## Figure Legends

1. The geometry of the model RyR pore. In the experiments and calculations, the lumen of the sarcoplasmic reticulum (SR) is electrically grounded. The circle around each labeled amino acid in meant to illustrate the range of the motion of the terminal carboxyl group. Aspartates (solid circles) are given a radius of $5 \AA$ and glutamates (dashed circles) $7 \AA$. Only the amino acids of one of the four identical RyR subunits is shown. Asp-4945, Asp-4938, Asp-4899, Glu-4900, and Glu-4902 are the only amino acids explicitly modeled in the theory. The GGGIG sequence (4894-4898 in the numbering) at the cytosolic end of the selectivity filter is only a reference point for readers familiar with the RyR sequence.
2. Experimental verification of the AMFE predicted by the theory. The lines are the theory and the symbols are the experimental data with standard error bars and the number of experiments in parentheses. The solid line and symbols are the addition of $\mathrm{Ca}^{2+}$ to $\mathrm{Na}^{+}$and the dashed line and open symbols are the addition of $\mathrm{Ca}^{2+}$ to $\mathrm{Cs}^{+}$. In all cases, the monovalent-chloride concentration was 150 mM in both cytosolic and lumenal baths and the indicated amount $\mathrm{Ca}^{2+}$ was added to the lumenal bath. The current at -20 mV is shown.
3. The partitioning $\ln \left(\rho_{i}(x) / \rho_{i}^{\text {bath }}\right)$ of $\mathrm{K}^{+}$(panel A) and $\mathrm{Ca}^{2+}$ (panel B) from the bath into the pore. $\left[\mathrm{K}^{+}\right]=150 \mathrm{mM}$ and the indicated $\left[\mathrm{Ca}^{2+}\right]$ is in both baths.
4. The electrostatic component of partitioning $z_{i} e \phi(x) / k T$ of $\mathrm{K}^{+}$(panel A) and $\mathrm{Ca}^{2+}$ (panel B) in the pore. $\left[\mathrm{K}^{+}\right]=150 \mathrm{mM}$ and the indicated $\left[\mathrm{Ca}^{2+}\right]$ is in both baths.
5. The screening component of partitioning $\Delta \mu_{\mathrm{i}}^{\mathrm{SC}}(x) / k T$ of $\mathrm{K}^{+}$(solid lines) and $\mathrm{Ca}^{2+}$ (dashed lines) in the pore. $\left[\mathrm{K}^{+}\right]=150 \mathrm{mM}$ and $\left[\mathrm{Ca}^{2+}\right]$ is changed from $1 \mu \mathrm{M}$ to 50 mM . Because the curves are so close together $\left[\mathrm{Ca}^{2+}\right]$ is not indicated.
6. The excluded-volume (hard-sphere) component of partitioning $\Delta \mu_{i}^{\mathrm{HS}}(x) / k T$ of $\mathrm{K}^{+}$ (solid lines) and $\mathrm{Ca}^{2+}$ (dashed lines) in the pore. $\left[\mathrm{K}^{+}\right]=150 \mathrm{mM}$ and $\left[\mathrm{Ca}^{2+}\right]$ is changed from $1 \mu \mathrm{M}$ to 50 mM . Because the curves are so close together $\left[\mathrm{Ca}^{2+}\right]$ is not indicated.
7. Components of the binding selectivity from Eq. (6) in the selectivity filter ( $x=20$ $\AA$ in Fig. 1 that shows the geometry of the pore). $\left[\mathrm{K}^{+}\right]=150 \mathrm{mM}$ and the indicated $\left[\mathrm{Ca}^{2+}\right]$ is in both baths. The horizontal-hatched bar is the number advantage, the diagonal-hatched bar is the mean electrostatic advantage, the crosshatched bar is the screening advantage, and the solid bar is the excluded-volume advantage. The horizontal line is the binding selectivity of Eq. (6) (i.e., the sum of all the terms). A positive term favors the binding of $\mathrm{Ca}^{2+}$ while a negative term favors $\mathrm{K}^{+}$.
8. Concentration profiles in the pore of the monovalent cation (panel A) and $\mathrm{Ca}^{2+}$ (panel B). For each indicated monovalent cation $\mathrm{X}^{+},\left[\mathrm{X}^{+}\right]=150 \mathrm{mM}$ and $\left[\mathrm{Ca}^{2+}\right]=$ 1 mM in both baths.
9. Components of the binding selectivity from Eq. (6) in the selectivity filter ( $x=20$ $\AA$ in Fig. 1 that shows the geometry of the pore). For each indicated monovalent cation $\mathrm{X}^{+},\left[\mathrm{X}^{+}\right]=150 \mathrm{mM}$ and $\left[\mathrm{Ca}^{2+}\right]=1 \mathrm{mM}$ in both baths. Ion diameters: $\mathrm{Li}^{+}$ $1.33 \AA ; \mathrm{Na}^{+} 2.00 \AA ; \mathrm{K}^{+} 2.76 \AA ; \mathrm{Cs}^{+} 3.42 \AA$. The horizontal-hatched bar is the number advantage, the diagonal-hatched bar is the mean electrostatic advantage,
