advantage that describes which ion species has a larger concentration in the baths; (2) the mean electrostatic advantage that describes the average electrostatic well/barrier in the channel due to the average local net charge (through the Poisson equation); (3) the screening advantage that describes the ability of an ion to electrostatically coordinate with other ions within a screening (Debye) length; (4) the excluded-volume advantage that, in this paper, describes the energy needed to insert an uncharged hard sphere the size of an ion into a location. In this model of RyR, there is no explicit ion dehydration energy because water is an uncharged, hard sphere in a continuum dielectric; all the experimental data—including the high conductance of Mg²⁺ through RyR—is reproduced with this simple model of water. This prediction of the model that the ion dehydration step is small must be tested and will be explored in future work.

Each of the four chemical potential terms plays an important role in Ca²⁺ vs. monovalent cation selectivity, as detailed now.

Number advantage

In calcium-selective channels, the number advantage that monovalents generally have over divalents is the challenge that selectivity must overcome; all other energies must overcome the number advantage. For example, under physiological conditions in the sarcoplasmic reticulum, $[Ca^{2+}]$ is approximately 1 mM while $[K^+]$ is approximately 150 mM—a number advantage equivalent to 5 kT of chemical potential in favor of K^+ . Also, in experiments (e.g., on the L-type calcium channel or in Fig. 2) $[Ca^{2+}]$ can be 1 μ M (or less)—a number advantage of 12 kT (or more) in favor of the monovalent.

In RyR, when the number advantage for K^+ is removed by increasing $[Ca^{2+}]$, the mean electrostatic potential throughout the pore goes to zero as more Ca^{2+} enters (Fig. 4) and K^+ is displaced (Fig. 3A). Recent work using grand canonical Monte Carlo simulations has shown that this displacement of K^+ is a nonlinear function of the environment in the pore and how important it is to do all calculations at the experimental $[Ca^{2+}]$ (11,12,53). Currently, all MD and BD simulation require at least 10 mM Ca^{2+} in the bath. While simulation results from 18 mM Ca^{2+} have been extrapolated down to 1 μ M Ca^{2+} by Corry et al. (15), a theory is required to do this. Without further simulations, however, it is impossible to verify the theory or its assumptions. Rather, a theory like PNP/DFT that spans *all* concentration ranges can be applied. Since PNP/DFT directly computes the average thermodynamic quantities and does not simulate particle trajectories, bath concentrations are just input parameters for the theory.

Electrostatics

In general, the largest contributions to RyR being a calcium channel come from the two electrostatic terms that always favor Ca²⁺ binding in the pore over monovalent cations. Also, it is only these terms that change substantially in mutations. These two terms, while both electrostatic in nature, are physically distinct: the mean electrostatic advantage reflects the long-time, many-particle *average* electrostatic potential in the pore produced by the *average* ion concentrations in the Poisson equation (Eq. (3)); on the other hand, the screening advantage reflects the ability to form long-time ion correlations (i.e., ion coordination or screening) produced by the ions' sizes and the *instantaneous* local electrostatic environment (on the atomic motion timescale) that is not included in the long-time mean electrostatic potential (22,33,34).

In total, the electrostatics of the system *are* the major driving force for Ca²⁺ vs. monovalent selectivity, in general agreement with Corry et al. (15,16). However, since the DFT approach naturally decomposes the electrostatics into these two physically different terms, the PNP/DFT approach can give a more thorough understanding of how the electrostatics contributes to selectivity. With 150 mM K⁺ in the bath, the screening advantage of Ca²⁺ is always more than the mean electrostatic advantage if [Ca²⁺] is more than 0.1 mM (Fig. 7). Moreover, the mean electrostatic advantage disappears as [Ca²⁺] is increased while the screening advantage remains largely unchanged (Fig. 7). Therefore, it is the screening advantage of Ca²⁺ that is the dominant electrostatic term.

Ionic screening is a reflection of an ion's ability to coordinate with neighboring ions and thereby lower the system's energy. This coordination is a function of both the ion's charge and size (as well as the other ions' charges and sizes) and is a balance of electrostatic and excluded-volume forces (14,30,33); it is even possible for a small monovalent ion can screen better than a large divalent (54,55). An ion species' screening advantage then directly reflects the CSC mechanism of selectivity; the excluded-volume term reflects another component. This is especially true for Ca²⁺ because its screening advantage over monovalent cations is large (~4

kT), indicating that Ca^{2+} coordinates significantly better, especially in the crowded environment of the selectivity filter (Fig. 7). In other words, the large screening advantage of Ca^{2+} shows that Ca^{2+} can more efficiently balance the negative charges of the protein (e.g., Asp-4899 in the selectivity filter) than the monovalents.

Excluded volume

While the electrostatic terms are generally the largest, the excluded-volume (hard-sphere) term is generally the smallest—but still important in selectivity. If electrostatics were purely responsible for Ca^{2+} vs. monovalent selectivity, then there would be little difference in the concentration of Ca^{2+} and different monovalent cations in the selectivity filter. The calculations, however, show a large difference (Fig. 8); there is significantly less Ca^{2+} in the pore with the small Li^{+} (1.33 Å diameter) as the monovalent than with the large Cs^{+} (3.40 Å diameter). The chemical potential decomposition done in the DFT (Fig. 9) demonstrates that this difference is due to changes in both the screening (up to \sim 0.5 kT) and excluded-volume terms (up to \sim 1 kT). The larger the monovalent, the more both terms favor Ca^{2+} binding.

This trend reflects the CSC selectivity mechanism: it is the small ions (e.g., Li⁺ and Ca²⁺) that can more efficiently balance the protein charges than the large ions (e.g., Cs⁺) because they occupy less space in the crowded selectivity filter. Fig. 8 shows this in terms of ion concentrations in the pore. If Cs⁺ is replaced by Li⁺ as the monovalent, then Ca²⁺ concentration in the selectivity filter decreases approximately 30% while monovalent concentration increases approximately 500% (compare dotted and solid lines in Fig. 8). The small Li⁺ takes up only 6% the volume of the large Cs⁺ and therefore fits more easily into the selectivity filter. Ca²⁺ is displaced because more monovalents are in the filter to balance the negative Asp-4899 protein charges. The exact ratio of Ca²⁺ to monovalent concentration in the pore is a balance of the electrostatic and excluded-volume forces—charge/space competition.

It is important to note that, while changes in the excluded-volume advantage are relatively small at around 1 kT or less, the ion concentrations in the pore depend on all the terms *exponentially* (Eq. (4)); small changes in any term can have a large effect. It is because of this that any model must reproduce experimental data over a wide range of conditions. Only then can one have confidence that the energies in the model change correctly as conditions are changed. For this reason, all the data reproduced by the model—more than 100 different ionic solutions—are shown in this paper (main text and Appendix). Specifically, Figs. 2 and 22 show that the PNP/DFT model correctly reproduces RyR's Ca²⁺ vs. monovalent affinity as [Ca²⁺] is changed.

Flexible coordination in the selectivity filter

The balance of electrostatics and excluded volume in the selectivity filter that is the CSC mechanism of selectivity is consistent with a more general idea of selectivity that is emerging from the study other ion channels. In the potassium channel, Noskov and Roux (56) and Varma and Rempe (57) describe how the carbonyl oxygens in that selectivity filter form an environment that best coordinates K⁺. In the sodium channel, Boda et al. (53) show how the amino acids of the DEKA locus arrange around the permeant ions, with Na⁺ being coordinated best compared to K⁺ and Ca²⁺. In those channels and in the calcium channels studied previously with Monte Carlo simulations (8-12,58), the channel protein forms a flexible environment that coordinates the "correct" ion better than the other ions, leading to binding selectivity.

The situation is the same for RyR with the carboxyl groups of the DDDD locus (from Asp-4899) coordinating Ca²⁺ best among the permeant ions. This is quantified by the screening and excluded-volume advantages of Ca²⁺. Both of these terms indicate how well an ion "fits into" the crowded environment of the selectivity filter, either by its ability to coordinate with (screen) neighboring ions and protein charges—the screening advantage—or by its ability to find space among the other atoms—the excluded-volume advantage.

Conclusion

A PNP/DFT model was used to analyze the energetics of equilibrium binding selectivity in RyR. The extension of a previous model (20) presented here uses 9 data points to determine model parameters that were then never changed. The model reproduces both native and mutant RyR permeation and selectivity data in over 100 different ionic solutions and predicted the presence of different sized AMFEs when Ca²⁺ was added to Na⁺ and when Ca²⁺ was added to Cs⁺. It had previously predicted an AMFE for mixtures of Na⁺ and Cs⁺ (20). While there are approximations in the model that need to be explored further (e.g., no dehydration penalty for ions moving from the bath into the pore), the PNP/DFT approach has advantages over other methods including fast computing time (minutes for an entire current/voltage curve) and arbitrarily small bath concentrations.

The model shows that Ca²⁺ vs. monovalent cation selectivity in RyR is determined by the CSC mechanism that balances the electrostatic attraction of the negative protein charges (especially Asp-4899) with the excluded volume of the ions and protein charges in the selectivity filter. This balance in favor of Ca²⁺ is achieved by having a selectivity filter that contains negatively-charged carboxyl groups on tethers so they are free to move in response to the permeant ions currently in the filter and by thermal motion. In this sense the CSC mechanism is consistent with the selectivity by the flexible coordination provided by the channel protein seen in other channels (53,56,57). The PNP/DFT approach allows one to quantify the chemical potentials involved through the large screening advantage of Ca²⁺ over monovalent cations—a measure of the coordination of Ca²⁺ with the other charges in the selectivity filter—and in the excluded-volume advantage of Ca²⁺ over larger monovalent cations—a measure of much better the smaller ion fits into the crowded selectivity filter.

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Appendix: Constructing the model

The model of ion permeation through the open RyR channel is a refinement of the model described in Ref. (20) that includes new mutation data (41) that was not available when the first model was created. Specifically, two charge-neutralizing mutations of aspartates in the cytosolic (*cis*) vestibule of the pore (D4938N and D4945N) were shown to affect RyR conductance and selectivity: the conductances in 250 mM symmetric KCl were 65% and 92% of WT for D4938N and D4945N, respectively, and permeability ratios P_{Ca}/P_K were reduced from 7.0 to 3.3 and 6.5. Charge-neutralizing mutations (D or E to N or Q) of other charged amino acids in the cytosolic vestibule did not affect either K⁺ conductance or Ca²⁺ vs. K⁺ selectivity (41).

Previous experiments (7) showed that neutralizing the charge on two negatively-charged amino acids (Asp-4899 and Glu-4900) significantly reduced both conductance and selectivity: the conductances in 250 mM symmetric KCl were 20% and 56% of WT for D4899N and E4900Q, respectively, and permeability ratios $P_{\text{Ca}}/P_{\text{K}}$ were reduced from 7.0 to 3.4 and 3.2. Except for the mutation E4902Q, charge-neutralizing mutations of other charged amino acids in the lumenal vestibule did not affect either K⁺ conductance or Ca²⁺ vs. K⁺ selectivity. While the conductance of E4902Q was found to be similar to WT, a small but statistically significant change from WT in Ca²⁺ selectivity was found (7) so E4902 was also included in this model.

Only Asp-4899 and Glu-4900 were explicitly included in the first model of RyR (20), although a region of negative charge in the cytosolic vestibule was required to reproduce the data. In hindsight, these were the then-unknown Asp-4938 and Asp-4945. In the model described here, all of the charged amino acids found in mutation experiments to affect RyR conductance and selectivity (while still producing functional and caffeine- and ryanodine-sensitive channels) were included: Asp-4899 in the selectivity filter, Asp-4938 and Asp-4945 in the cytosolic vestibule, and Glu-4900 and Glu-4902 in the lumenal vestibule (Fig. 1).

Since no high-resolution structures of the RyR are available, it was necessary to reverse-engineer the location of these amino acids. Several low-resolution electron microscopy structures of the entire RyR protein in the closed state that were published after the initial model were used to guide the making of the model pore (59,60). Construction of the model pore was done in a way similar that described in Ref. (20), but the basic method is outlined here. Because of the homology between RyR and the potassium channel (60), the pore was given a narrow selectivity filter with a wider cytosolic vestibule. The selectivity filter radius was chosen to be the same as in the previous model (4 Å) and 15 Å in length. Homology models derived from low-resolution structures of the RyR pore indicate that the selectivity filter includes residues 4894 to 4899 (GGGIGD) (59). The model selectivity filter is long enough to include these amino acids, but only Asp-4899 is explicitly modeled (Fig. 1). The cytosolic vestibule radius was chosen to be 7 Å in accordance with low-resolution RyR structures (M. Samsó, Harvard Medical School, personal communication, 2007), although the model cannot distinguish between different vestibule radii as it can between different selectivity filter radii (Fig. 15 of Ref. (20)).

As in the previous model, Glu-4900 was placed at the selectivity filter/lumenal vestibule junction. Glu-4902 was placed on the lumenal face of the channel. These are in accordance with other modeling of the RyR pore based on KcsA homology and mutation experiments (Fig. 2 of Ref. (7)). Asp-4938 was placed in the cytosolic vestibule in accordance with homology modeling from low-resolution RyR structures and 15 Å away from Asp-4899 (59). Asp-4945 was placed 10 Å away from Asp-4938 toward the cytosolic end of the pore (59,60) because, as part of the same α -helix, they are approximately two helix turns apart. Because the structure of

the RyR pore in the open state has not yet been determined at a resolution sufficient to distinguish the conformation of the inner helices, the increase in pore radius near Asp-4945 was arbitrarily chosen to be 45°. The model is not sensitive enough to distinguish between different helix tilt angles.

Each of the aspartates and glutamates were assumed to be fully-charged and facing into the permeation pathway with the terminal carboxyl (COO $^-$) group on a flexible tether than can span a hemisphere of radius 5 Å for aspartates and 7 Å for glutamates (Fig. 1). In the one-dimensional Poisson-Nernst-Planck/Density Functional Theory (PNP/DFT) model (13,20), residues Asp-4938, Asp-4899, and Glu-4900 were modeled as two, independent, half-charged oxygen ions (2.8 Å diameter) confined to a region of the long axis of the pore spanned by each residue's hemisphere (8,11,12,14,20). For example, the centers of the oxygens for Asp-4899 were confined to 15 Å < x < 25 Å in Fig. 1. The other residues in the model (Asp-4945 and Glu-4900) were modeled as regions of uniform fixed charge (i.e., just a background charge and not as ions that take up space) because the pore radius where they were located was too wide for the residues to exert excluded-volume effects on the permeating ions; their presence was only felt electrostatically by the permeating ions.