the cross-hatched bar is the screening advantage, and the solid bar is the excludedvolume advantage. The horizontal line is the binding selectivity of Eq. (6) (i.e., the sum of all the terms). A positive term favors the binding of $\mathrm{Ca}^{2+}$ while a negative term favors $\mathrm{K}^{+}$.
10. Concentration profiles in the pore of $\mathrm{K}^{+}$(panel A) and $\mathrm{Ca}^{2+}$ (panel B) for the native (WT) channel (solid line) and the mutation D4899N (dashed line). $\left[\mathrm{K}^{+}\right]=$ 150 mM and $\left[\mathrm{Ca}^{2+}\right]=1 \mathrm{mM}$ in both baths. In the model, the mutation is created by "turning off" the charge on the four Asp-4899. The mutation site is the region from which the charge on the four Asp-4899 has been removed.
11. Concentration profiles in the pore of $\mathrm{K}^{+}$(panel A) and $\mathrm{Ca}^{2+}$ (panel B) for the native (WT) channel (solid line) and the mutation D4938N (dashed line). $\left[\mathrm{K}^{+}\right]=$ 150 mM and $\left[\mathrm{Ca}^{2+}\right]=1 \mathrm{mM}$ in both baths. In the model, the mutation is created by "turning off" the charge on the four Asp-4938. The mutation site is the region from which the charge on the four Asp-4938 has been removed.
12. Profiles of the binding selectivity from Eq. (6) (panel A) and its components (excluded volume, panel B ; mean electrostatic, panel C; screening, panel D) for the native (WT) channel (solid line) and the mutation D4899N (dashed line). The conditions are those described in Fig. 9.
13. Profiles of the binding selectivity from Eq. (6) (panel A) and its components (excluded volume, panel B; mean electrostatic, panel C; screening, panel D) for the native (WT) channel (solid line) and the mutation D4938N (dashed line). The conditions are those described in Fig. 10.
14. Current/voltage curves in $\mathrm{KCl}(\mathrm{A}-\mathrm{H})$. (I) The conductance at reversal potential with cytosolic $\left[\mathrm{K}^{+}\right]$is held at 250 mM and lumenal $\left[\mathrm{K}^{+}\right]$is varied. For both experiment and theory the current/voltage was fitted with a line and the slope is plotted. In this and the following figures, concentrations are listed as cytosolic | lumenal. The solid lines are the model and symbols are the experimental data.
15. Current/voltage curves of (A) the D4899N (■) and E4900Q (ם) mutants and (B) the D 4938 N mutant in 250 mM symmetric KCl .
16. Current/voltage curves in LiCl . The dashed line is the model result for 250 mM cytosolic and 25 mM lumenal bath concentrations ( $\Delta$ ).
17. Current/voltage curves in NaCl .
18. Current/voltage curves in RbCl .
19. Current/voltage curves in CsCl .
20. Mole fraction experiments at 250 mM total cation concentration in symmetric solutions. (A) NaCl and CsCl mixtures. The experimental point at mole fraction 0.6 is statistically significantly different than the point at mole fraction 1 ( $p<$ 0.05 ). (B) LiCl and KCl mixtures.
21. Current/voltage curves in bi-ionic conditions.
22. Current/voltage curves with divalent and monovalent cations. (A) KCl and $\mathrm{CaCl}_{2}$. (B) NaCl and $\mathrm{CaCl}_{2}$. (C) CsCl and $\mathrm{CaCl}_{2}$. (D) KCl and $\mathrm{MgCl}_{2}$. In both baths are 250 mM monovant- Cl and in the lumenal bath is $5 \mathrm{mM}(\mathbf{\square}), 10 \mathrm{mM}$ (ロ), and 50 $\mathrm{mM}(\mathbf{\Delta})$ divalent- $\mathrm{Cl}_{2}$ or the baths contain 250 mM cytosolic monovant- Cl and 25 mM lumenal divalent-Cl $\mathrm{C}_{2}(\Delta)$. Current/voltage curves of (E) the D4899N (■) and E4900Q (ㅁ) mutants and (F) the D4938N mutant in 250 mM symmetric KCl and 10 mM lumenal $\mathrm{CaCl}_{2}$.


Fig. 14


Fig. 15


Fig. 16


Fig. 17


Fig. 18


Fig. 19


Fig. 20


Fig. 21


Fig. 22