Many important structural inferences were made from the first model (20) that have not changed in this model (e.g., selectivity filter radius of 4 Å and the location of Glu-4900 at the selectivity filter/lumenal vestibule interface and that its range of tethered movement overlapped with that of Asp-4899). Other structural parameters were constrained by known structural information (e.g., distance of Asp-4938 from Asp-4899 or distance of Asp-4945 from Asp-4938) or were chosen to have a reasonable value (e.g., range of tethered movement of side chains, location of Glu-4902, or pore radius in the cytosolic vestibule). The results were insensitive to the exact choice of these latter values. Given the constraints of the previous model and known structural information and the insensitivity of the other parameters, there were no adjustable parameters with respect to the structure in this model.

There were, however, some parameters for the ions that had to be determined from the experimental data: the diffusion coefficients of the permeating ions and water are inputs to the PNP/DFT model. Because water does not contribute to the current and Cl does not permeate the channel, these were given diffusion coefficients of 1% of bulk within the pore. Previously it was shown that the results of the model did not change even when bulk diffusion coefficients were used (20). For the cations, three different diffusion coefficients were used within the pore, one in each of the following regions: in the cytosolic vestibule where Asp-4938 was confined (0 Å < x < 10 Å), in the selectivity filter (10 Å < x < 25 Å), and in the lumenal vestibule (25 Å < x < 32 Å). In all other regions, bulk (infinite dilution) diffusion coefficients were used. The resulting piecewise constant profile was smoothed as described (20).

For K⁺ the three diffusion coefficients were determined by reproducing the experimental current in symmetric 250 mM KCl in native RyR (80 pA at +100 mV) and in the mutants E4900Q (10 pA at +20 mV) and D4839N (52 pA at +100 mV). The diffusion K⁺ coefficients (from cytosolic to lumenal) were 122.1×10^{-11} , 6.91×10^{-11} , and 40.3×10^{-11} and m²/s. For all non-K⁺ cations (Li⁺, Na⁺, Rb⁺, Cs⁺, Mg²⁺, and Ca²⁺) only one diffusion coefficient was left undetermined by assuming that the ratio of bulk to cytosolic vestibule diffusion coefficients for K⁺ was the same for all other cations and by assuming that the ratio of selectivity filter to lumenal vestibule diffusion coefficients for K⁺ was the same for all other cations. The one open diffusion coefficient in the selectivity filter was determined for the monovalent cations by reproducing the current at +100 mV in 250 mM symmetric conditions: Li⁺ (21.2 pA), Na⁺ (48.1

pA), Rb⁺ (71.5 pA), and Cs⁺ (51.9 pA). For the divalent cations, selectivity filter diffusion coefficient was determined by reproducing the current at -100 mV in 250 mM symmetric KCl and 10 mM lumenal divalent-chloride: Mg²⁺ (-31 pA) and Ca²⁺ (-33 pA). The selectivity filter diffusion coefficients were found to be: 1.29×10^{-11} for Li⁺, 3.65×10^{-11} for Na⁺, 6.91×10^{-11} for K⁺, 5.92×10^{-11} for Rb⁺, 4.18×10^{-11} for Cs⁺, 0.42×10^{-11} for Mg²⁺, and 0.41×10^{-11} m²/s for Ca²⁺.

While no molecular dynamics simulations to determine diffusion coefficients inside a highly-charged calcium channel have been performed, these values for the selectivity filter diffusion coefficients are consistent with those used in other models of RyR (17-19) and consistent with diffusion coefficients used in models of other highly-charged ion channels (13,23,25,61,62) and of other channels (63-67). These values are also consistent with the fact that diffusion coefficients are reduced below bulk values by a combination of both geometric confinement (68,69) and—to an even larger extent—by a highly-charged environment (70-72) like that found in the selectivity filter of RyR or other calcium channels.

After determining the three diffusion coefficients for K⁺ and one diffusion coefficient for Li⁺, Na⁺, Rb⁺, Cs⁺, Mg²⁺, and Ca²⁺ using exactly 9 experimental data points out of more than a thousand, the model reproduces all the permeation and selectivity data of RyR2 (the cardiac isoform of RyR) in over 100 different ionic solutions—some yet to be published—without readjusting any parameters. The comparison of the revised model and experimental data for two mole fraction curves and 55 current/voltage curves in pure monovalent-chloride, biionic, and monovalent/divalent mixtures in native and mutant RyR of Ref. (20) are shown here and in the main text. Comparisons of model results and previously unpublished experiment data will be published later.

The additional structural and mutation data have substantially improved the results of the model. The new model also reproduces the conductances of mutations not in the previous model without any adjustable parameters; in 250 mM symmetric KCl, the model conductance is 718 pS for D4945N (experimental 737±11 pS (41)) and 792 pS for E4902Q (experimental 782±4 pS (7)).

Details of the modeling not described here are discussed in Ref. (20).

Figs. 14-22 show the results of the model compared to experiments in 66 ionic solutions in both native and three mutants (D4899N, E4900Q, and D4938N). These experimental data have been published previously (7,20,41). Comparisons of the model to as-yet unpublished experimental data will be shown in future work.

References

- 1. Hess, P., J. B. Lansman, and R. W. Tsien. 1986. Calcium channel selectivity for divalent and monovalent cations. Voltage and concentration dependence of single channel current in ventricular heart cells. J. Gen. Physiol. 88:293-319.
- 2. Almers, W., E. W. McCleskey, and P. T. Palade. 1984. A non-selective cation conductance in frog muscle membrane blocked by micromolar external calcium ions. J. Physiol. (London) 353:565-583.
- 3. Almers, W. and E. W. McCleskey. 1984. Non-selective conductance in calcium channels of frog muscle: calcium selectivity in a single-file pore. J. Physiol. (London) 353:585-608.
- 4. Smith, J. S., R. Coronado, and G. Meissner. 1985. Sarcoplasmic reticulum contains adenine nucleotide-activated calcium channels. Nature 316:446-449.
- 5. Heinemann, S. H., H. Terlau, W. Stuhmer, K. Imoto, and S. Numa. 1992. Calcium channel characteristics conferred on the sodium channel by single mutations. Nature 356:441-443.
- 6. Yang, J., P. T. Ellinor, W. A. Sather, J.-F. Zhang, and R. Tsien. 1993. Molecular determinants of Ca²⁺ selectivity and ion permeation in L-type Ca²⁺ channels. Nature 366:158-161.
- 7. Wang, Y., L. Xu, D. A. Pasek, D. Gillespie, and G. Meissner. 2005. Probing the Role of Negatively Charged Amino Acid Residues in Ion Permeation of Skeletal Muscle Ryanodine Receptor. Biophys. J. 89:256-265.
- 8. Boda, D., D. D. Busath, D. J. Henderson, and S. Sokolowski. 2000. Monte Carlo Simulations of the Mechanism of Channel Selectivity: The competition between Volume Exclusion and Charge Neutrality. J. Phys. Chem. B *104*:8903-8910.
- 9. Boda, D., D. Henderson, and D. D. Busath. 2001. Monte Carlo Study of the Effect of Ion and Channel Size on the Selectivity of a Model Calcium Channel. J. Phys. Chem. B 105:11574-11577.
- 10. Boda, D., D. Henderson, and D. D. Busath. 2002. Monte Carlo study of the selectivity of calcium channels: Improved geometry. Mol. Phys. 100:2361-2368.
- 11. Boda, D., M. Valiskó, B. Eisenberg, W. Nonner, D. J. Henderson, and D. Gillespie. 2006. The effect of protein dielectric coefficient on the ionic selectivity of a calcium channel. J. Chem. Phys. 125:034901.
- 12. Boda, D., M. Valiskó, B. Eisenberg, W. Nonner, D. J. Henderson, and D. Gillespie. 2007. Combined effect of pore radius and protein dielectric coefficient on the selectivity of a calcium channel. Phys. Rev. Lett. 98:168102.

- 13. Nonner, W. and B. Eisenberg. 1998. Ion Permeation and Glutamate Residues Linked by Poisson-Nernst-Planck Theory in L-Type Calcium Channels. Biophys. J. 75:1287-1305.
- 14. Nonner, W., L. Catacuzzeno, and B. Eisenberg. 2000. Binding and Selectivity in L-Type Calcium Channels: A Mean Spherical Approximation. Biophys. J. 79:1976-1992.
- 15. Corry, B., T. W. Allen, S. Kuyucak, and S.-H. Chung. 2001. Mechanisms of Permeation and Selectivity in Calcium Channels. Biophys. J. 80:195-214.
- 16. Corry, B., T. Vora, and S.-H. Chung. 2005. Electrostatic basis of valence selectivity in cationic channels. Biochimica et Biophysica Acta (BBA) Biomembranes 1711:72-86.
- 17. Chen, D., L. Xu, A. Tripathy, G. Meissner, and B. Eisenberg. 1997. Permeation through the calcium release channel of cardiac muscle. Biophys. J. 73:1337-1354.
- 18. Chen, D. P., L. Xu, A. Tripathy, G. Meissner, and B. Eisenberg. 1999. Selectivity and Permeation in Calcium Release Channel of Cardiac Muscle: Alkali Metal Ions. Biophys. J. 76:1346-1366.
- 19. Chen, D., L. Xu, B. Eisenberg, and G. Meissner. 2003. Calcium ion permeation through the calcium release channel (ryanodine receptor) of cardiac muscle. J. Phys. Chem. B 107:9139-9145.
- 20. Gillespie, D., L. Xu, Y. Wang, and G. Meissner. 2005. (De)constructing the ryanodine receptor: Modeling ion permeation and selectivity of the calcium release channel. J. Phys. Chem. B 109:15598-15610.
- 21. Nonner, W., D. Gillespie, D. J. Henderson, and B. Eisenberg. 2001. Ion accumulation in a biological calcium channel: effects of solvent and confining pressure. J. Phys. Chem. B 105:6427-6436.
- 22. Gillespie, D., W. Nonner, and R. S. Eisenberg. 2002. Coupling Poisson-Nernst-Planck and Density Functional Theory to Calculate Ion Flux. J. Phys.: Condens. Matter 14:12129-12145.
- 23. Miedema, H., A. Meter-Arkema, J. Wierenga, J. Tang, B. Eisenberg, W. Nonner, H. Hektor, D. Gillespie, and W. Meijberg. 2004. Permeation Properties of an Engineered Bacterial OmpF Porin Containing the EEEE-Locus of Ca²⁺ Channels. Biophys. J. 87:3137-3147.
- Vrouenraets, M., J. Wierenga, W. Meijberg, and H. Miedema. 2006. Chemical Modification of the Bacterial Porin OmpF: Gain of Selectivity by Volume Reduction. Biophys. J. 90:1202-1211.
- 25. Miedema, H., M. Vrouenraets, J. Wierenga, D. Gillespie, B. Eisenberg, W. Meijberg, and W. Nonner. 2006. Ca²⁺ Selectivity of a Chemically Modified OmpF with Reduced Pore Volume. Biophys. J. 91:4392-4400.

- 26. Marconi, U. M. B. and P. Tarazona. 1999. Dynamic density functional theory of fluids. J. Chem. Phys. 110:8032-8044.
- 27. Penna, F. and P. Tarazona. 2003. Dynamic density functional theory for steady currents: Application to colloidal particles in narrow channels. J. Chem. Phys. 119:1766-1776.
- 28. Archer, A. 2006. Dynamical density functional theory for dense atomic liquids. J. Phys.: Condens. Matter 18:5617–5628.
- 29. Schuss, Z., B. Nadler, and B. Eisenberg. 2001. Derivation of Poisson and Nernst-Planck equations in a bath and channel from a molecular model. Phys. Rev. E 64:036116.
- 30. Waisman, E. and J. L. Lebowitz. 1970. Exact solution of an integral equation for the structure of a primitive model of an electrolyte. J. Chem. Phys. 52:4307-4309.
- 31. Wu, J. 2006. Density functional theory for chemical engineering: From capillarity to soft materials. AIChE J. 52:1169-1193.
- 32. Rosenfeld, Y. 1993. Free enery model for inhomogeneous fluid mixtures: Yukawa-charged hard spheres, general interactions, and plasmas. J. Chem. Phys. 98:8126-8148.
- 33. Gillespie, D., W. Nonner, and R. S. Eisenberg. 2003. Density functional theory of charged, hard-sphere fluids. Phys. Rev. E 68:031503.
- 34. Barthel, J. M. G., H. Krienke, and W. Kunz. 1998. Physical Chemistry of Electrolyte Solutions: Modern Aspects. New York: Springer.
- 35. Evans, R. 1992. Density functionals in the theory of nonuniform fluids. In Fundamentals of Inhomogeneous Fluids. D. J. Henderson, editor. Marcel Dekker. New York. 85-176.
- 36. Berry, S. R., S. A. Rice, and J. Ross. 2000. Physical Chemistry. New York: Oxford. 1064 p.
- 37. Li, Z. and J. Wu. 2004. Density-functional theory for the structures and thermodynamic properties of highly asymmetric electrolyte and neutral component mixtures. Phys. Rev. E 70:031109.
- 38. Gillespie, D., M. Valiskó, and D. Boda. 2005. Density functional theory of the electrical double layer: the RFD functional. J. Phys.: Condens. Matter 17:6609-6626.
- 39. Gillespie, D. 1999. A singular perturbation analysis of the Poisson-Nernst-Planck system: Applications to ionic channels. Chicago, Illinois: Rush University.

- 40. Kettlun, C., A. Gonzalez, E. Ríos, and M. Fill. 2003. Unitary Ca²⁺ Current through Mammalian Cardiac and Amphibian Skeletal Muscle Ryanodine Receptor Channels under Near-physiological Ionic Conditions. J. Gen. Physiol. 122:407-417.
- 41. Xu, L., Y. Wang, D. Gillespie, and G. Meissner. 2006. Two rings of negative charges in the cytosolic vestibule of type-1 ryanodine receptor modulate ion fluxes. Biophys. J. 90:443-453.
- 42. Lindsay, A. R., S. D. Manning, and A. J. Williams. 1991. Monovalent cation conductance in the ryanodine receptor-channel of sheep cardiac muscle sarcoplasmic reticulum. J. Physiol. (London) 439:463-480.
- 43. Tinker, A. and A. J. Williams. 1992. Divalent cation conduction in the ryanodine receptor channel of sheep cardiac muscle sarcoplasmic reticulum. J. Gen. Physiol. 100:479-493.
- 44. Xu, L. and G. Meissner. 1998. Regulation of Cardiac Muscle Ca²⁺ Release Channel by Sarcoplasmic Reticulum Lumenal Ca²⁺. Biophys. J. 75:2302-2312.
- 45. Hille, B. 2001. Ion Channels of Excitable Membranes. Sunderland: Sinauer Associates Inc. 814. p.
- 46. Lundstrom, M. 2000. Fundamentals of Carrier Transport. New York: Cambridge University Press.
- 47. Chen, D. P., R. S. Eisenberg, J. W. Jerome, and C. W. Shu. 1995. Hydrodynamic model of temperature change in open ionic channels. Biophys. J. 69:2304-2322.
- 48. Hänggi, P., P. Talkner, and M. Borokovec. 1990. Reaction-rate theory: Fifty years after Kramers. Rev. Mod. Phys. 62:251-341.
- 49. Eisenberg, R. S., M. M. Kłosek, and Z. Schuss. 1995. Diffusion as a chemical reaction: Stochastic trajectories between fixed concentrations. J. Chem. Phys. 102:1767-1780.
- 50. Nonner, W., D. P. Chen, and B. Eisenberg. 1999. Progress and Prospects in Permeation. J. Gen. Physiol. 113:773-782.
- 51. Shannon, R. D. and C. T. Prewitt. 1969. Effective ionic radii in oxides and fluorides. Acta Crystallogr. B25:925-946.
- 52. Gao, L., D. Balshaw, L. Xu, A. Tripathy, C. Xin, and G. Meissner. 2000. Evidence for a Role of the Lumenal M3-M4 Loop in Skeletal Muscle Ca²⁺ Release Channel (Ryanodine Receptor) Activity and Conductance. Biophys. J. 79:828-840.
- 53. Boda, D., W. Nonner, M. Valisko, D. Henderson, B. Eisenberg, and D. Gillespie. 2007. Steric Selectivity in Na Channels Arising from Protein Polarization and Mobile Side Chains. Biophys. J.:biophysj.107.105478.

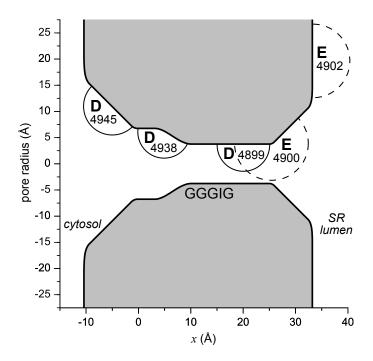
- 54. Woelki, S. and H.-H. Kohler. 2000. A modified Poisson-Boltzmann equation, II. Models and solutions. Chem. Phys. 261:421-438.
- 55. Valiskó, M., D. Boda, and D. Gillespie. 2007. Selective adsorption of ions with different diameter and valence at highly-charged interfaces. J. Phys. Chem. B:submitted.
- 56. Noskov, S. Y. and B. Roux. 2007. Importance of Hydration and Dynamics on the Selectivity of the KcsA and NaK Channels. J. Gen. Physiol. 129:135-143.
- 57. Varma, S. and S. Rempe. 2007. Tuning ion coordination architectures to enable selective partitioning. Biophys. J.:biophysj.107.107482.
- 58. Boda, D., D. Busath, B. Eisenberg, D. J. Henderson, and W. Nonner. 2002. Monte Carlo simulations of ion selectivity in a biological Na⁺ channel: charge-space competition. Phys. Chem. Chem. Phys. 4:5154-5160.
- 59. Ludtke, S. J., I. I. Serysheva, S. L. Hamilton, and W. Chiu. 2005. The Pore Structure of the Closed RyR1 Channel. Structure 13:1203-1211.
- 60. Samsó, M., T. Wagenknecht, and P. D. Allen. 2005. Internal structure and visualization of transmembrane domains of the RyR1 calcium release channel by cryo-EM. Nature Structural & Molecular Biology 12:539-544.
- 61. Chen, D., J. Lear, and B. Eisenberg. 1997. Permeation through an open channel: Poisson-Nernst-Planck theory of a synthetic ionic channel. Biophys. J. 72:97-116.
- 62. Rodriguez-Contreras, A., W. Nonner, and E. N. Yamoah. 2002. Ca²⁺ transport properties and determinants of anomalous mole fraction effects of single voltage-gated Ca²⁺ channels in hair cells from bullfrog saccule. J Physiol 538:729-745.
- 63. Hollerbach, U., D. P. Chen, D. D. Busath, and B. Eisenberg. 2000. Predicting Function from Structure Using the Poisson-Nernst-Planck Equations: Sodium Current in the Gramicidin A Channel. Langmuir 16:5509-5514.
- 64. Cardenas, A. E., R. D. Coalson, and M. G. Kurnikova. 2000. Three-Dimensional Poisson-Nernst-Planck Theory Studies: Influence of Membrane Electrostatics on Gramicidin A Channel Conductance. Biophys. J. 79:80-93.
- 65. Furini, S., F. Zerbetto, and S. Cavalcanti. 2006. Application of the Poisson-Nernst-Planck Theory with Space-Dependent Diffusion Coefficients to KcsA. Biophys. J. 91:3162-3169.
- 66. Mamonov, A. B., M. G. Kurnikova, and R. D. Coalson. 2006. Diffusion constant of K+ inside Gramicidin A: A comparative study of four computational methods. Biophys. Chem. 124:268-278.

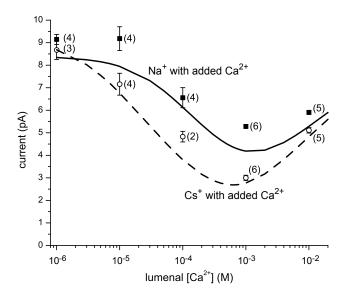
- 67. Bostick, D. and M. L. Berkowitz. 2003. The Implementation of Slab Geometry for Membrane-Channel Molecular Dynamics Simulations. Biophys. J. 85:97-107.
- 68. Tieleman, D. P. and H. J. C. Berendsen. 1998. A Molecular Dynamics Study of the Pores Formed by Escherichia coli OmpF Porin in a Fully Hydrated Palmitoyloleoylphosphatidylcholine Bilayer. Biophys. J. 74:2786-2801.
- 69. Smith, G. R. and M. S. P. Sansom. 1998. Dynamic Properties of Na⁺ Ions in Models of Ion Channels: A Molecular Dynamics Study. Biophys. J. 75:2767-2782.
- Laudernet, Y., T. Cartailler, P. Turq, and M. Ferrario. 2003. A microscopic description of concentrated potassium fluoride aqueous solutions by molecular dynamics simulation. J. Phys. Chem. B 107:2354-2361.
- 71. Allen, T. W., S. Kuyucak, and S.-H. Chung. 2000. Molecular dynamics estimates of ion diffusion in model hydrophobic and KcsA potassium channels. Biophys. Chem. 86:1-14.
- 72. Chowdhuri, S. and A. Chandra. 2001. Molecular dynamics simulations of aqueous NaCl and KCl solutions: Effects of ion concentration on the single-particle, pair, and collective dynamical properties of ions and water molecules. J. Chem. Phys. 115:3732-3741.

Figure Legends

- 1. The geometry of the model RyR pore. In the experiments and calculations, the lumen of the sarcoplasmic reticulum (SR) is electrically grounded. The circle around each labeled amino acid in meant to illustrate the range of the motion of the terminal carboxyl group. Aspartates (solid circles) are given a radius of 5 Å and glutamates (dashed circles) 7 Å. Only the amino acids of one of the four identical RyR subunits is shown. Asp-4945, Asp-4938, Asp-4899, Glu-4900, and Glu-4902 are the only amino acids explicitly modeled in the theory. The GGGIG sequence (4894-4898 in the numbering) at the cytosolic end of the selectivity filter is only a reference point for readers familiar with the RyR sequence.
- 2. Experimental verification of the AMFE predicted by the theory. The lines are the theory and the symbols are the experimental data with standard error bars and the number of experiments in parentheses. The solid line and symbols are the addition of Ca²⁺ to Na⁺ and the dashed line and open symbols are the addition of Ca²⁺ to Cs⁺. In all cases, the monovalent-chloride concentration was 150 mM in both cytosolic and lumenal baths and the indicated amount Ca²⁺ was added to the lumenal bath. The current at -20 mV is shown.
- 3. The partitioning coefficient of K^+ (panel A) and Ca^{2+} (panel B) plotted logarithmically. $[K^+] = 150$ mM and the indicated $[Ca^{2+}]$ is in both baths.
- 4. The electrostatic component of partitioning $z_i e \phi(x)/kT$ of K⁺ (panel A) and Ca²⁺ (panel B) in the pore. [K⁺] = 150 mM and the indicated [Ca²⁺] is in both baths.
- 5. The screening component of partitioning $\Delta \mu_i^{SC}(x)/kT$ of K⁺ (solid lines) and Ca²⁺ (dashed lines) in the pore. [K⁺] = 150 mM and [Ca²⁺] is changed from 1 μ M to 50 mM. Because the curves are so close together [Ca²⁺] is not indicated.
- 6. The excluded-volume (hard-sphere) component of partitioning $\Delta \mu_i^{HS}(x)/kT$ of K⁺ (solid lines) and Ca²⁺ (dashed lines) in the pore. [K⁺] = 150 mM and [Ca²⁺] is changed from 1 μ M to 50 mM. Because the curves are so close together [Ca²⁺] is not indicated.
- 7. Components of the binding selectivity from Eq. (6) in the selectivity filter (x = 20 Å in Fig. 1 that shows the geometry of the pore). $[K^+] = 150$ mM and the indicated $[Ca^{2+}]$ is in both baths. The horizontal-hatched bar is the number advantage, the diagonal-hatched bar is the mean electrostatic advantage, the cross-hatched bar is the screening advantage, and the solid bar is the excluded-volume advantage. The horizontal line is the binding selectivity of Eq. (6) (i.e., the sum of all the terms). A positive term favors the binding of Ca^{2+} while a negative term favors K^+ .
- 8. Concentration profiles in the pore of the monovalent cation (panel A) and Ca^{2+} (panel B). For each indicated monovalent cation X^+ , $[X^+] = 150$ mM and $[Ca^{2+}] = 1$ mM in both baths.
- 9. Components of the binding selectivity from Eq. (6) in the selectivity filter (x = 20 Å in Fig. 1 that shows the geometry of the pore). For each indicated monovalent cation X^+ , $[X^+] = 150$ mM and $[Ca^{2+}] = 1$ mM in both baths. Ion diameters: Li⁺ 1.33 Å; Na⁺ 2.00 Å; K⁺ 2.76 Å; Cs⁺ 3.42 Å. The horizontal-hatched bar is the number advantage, the diagonal-hatched bar is the mean electrostatic advantage,

- the cross-hatched bar is the screening advantage, and the solid bar is the excluded-volume advantage. The horizontal line is the binding selectivity of Eq. (6) (i.e., the sum of all the terms). A positive term favors the binding of Ca^{2+} while a negative term favors K^+ .
- Concentration profiles in the pore of K^+ (panel A) and Ca^{2+} (panel B) for the native (WT) channel (solid line) and the mutation D4899N (dashed line). $[K^+] = 150 \text{ mM}$ and $[Ca^{2+}] = 1 \text{ mM}$ in both baths. In the model, the mutation is created by "turning off" the charge on the four Asp-4899. The mutation site is the region from which the charge on the four Asp-4899 has been removed.
- 11. Concentration profiles in the pore of K^+ (panel A) and Ca^{2+} (panel B) for the native (WT) channel (solid line) and the mutation D4938N (dashed line). $[K^+] = 150 \text{ mM}$ and $[Ca^{2+}] = 1 \text{ mM}$ in both baths. In the model, the mutation is created by "turning off" the charge on the four Asp-4938. The mutation site is the region from which the charge on the four Asp-4938 has been removed.
- 12. Profiles of the binding selectivity from Eq. (6) (panel A) and its components (excluded volume, panel B; mean electrostatic, panel C; screening, panel D) for the native (WT) channel (solid line) and the mutation D4899N (dashed line). The conditions are those described in Fig. 9.
- 13. Profiles of the binding selectivity from Eq. (6) (panel A) and its components (excluded volume, panel B; mean electrostatic, panel C; screening, panel D) for the native (WT) channel (solid line) and the mutation D4938N (dashed line). The conditions are those described in Fig. 10.
- 14. Current/voltage curves in KCl (A-H). (I) The conductance at reversal potential with cytosolic [K⁺] is held at 250 mM and lumenal [K⁺] is varied. For both experiment and theory the current/voltage was fitted with a line and the slope is plotted. In this and the following figures, concentrations are listed as cytosolic | lumenal. The solid lines are the model and symbols are the experimental data.
- 15. Current/voltage curves of (A) the D4899N (■) and E4900Q (□) mutants and (B) the D4938N mutant in 250 mM symmetric KCl.
- 16. Current/voltage curves in LiCl. The dashed line is the model result for 250 mM cytosolic and 25 mM lumenal bath concentrations (Δ).
- 17. Current/voltage curves in NaCl.
- 18. Current/voltage curves in RbCl.
- 19. Current/voltage curves in CsCl.
- 20. Mole fraction experiments at 250 mM total cation concentration in symmetric solutions. (A) NaCl and CsCl mixtures. The experimental point at mole fraction 0.6 is statistically significantly different than the point at mole fraction 1 (p < 0.05). (B) LiCl and KCl mixtures.
- 21. Current/voltage curves in bi-ionic conditions.
- 22. Current/voltage curves with divalent and monovalent cations. (A) KCl and CaCl₂. (B) NaCl and CaCl₂. (C) CsCl and CaCl₂. (D) KCl and MgCl₂. In both baths are 250 mM monovant-Cl and in the lumenal bath is 5 mM (■), 10 mM (□), and 50 mM (▲) divalent-Cl₂ or the baths contain 250 mM cytosolic monovant-Cl and 25 mM lumenal divalent-Cl₂ (Δ). Current/voltage curves of (E) the D4899N (■) and E4900Q (□) mutants and (F) the D4938N mutant in 250 mM symmetric KCl and 10 mM lumenal CaCl₂.





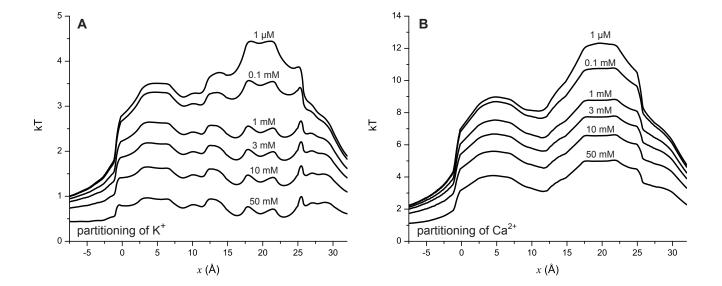
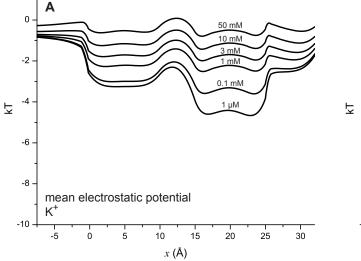
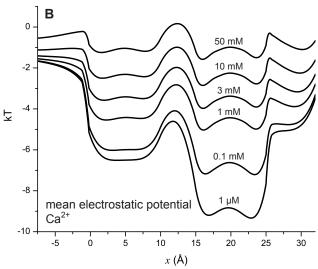
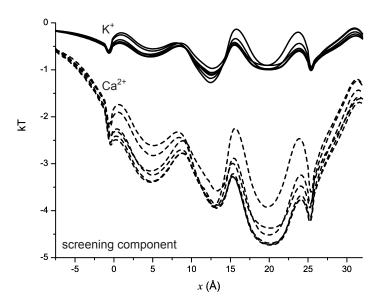
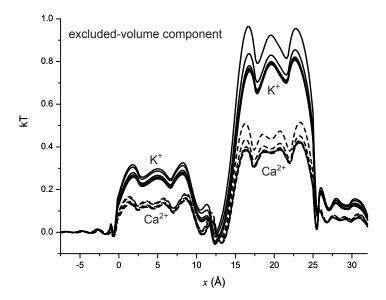


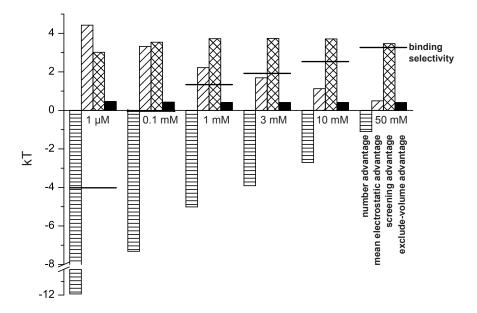
Fig. 3











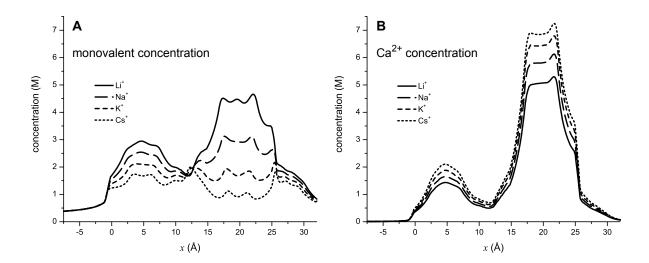


Fig. 8

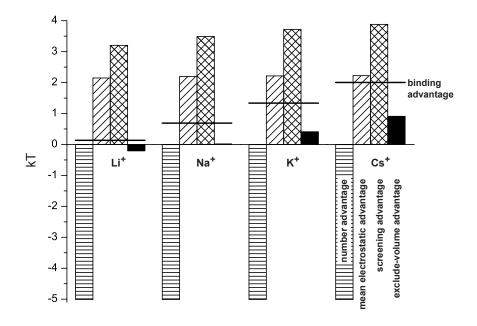
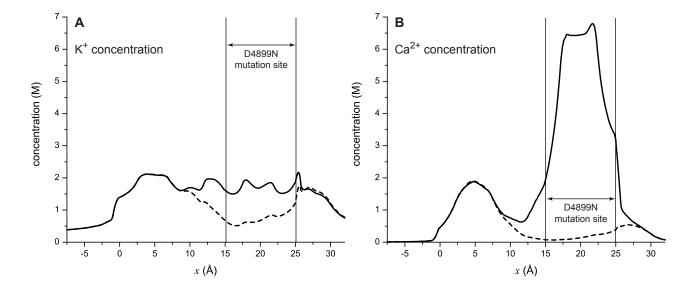


Fig. 9



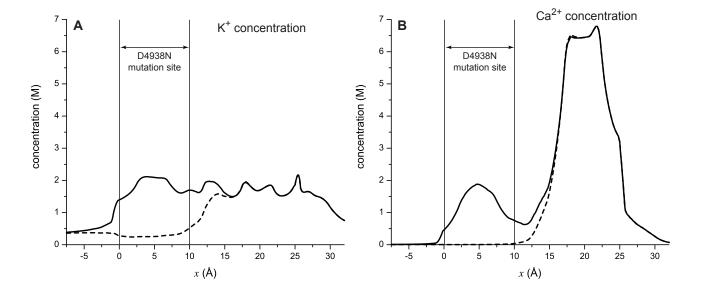
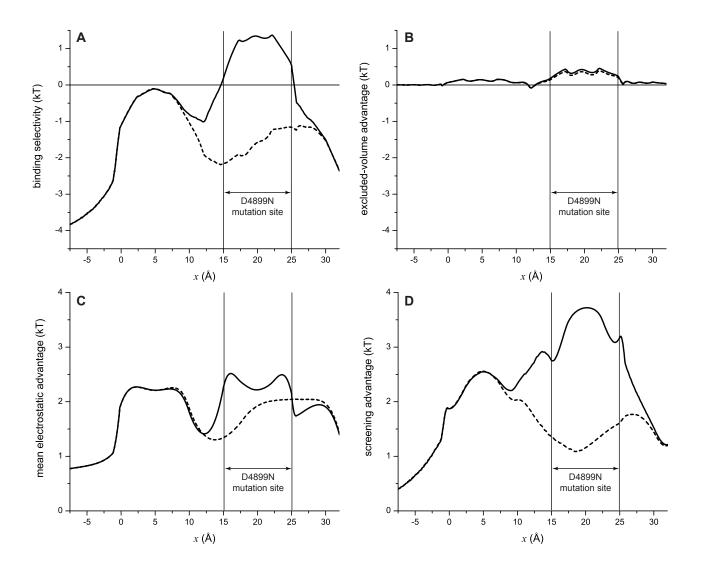


Fig. 11



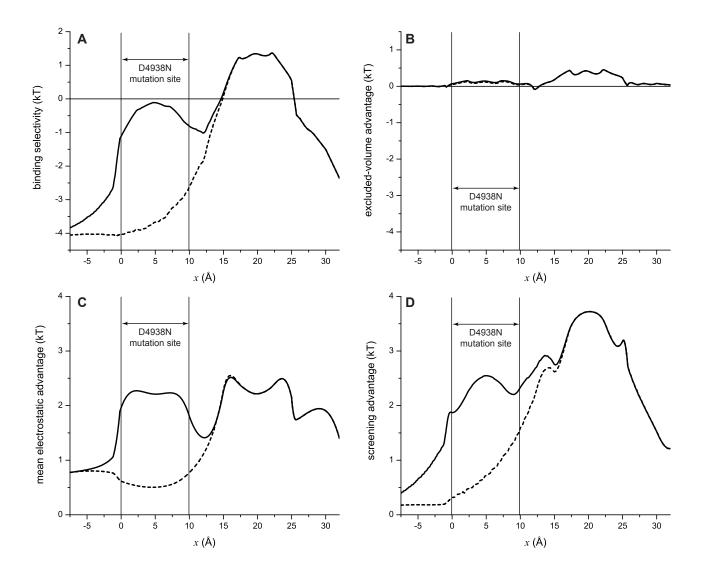


Fig. 13

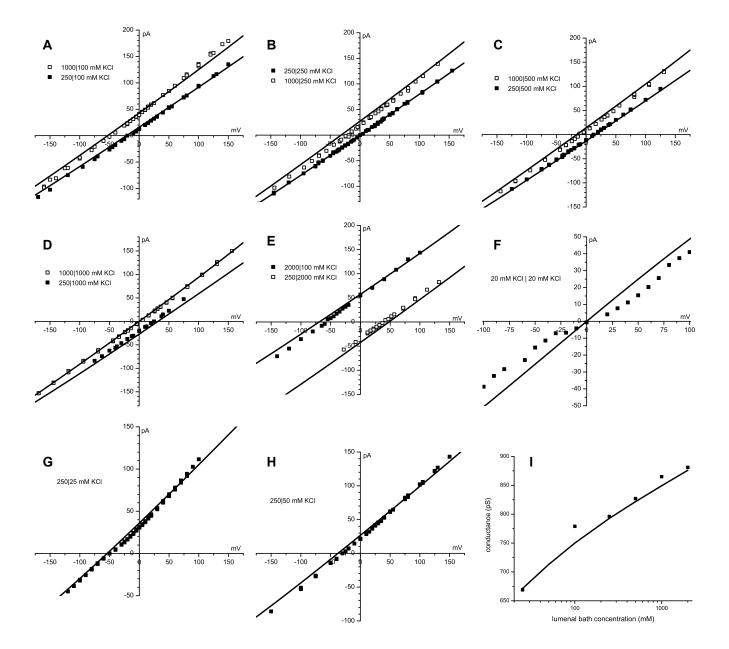
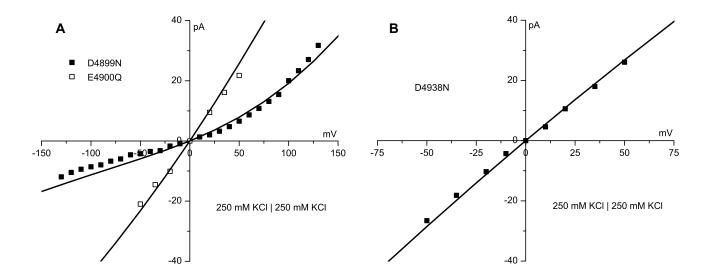
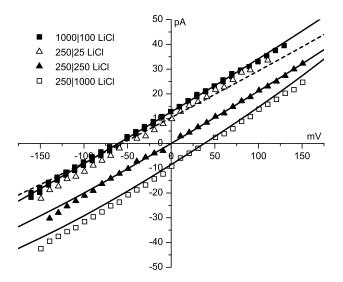
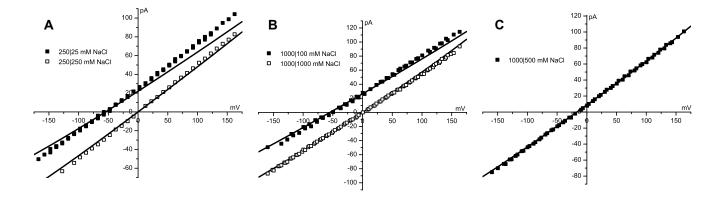
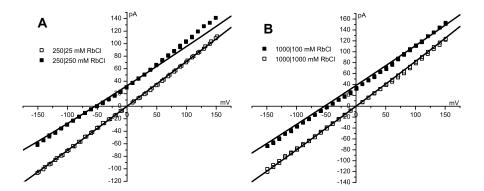


Fig. 14









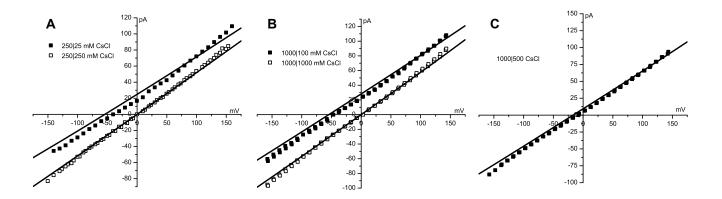
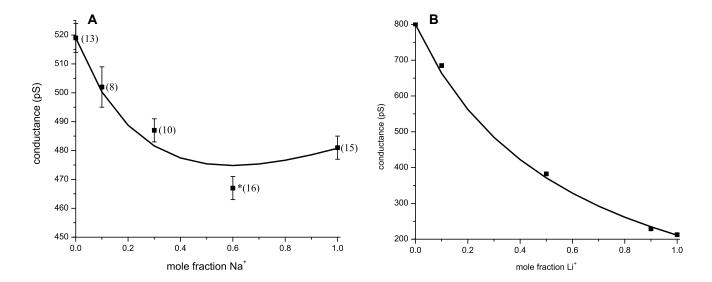


Fig. 19



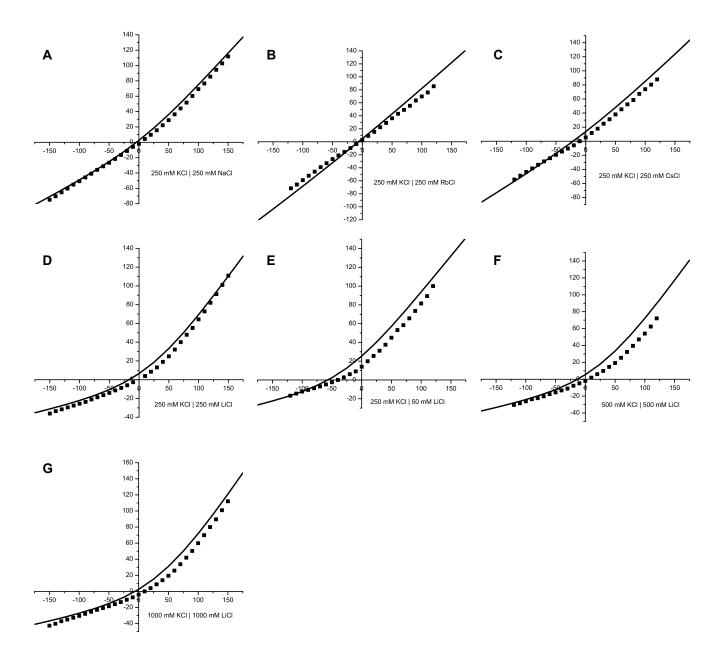


Fig. 21

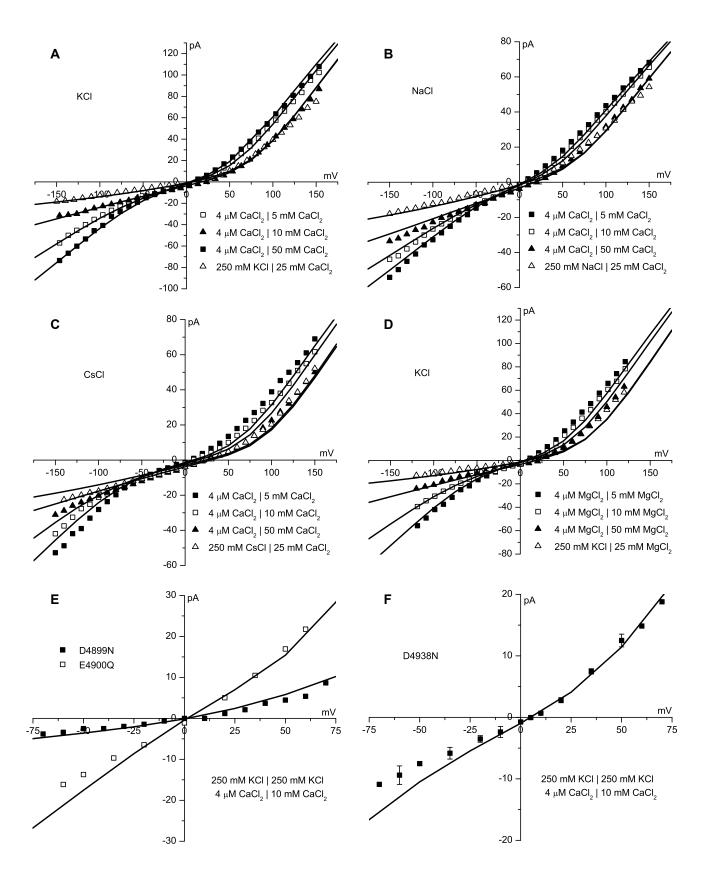


Fig. 22